

Machine Learning for Fundamental Physics

Benjamin Nachman

Lawrence Berkeley National Laboratory

bpnachman.com

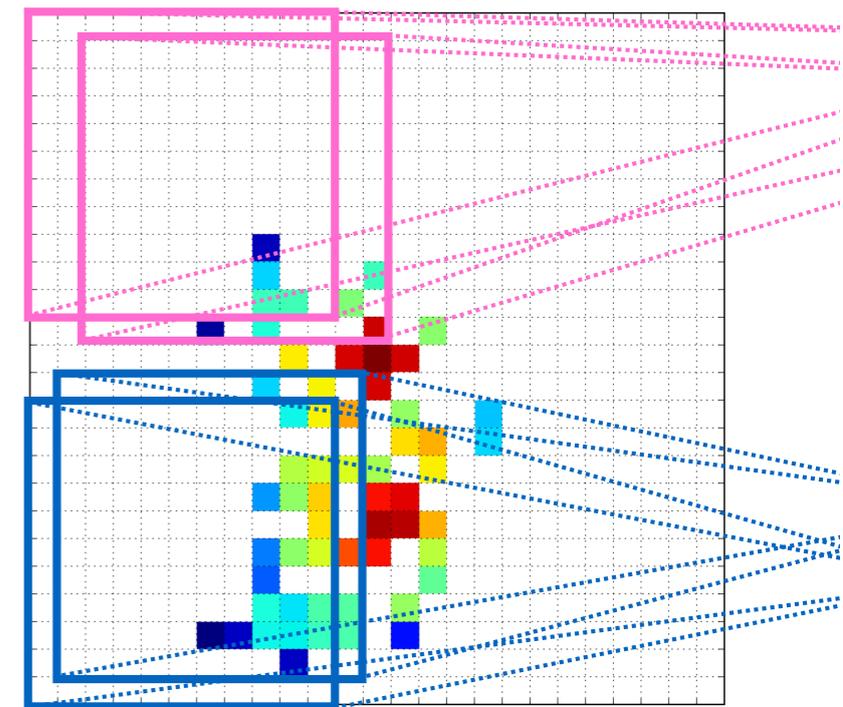
bpnachman@lbl.gov



@bpnachman



bnachman



Yale
Physics Club
October 2022

Questions in fundamental physics



Theoretical and experimental questions motivate a deep exploration **of the fundamental structure of nature**

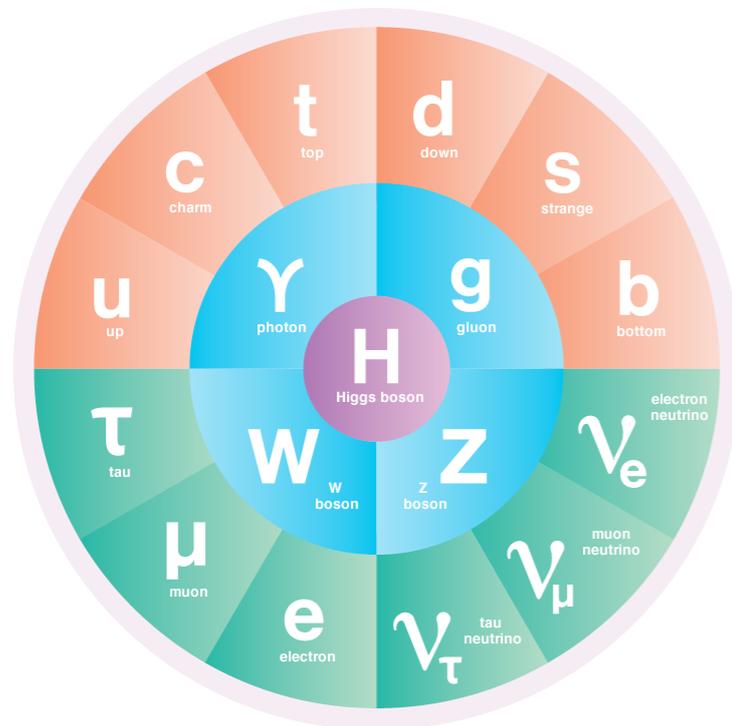
Questions in fundamental physics

3

Theoretical and experimental questions motivate a deep exploration **of the fundamental structure of nature**

Why is the Higgs boson so light?

Hierarchy problem



See also: quantum gravity

Questions in fundamental physics

4

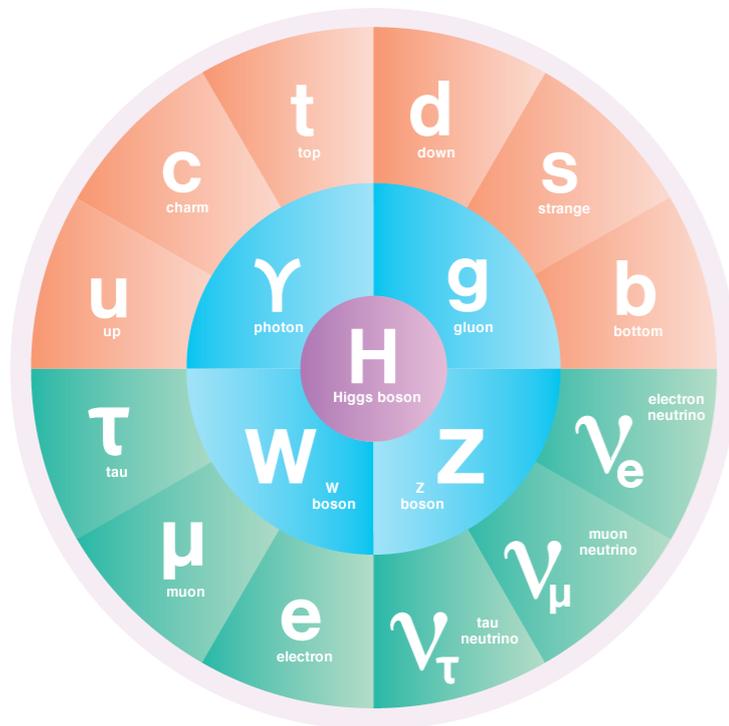
Theoretical and experimental questions motivate a deep exploration **of the fundamental structure of nature**

Why is the Higgs boson so light?

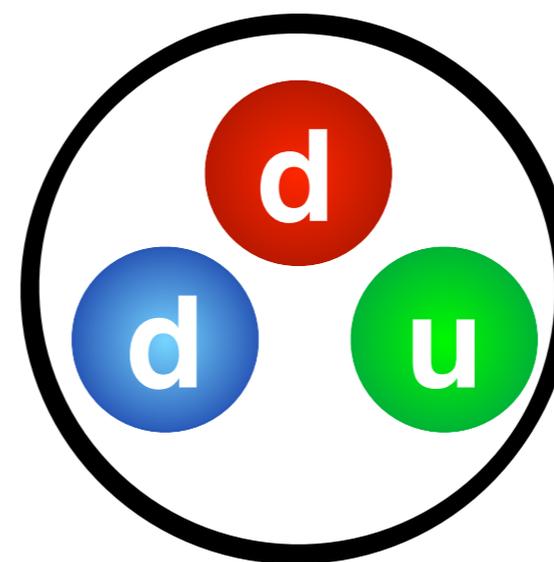
Hierarchy problem

Why do neutrons have no dipole moment?

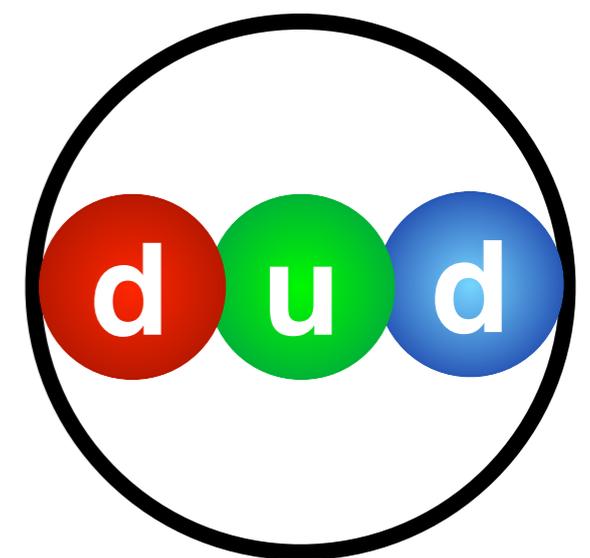
Strong CP



See also: quantum gravity



>99% of pictures on the internet



Reality

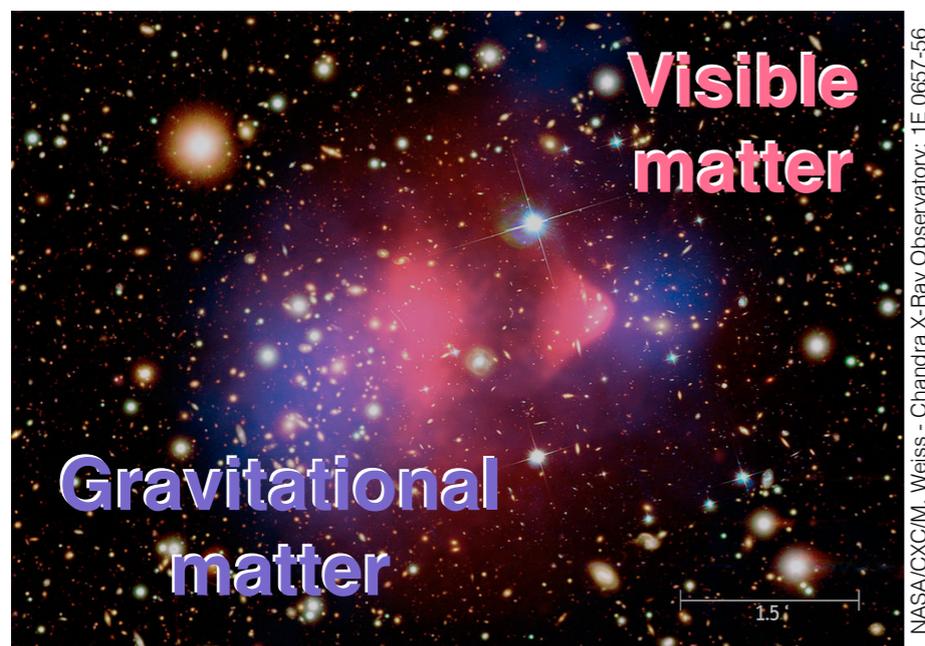
Questions in fundamental physics

5

Theoretical and **experimental** questions motivate a deep exploration **of the fundamental structure of nature**

What is the extra
gravitational matter?

Dark Matter



See also: dark energy

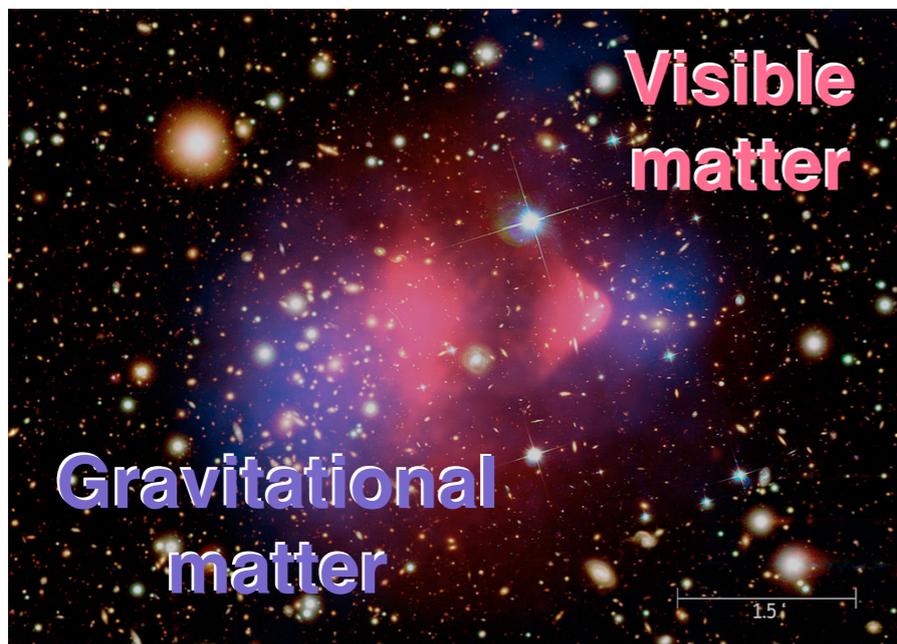
Questions in fundamental physics

6

Theoretical and **experimental** questions motivate a deep exploration **of the fundamental structure of nature**

What is the extra gravitational matter?

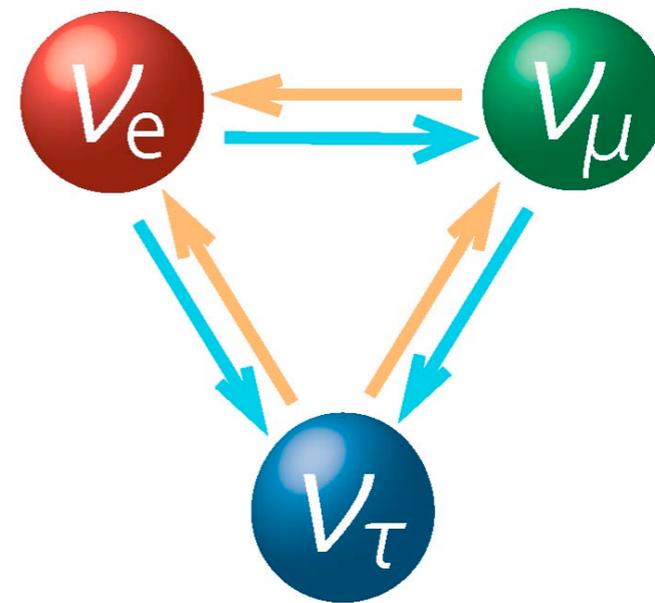
Dark Matter



See also: dark energy

Why do neutrinos have a mass?

Flavor puzzles



See also: Where did all the anti-particles go? (Baryogenesis)

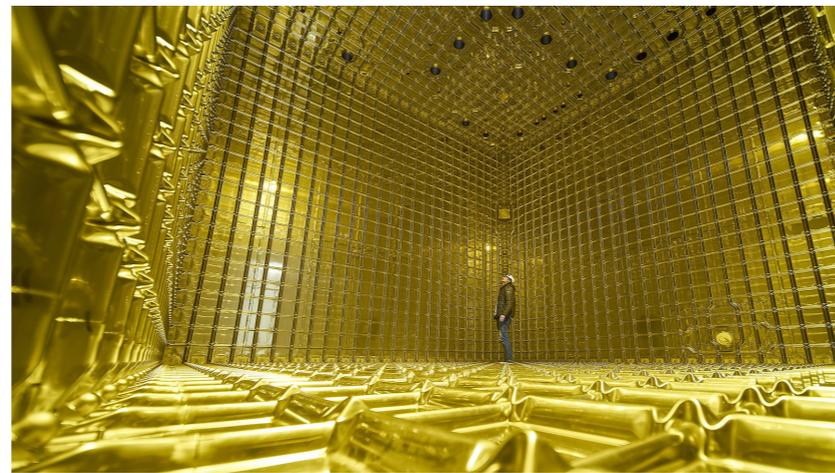
Addressing the questions



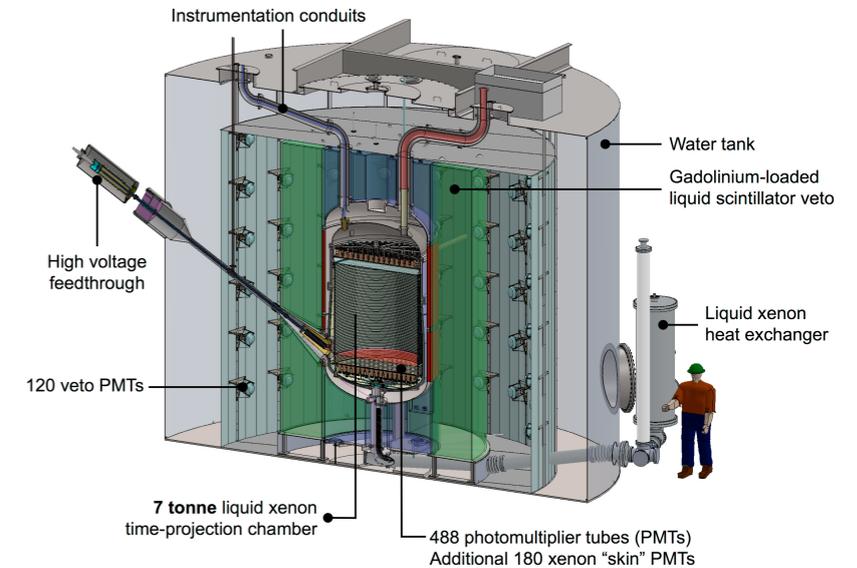
Dark matter/energy
with Vera Rubin,
CMB-S4, ...



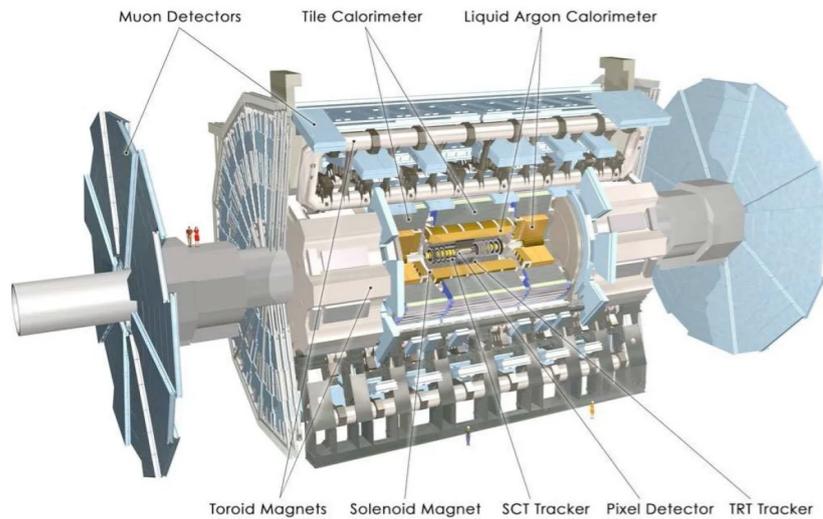
Fermilab, KEK neutrino
experiments, ...



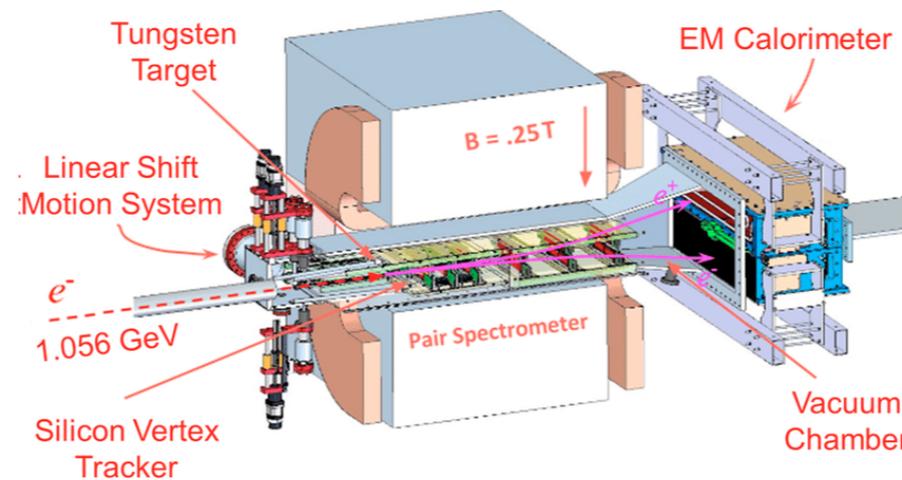
Dark Matter with
LZ, XENON, ...



Large Hadron Collider



Heavy Photon Search, ...



+ others !

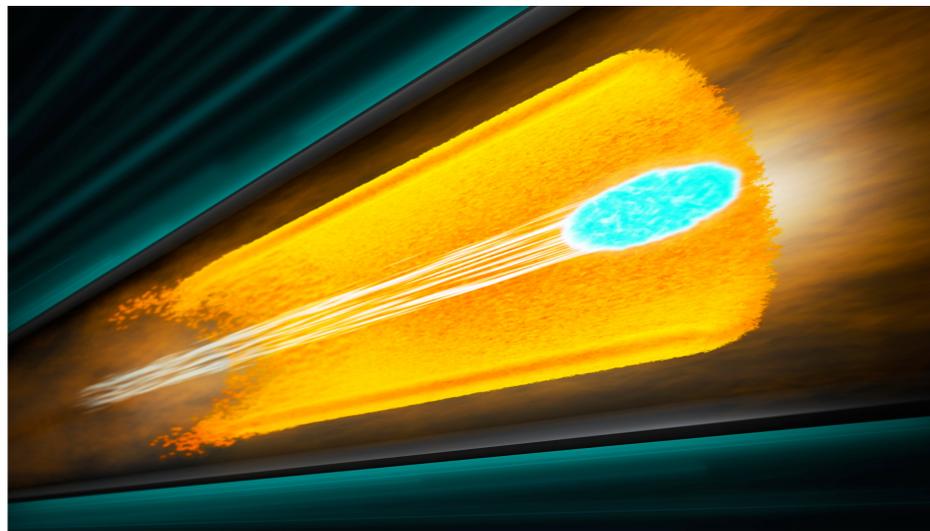
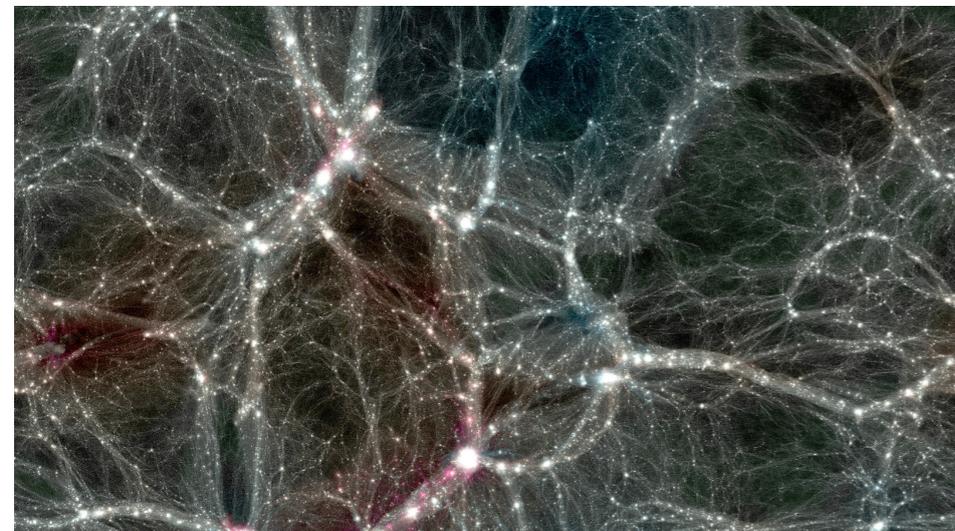
Addressing the questions



N-body simulations

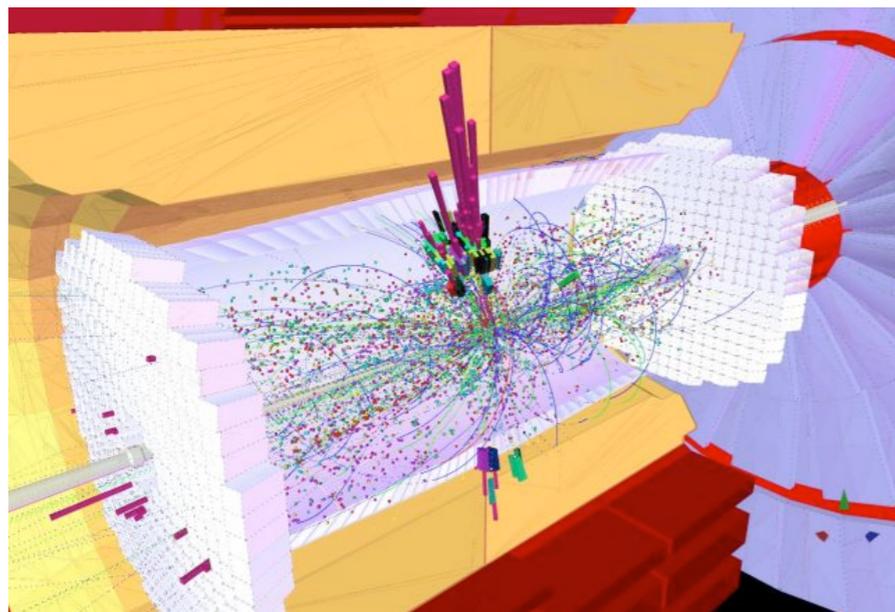
Advanced accelerators

Supercomputers



Material interactions with Geant4

Theory Calculations



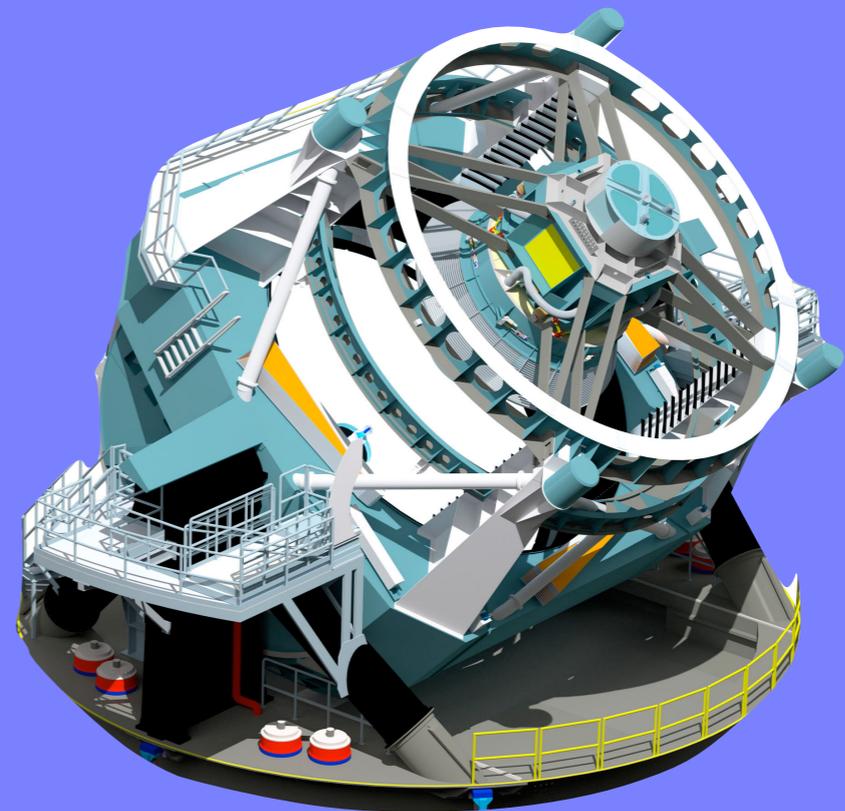
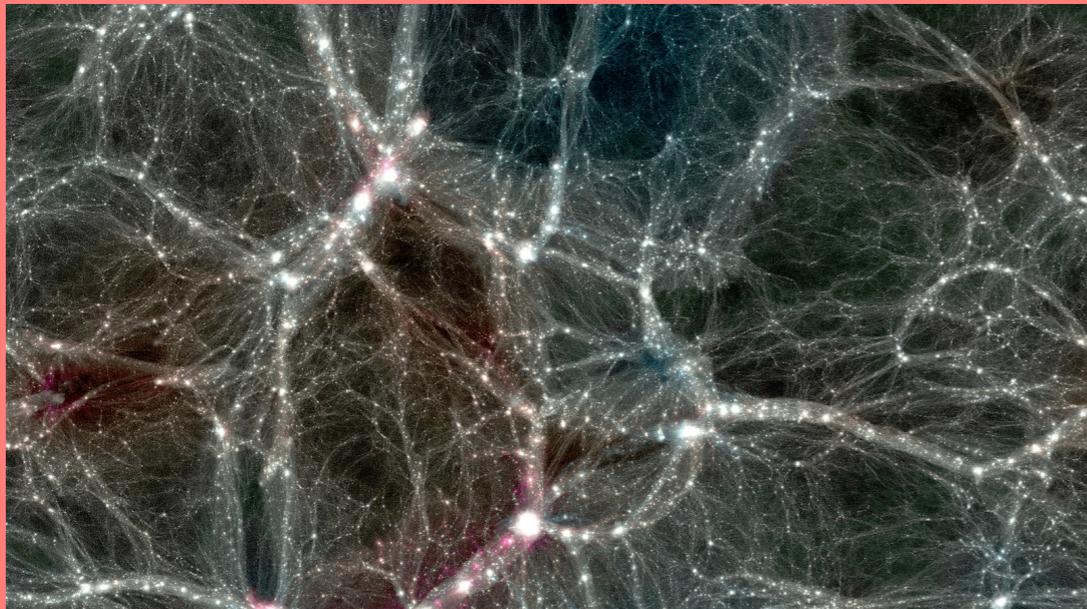
$$2\text{Im} \left(\text{Diagram with wavy line and dashed line} \right) = \int d\Pi \left| \text{Diagram with wavy line} \right|^2$$

+ others !

A *hyper* challenge



Key **challenge** and **opportunity**: *hypervariate phase space*
& *hyper spectral data*



A *hyper* challenge

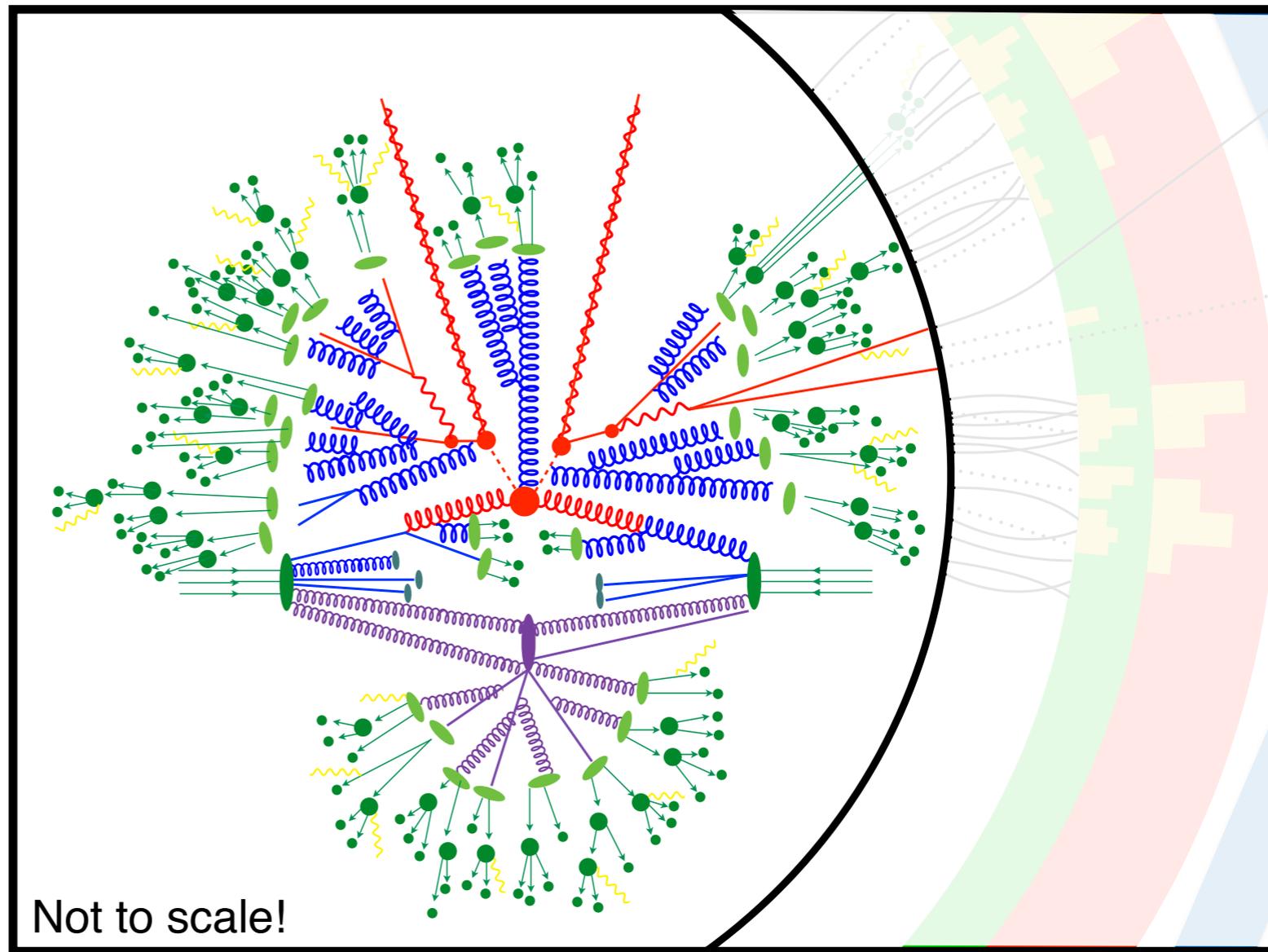
10

Key **challenge** and **opportunity**: *hypervariate phase space*
& *hyper spectral data*

Typical collision events
at the LHC produce
O(1000+) particles

We detect these
particles with
O(100 M)
readout channels

Image inspired by JHEP 02 (2009) 007



Not to scale!

A *hyper* challenge

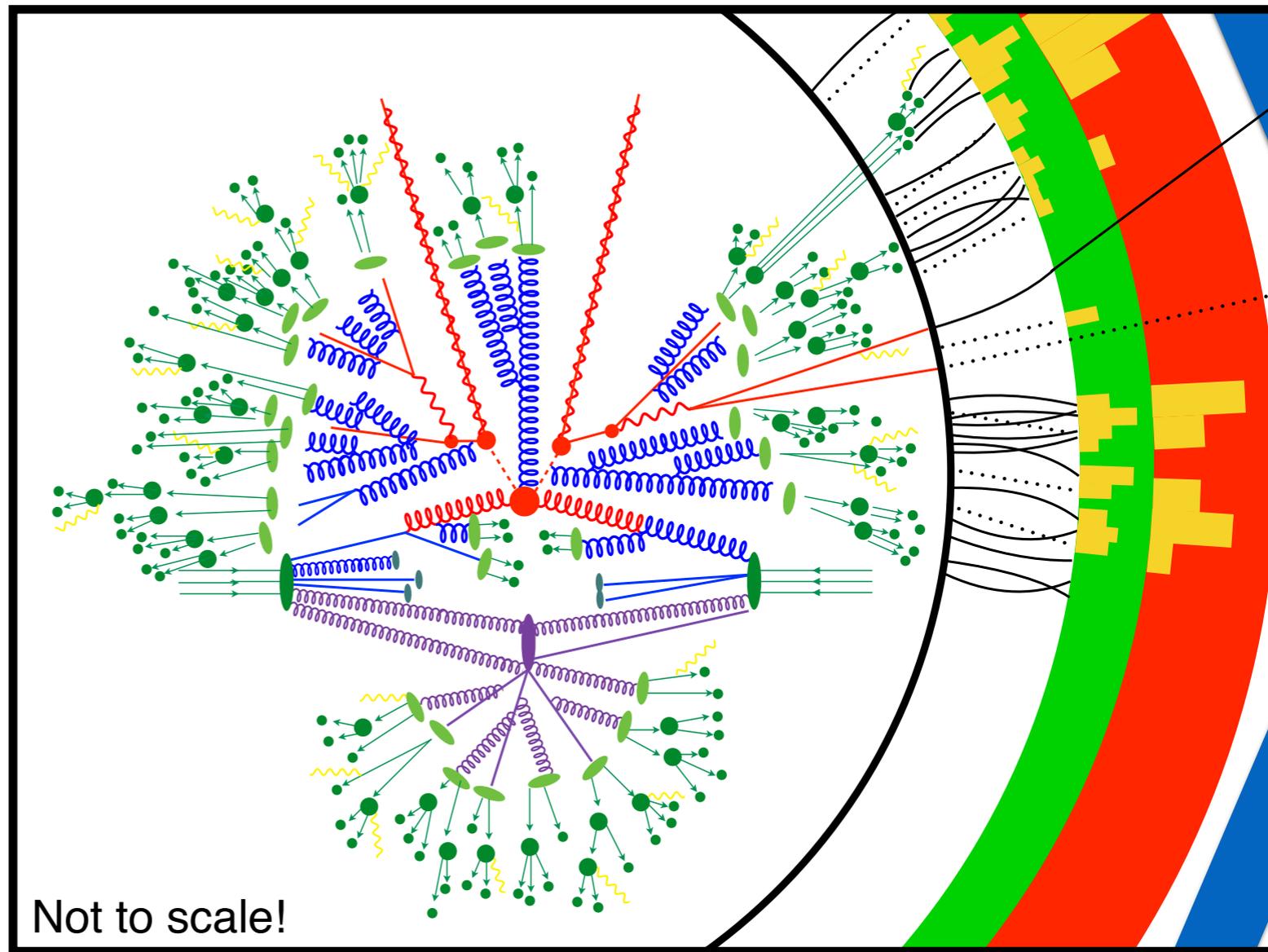
11

Key **challenge** and **opportunity**: *hypervariate phase space*
& *hyper spectral data*

Typical collision events
at the LHC produce
O(1000+) particles

We detect these
particles with
O(100 M)
readout channels

Image inspired by JHEP 02 (2009) 007



Not to scale!

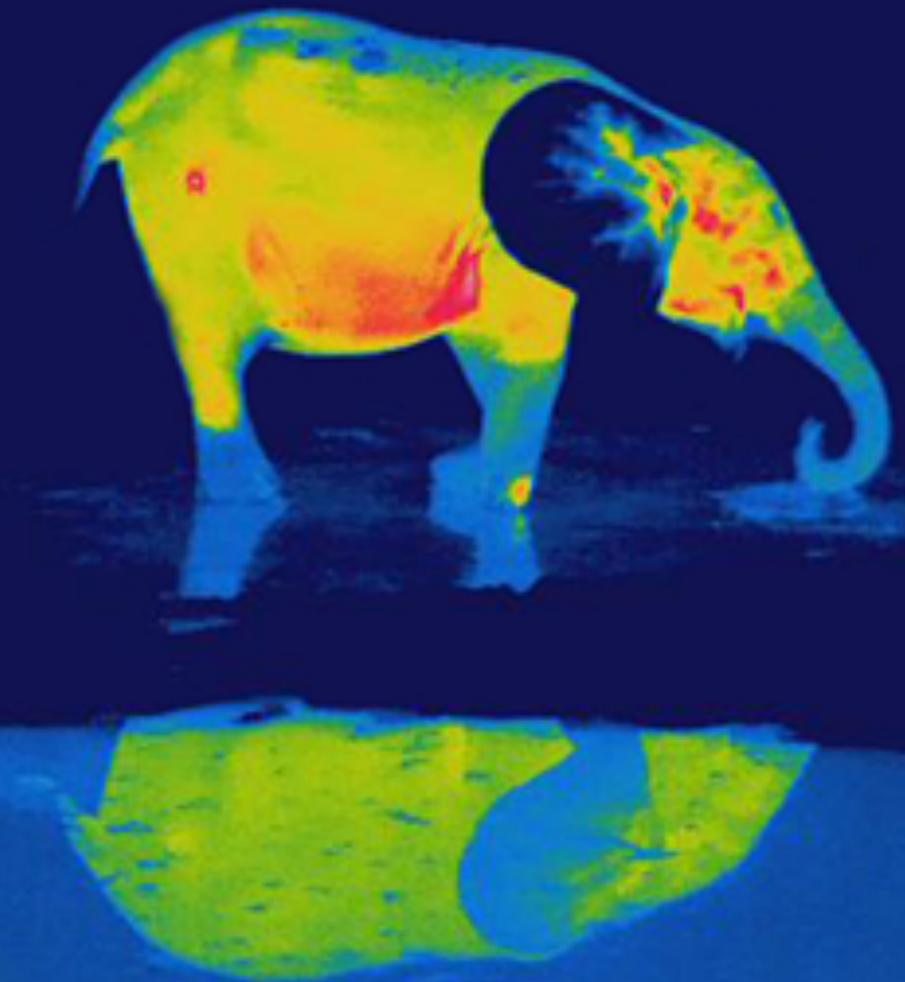
Hypervariate vision with deep learning

12

We have been conducting “multivariate” analysis of collision events for many years

However, recent advances have opened up a **new way** of looking at our data. This **hypervariate vision** will lead to a deeper understanding of nature and perhaps surprises along the way...

Everyone is aware that there must be new physics, but maybe we need hypervariate vision to see it?

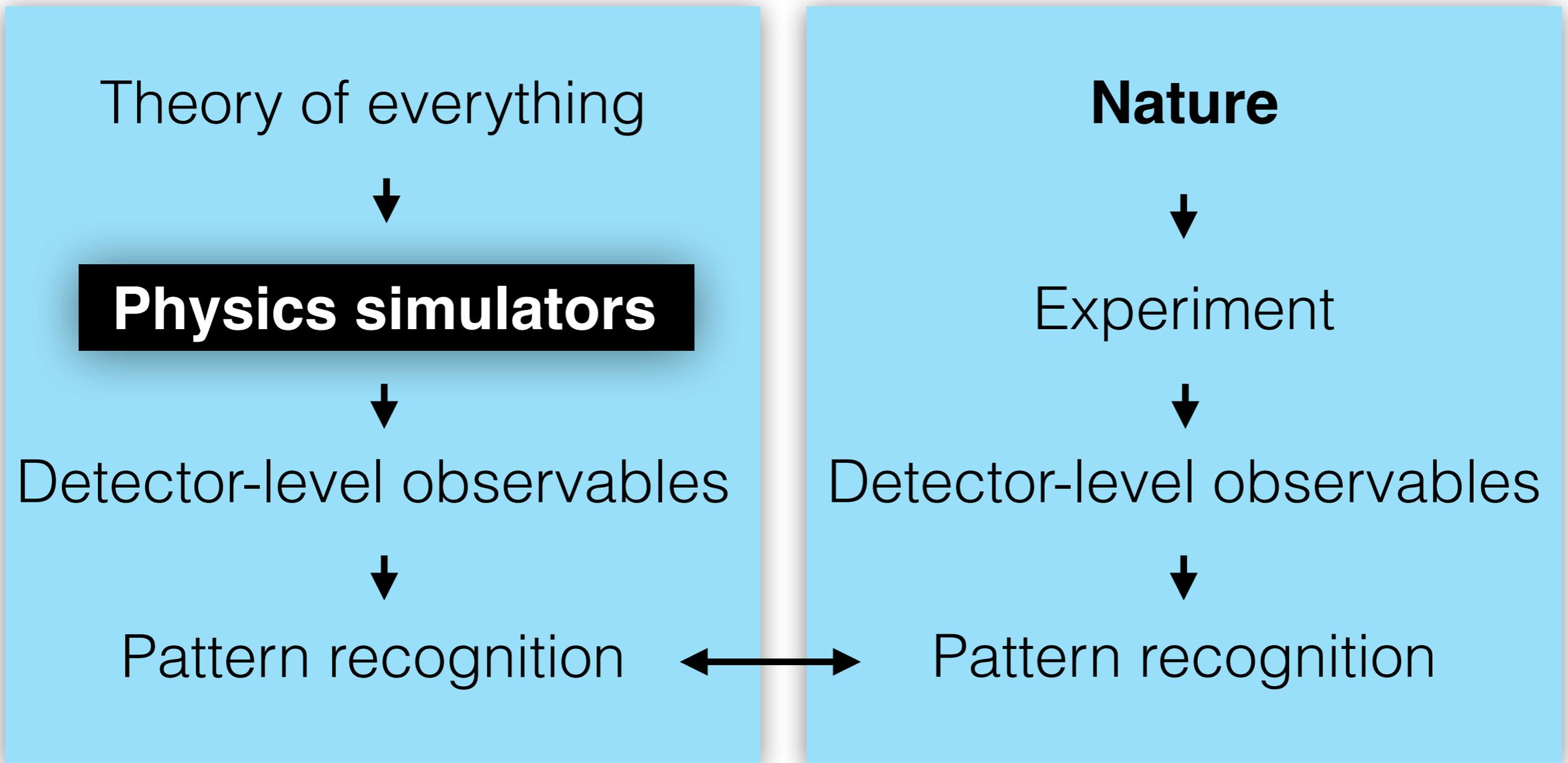


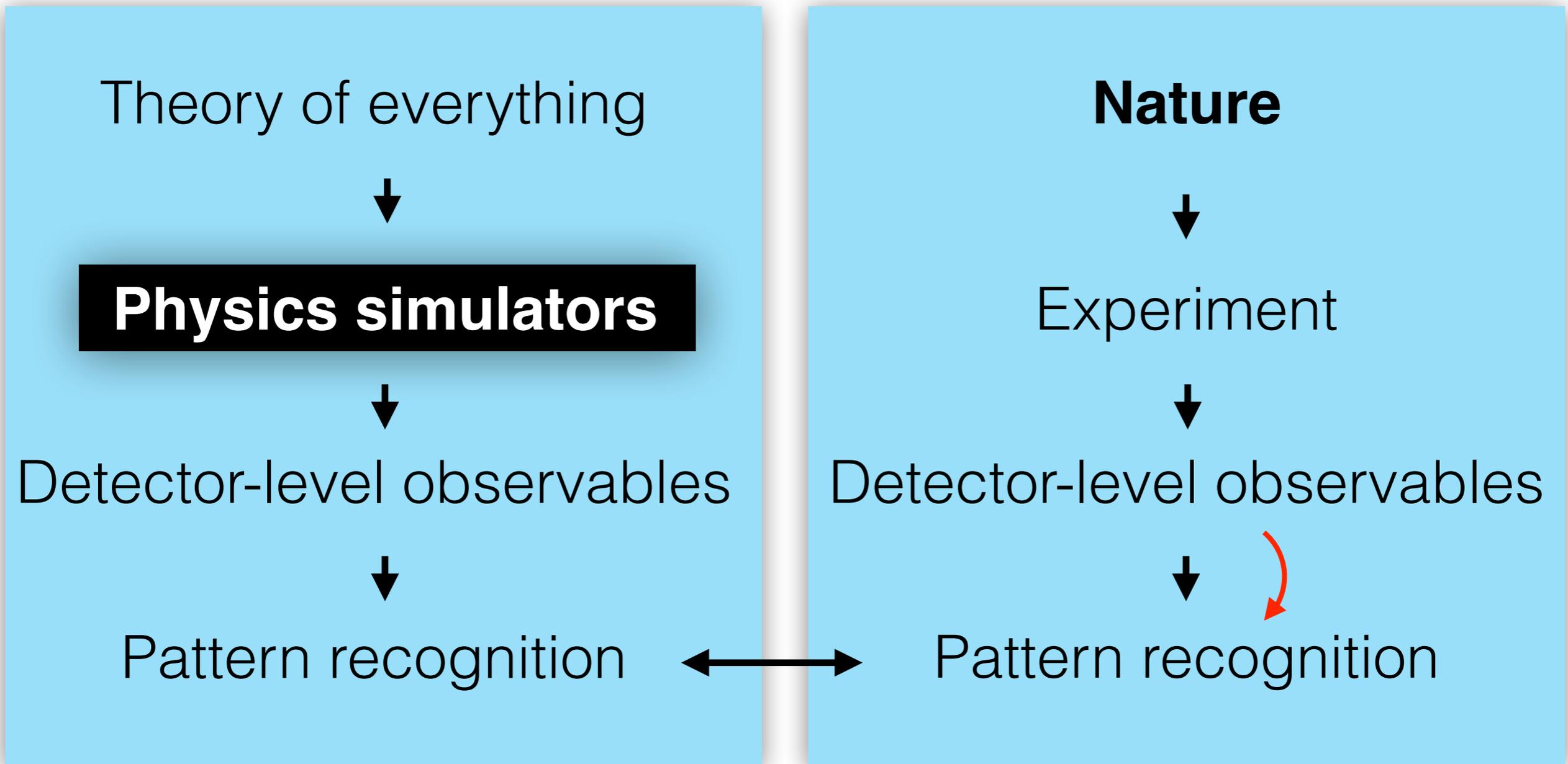
Hypervariate vision with deep learning

13

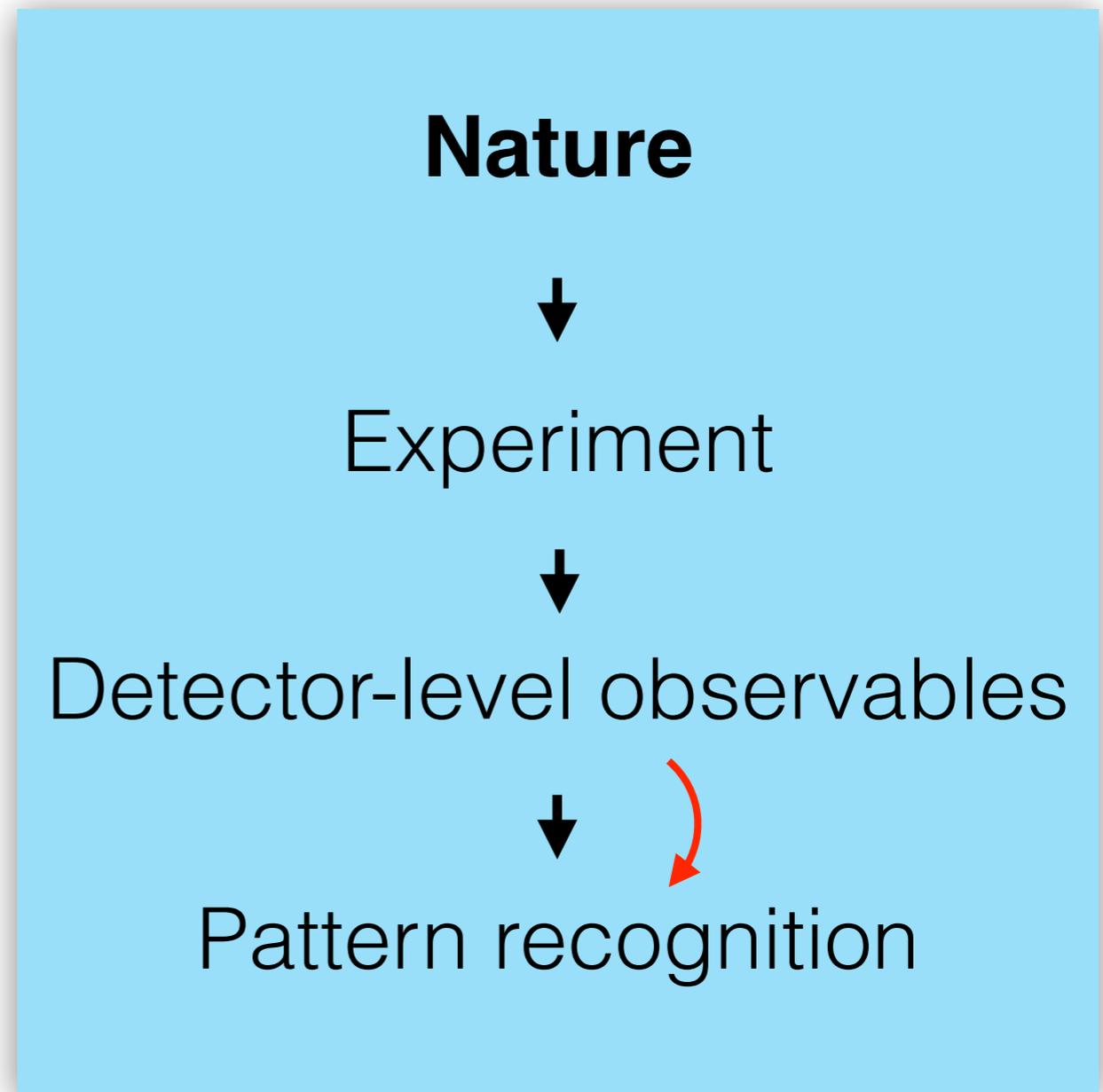
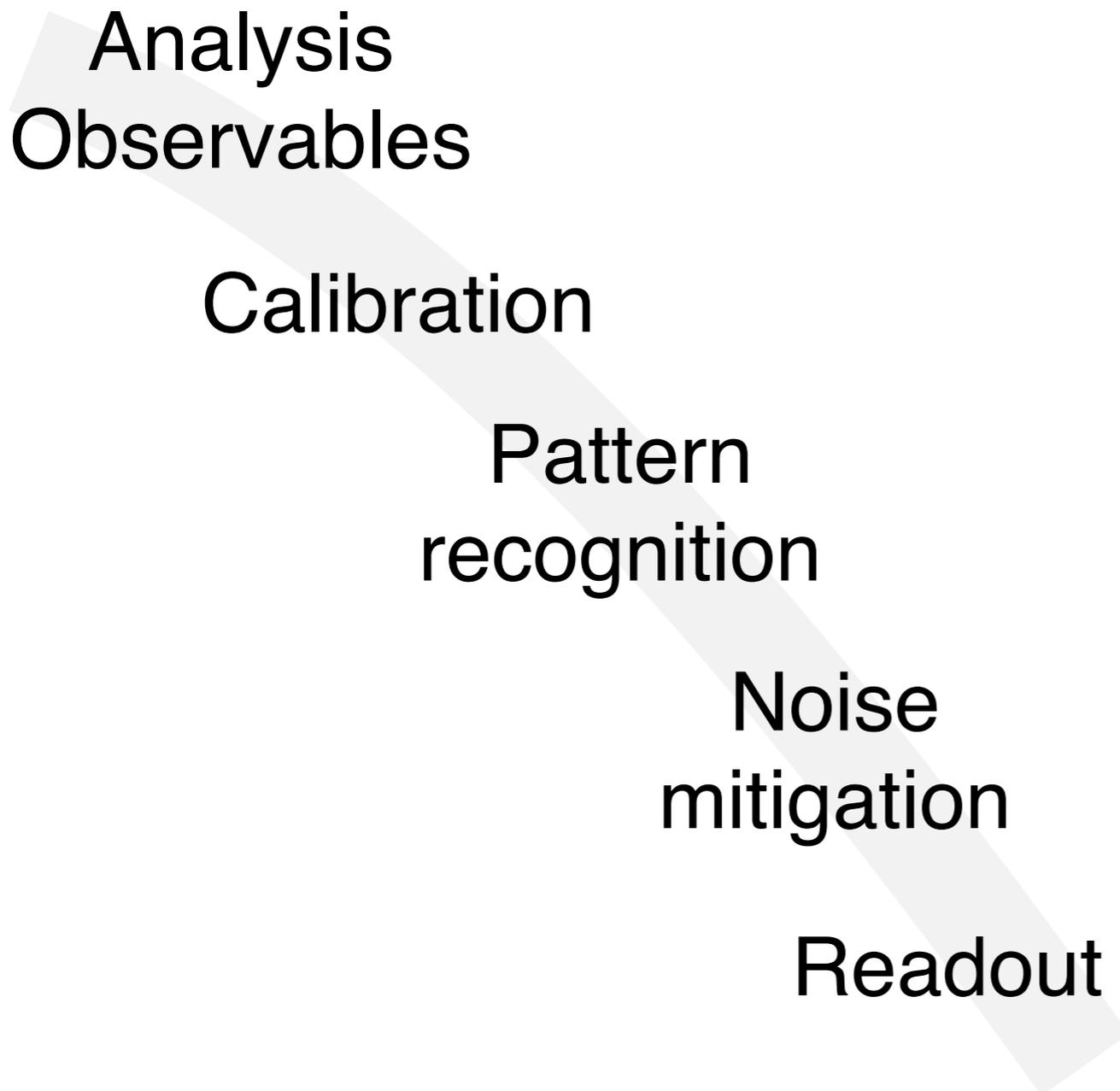
We need innovative computational techniques to make the **data-driven discoveries of the future.**

*This is not just about improving precision,
it is about enabling new science!*





This is where most machine learning is being applied.



This is where most machine learning is being applied.
I won't discuss this area at all for the remainder of the talk

Data analysis in fundamental physics

17

Lorentz Covariant Networks

S. Qiu, S. Han, X. Ju, **BN**, H. Wang
2203.05687

Algorithmic fairness ("decorrelation")

O. Kitouni, **BN**, C. Weisser, M. Williams
JHEP 04 (2021) 70, 2010.09745

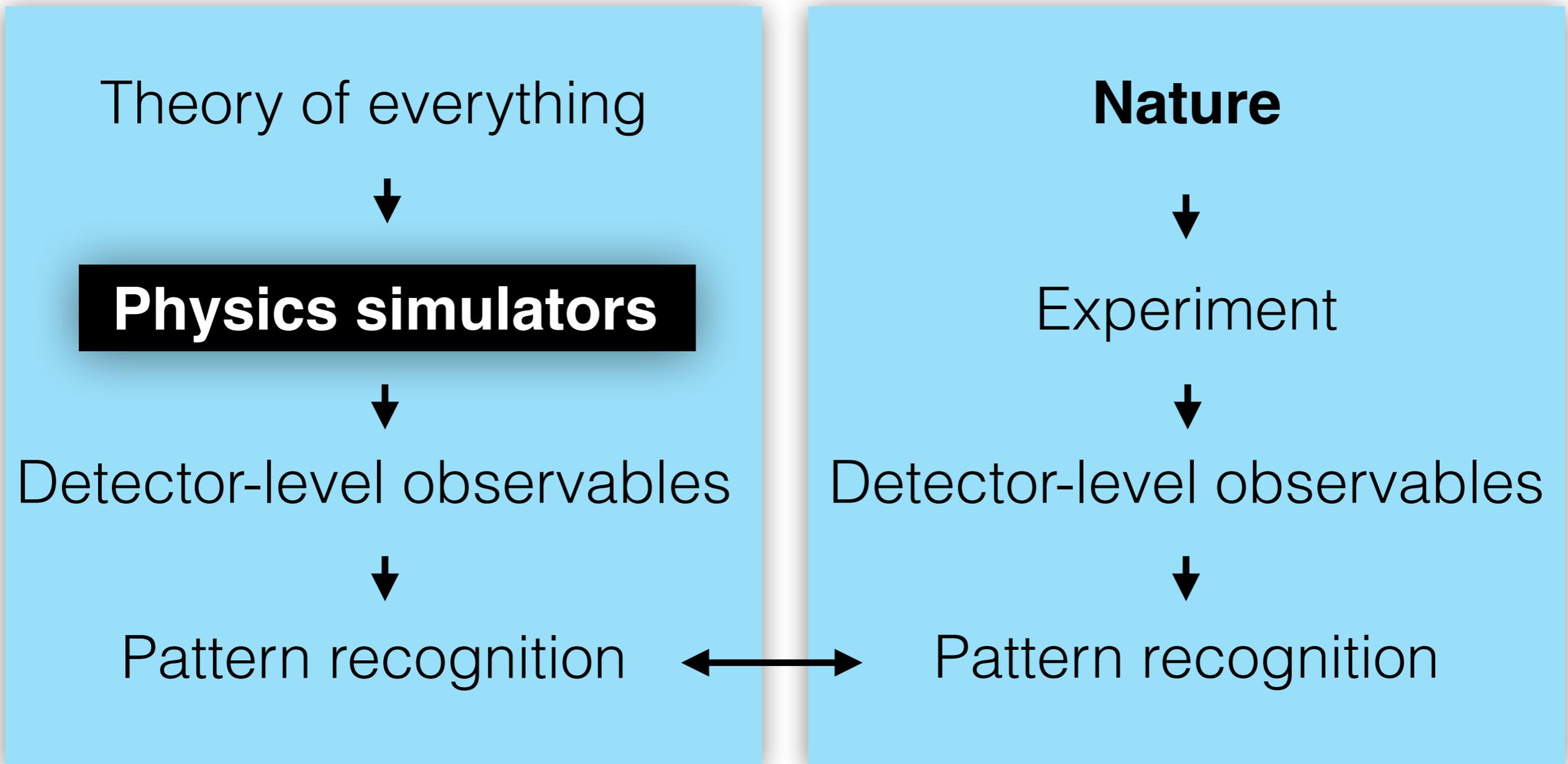
Uncertainty-aware learning

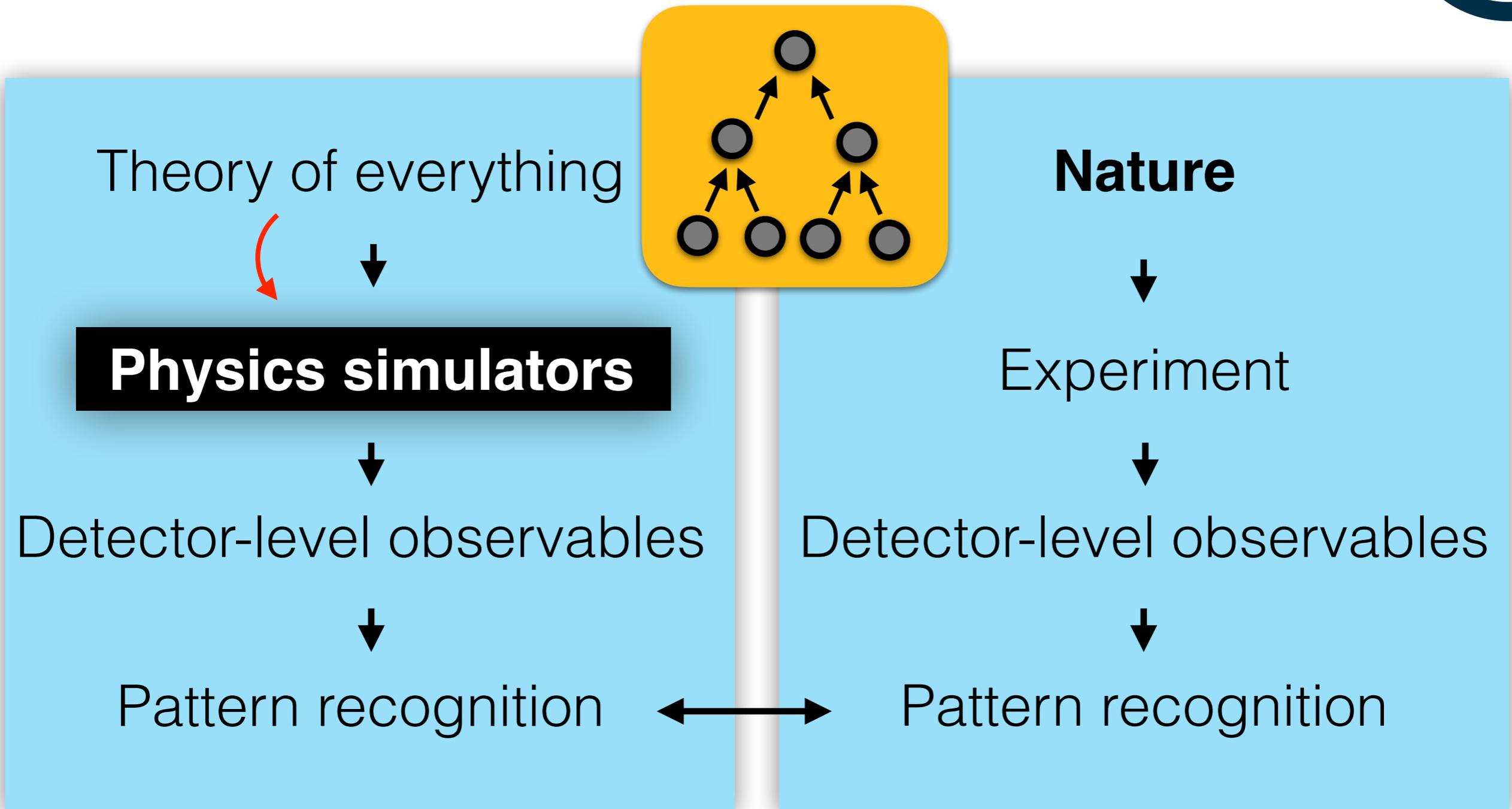
A. Ghosh, **BN**, D. Whiteson
PRD 104 (2021) 056025, 2105.08742

Symmetry Discovery

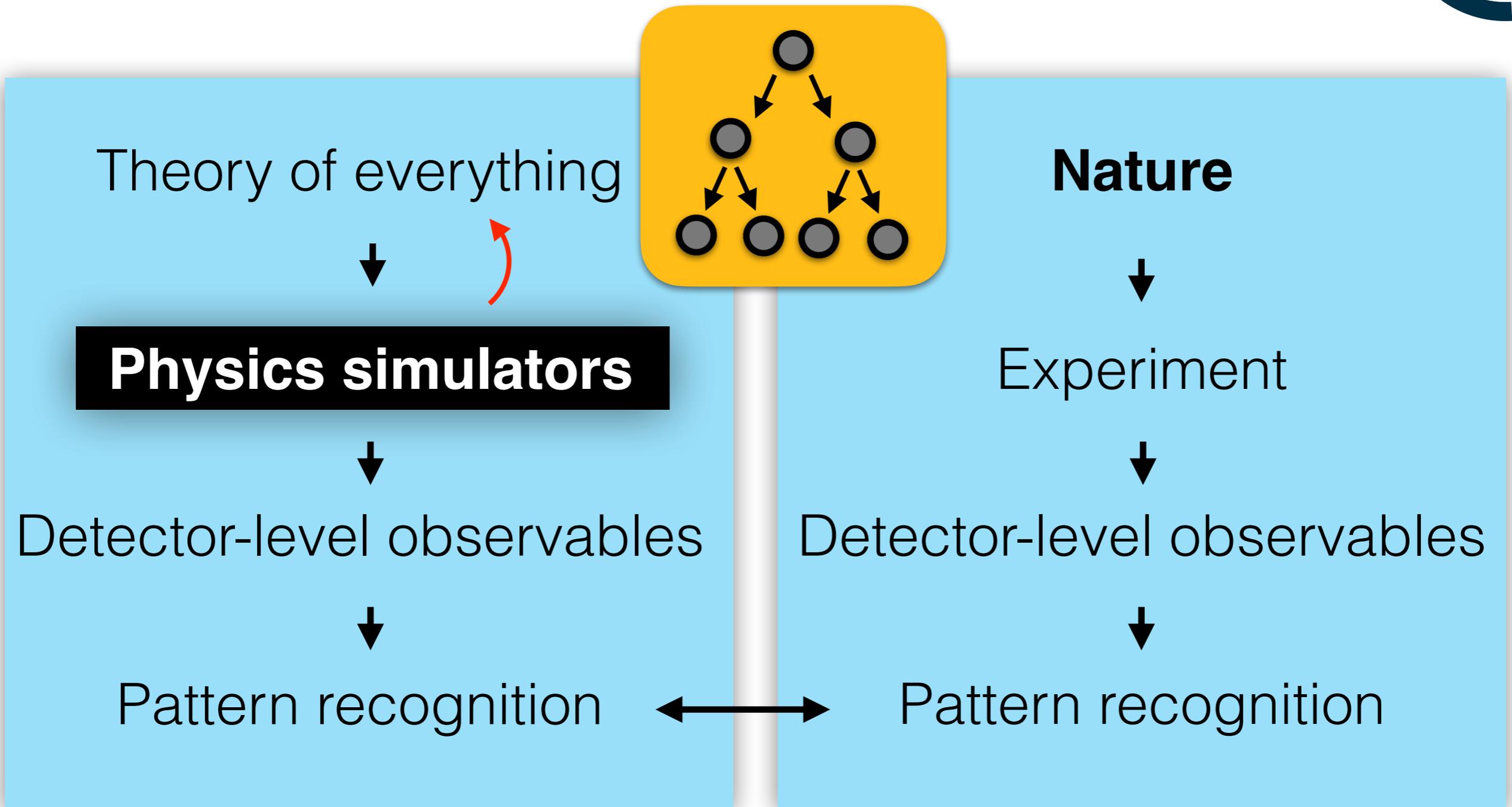
K. Desai, **BN**, J. Thaler
PRD (2022), 2112.05722

...many exciting topics I'd be happy to discuss later!
I won't discuss this area at all for the remainder of the talk

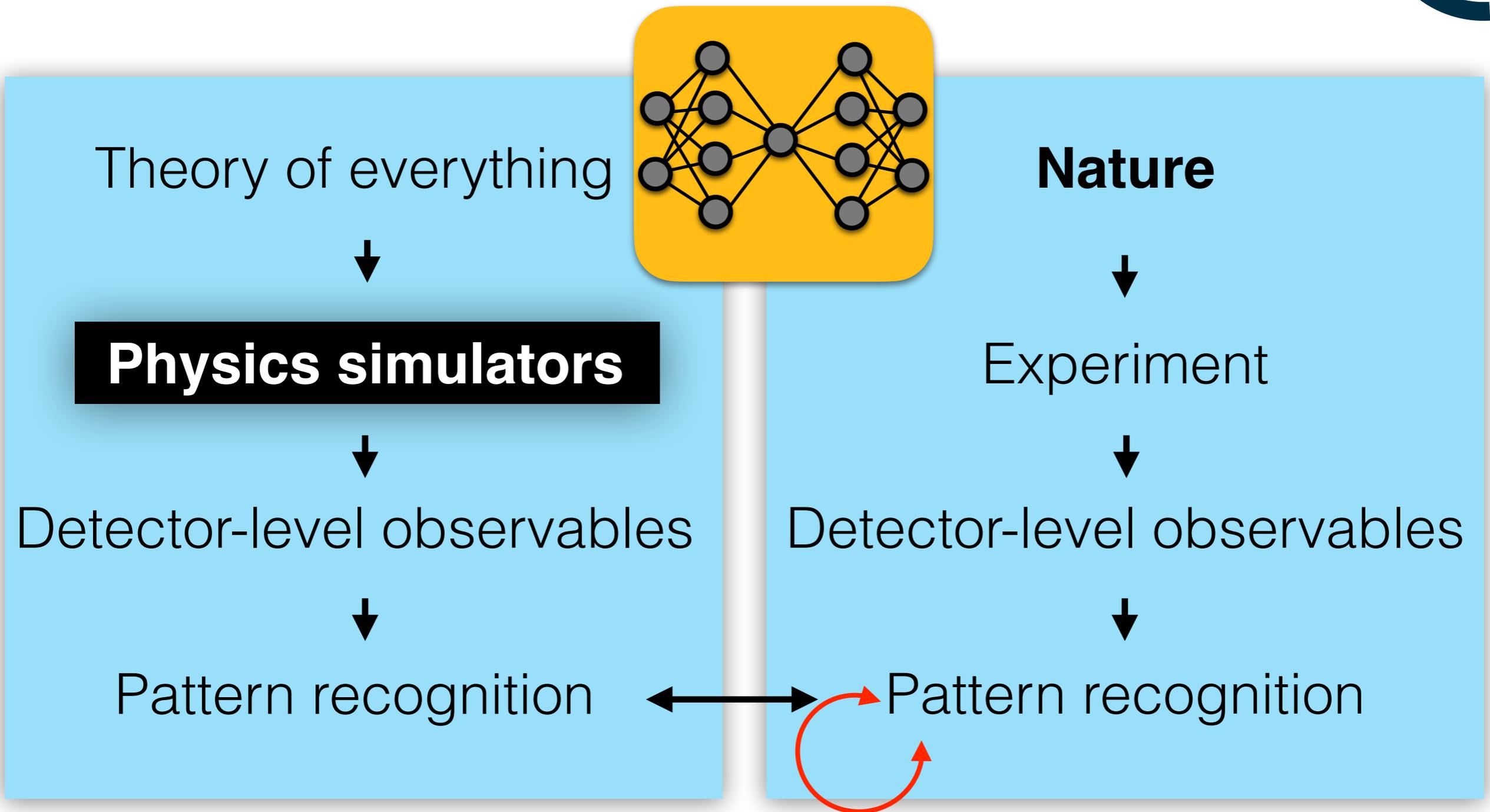




A growing toolkit called “generative models” are being developed to accelerate or augment simulations.



This is the “inverse” direction, where we use simulations to infer properties of the fundamental theory.

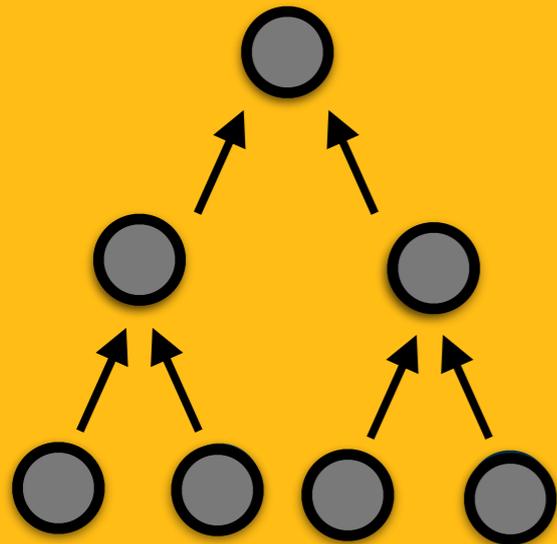


There is a growing need for simulation-independent methods that allow us to look for unanticipated scenarios.

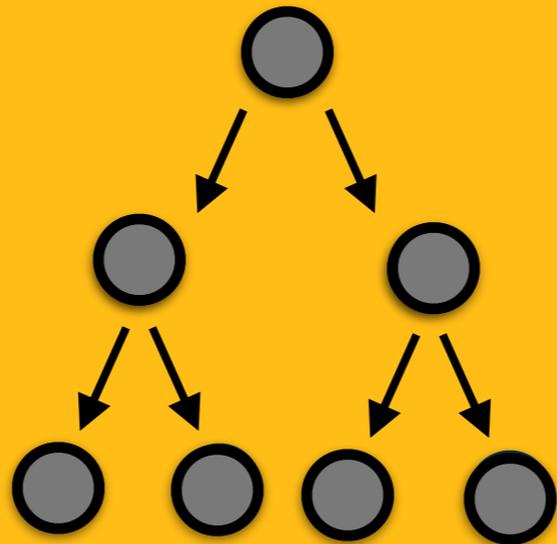
Outline for today

22

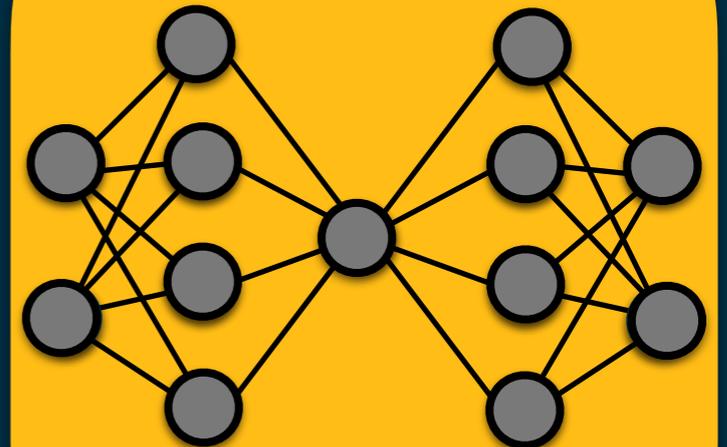
I'll focus on three core, cross-cutting areas of $ML \cap Physics$



Forward Models



Inverse Models

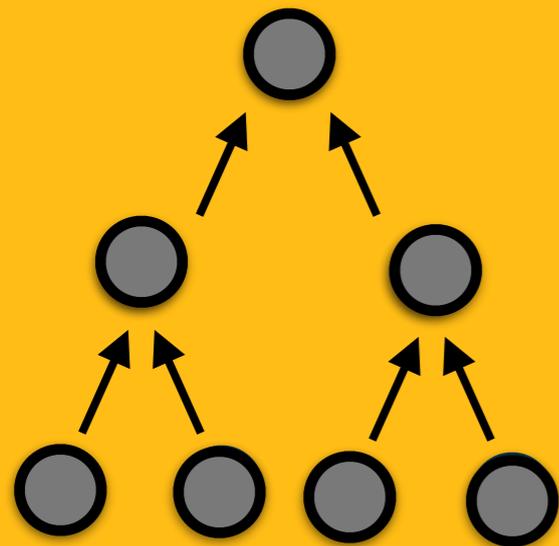


Simulation-free

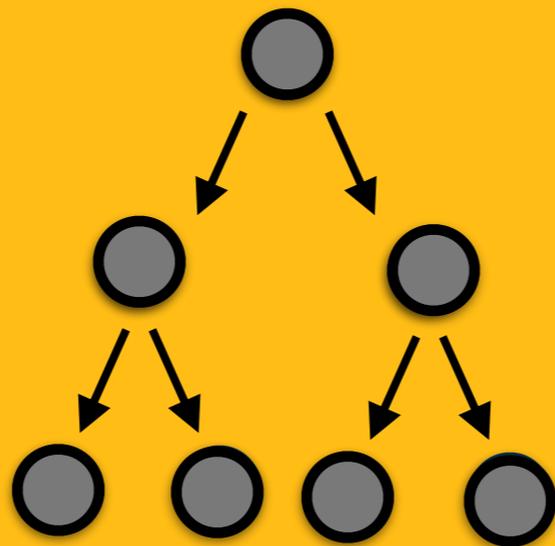
Outline for today

23

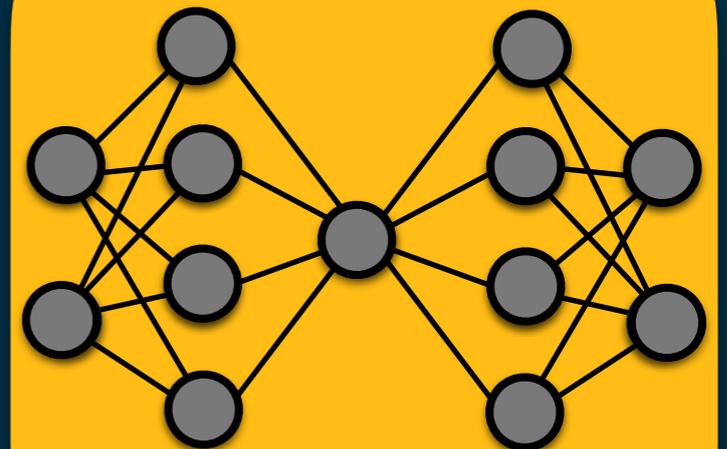
I'll focus on three core, cross-cutting areas of $ML \cap Physics$



Forward Models
(fast simulation)



Inverse Models
(unfolding)



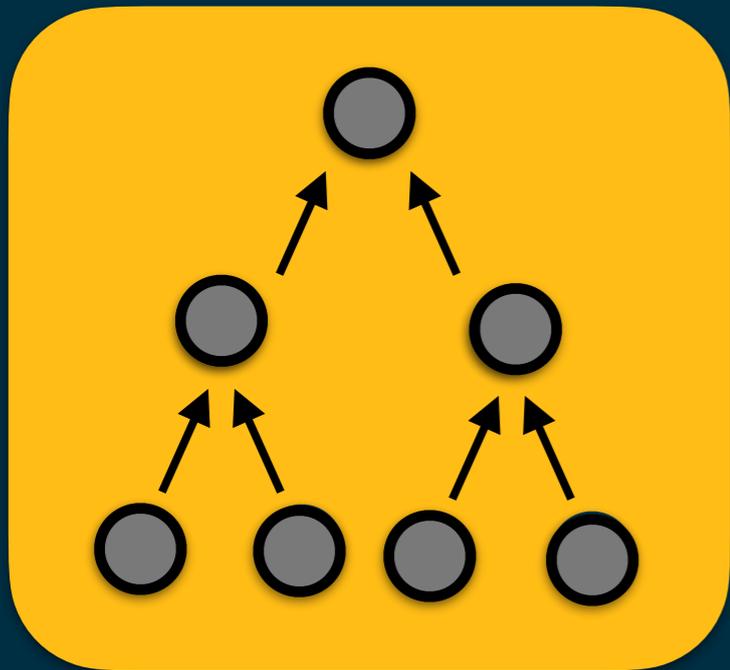
Simulation-free
(anomaly detection)

To illustrate these exciting topics, I'll give one vignette per area

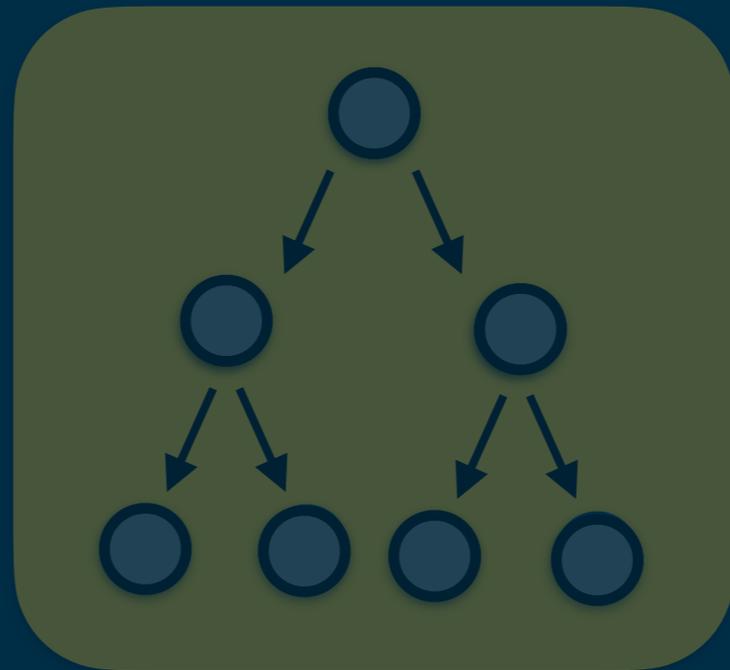
Outline for today

24

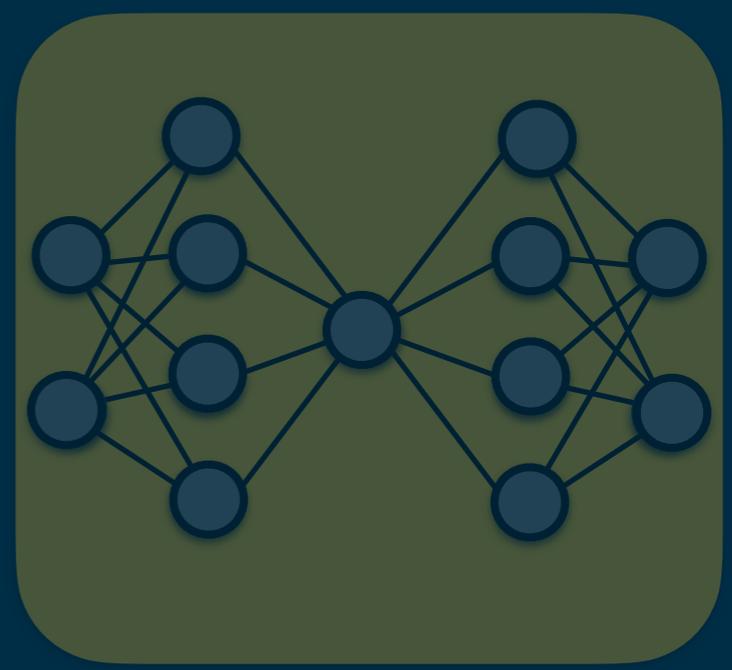
I'll focus on three core, cross-cutting areas of $ML \cap Physics$



Forward Models
(fast simulation)



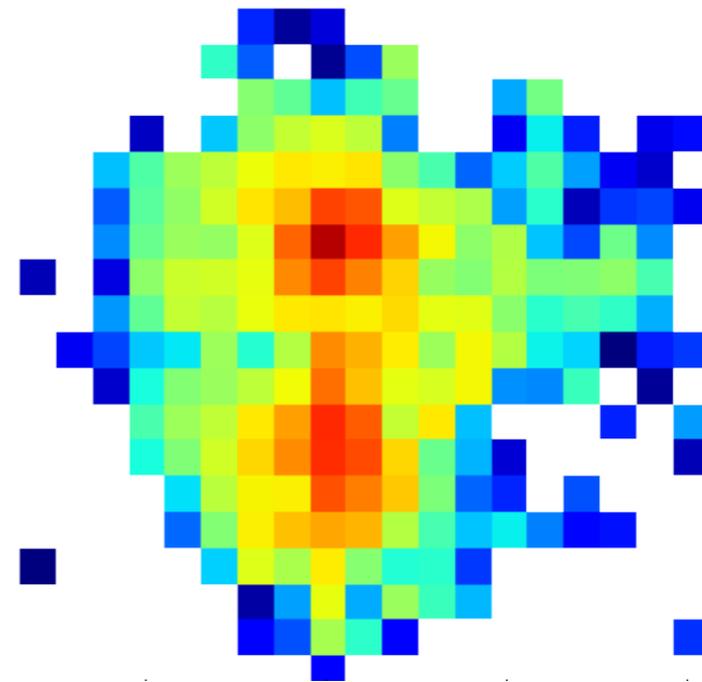
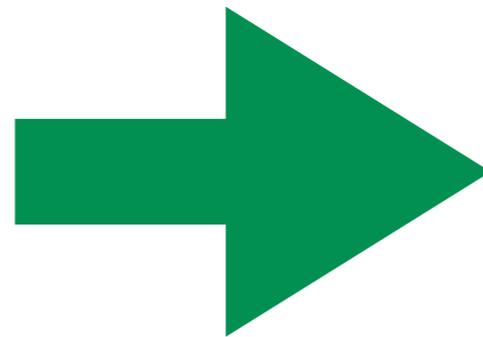
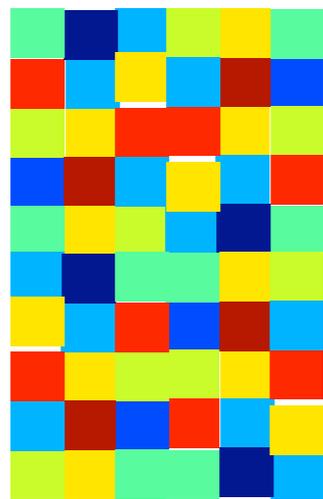
Inverse Models
(unfolding)



Simulation-free
(anomaly detection)

To illustrate these exciting topics, I'll give one vignette per area

A **generator** is nothing other than a function that maps random numbers to structure.



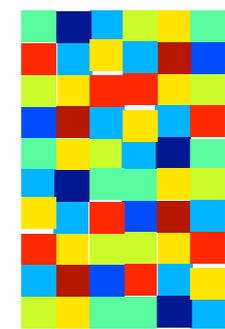
Deep generative models: the map is a deep neural network.

Introduction: GANs

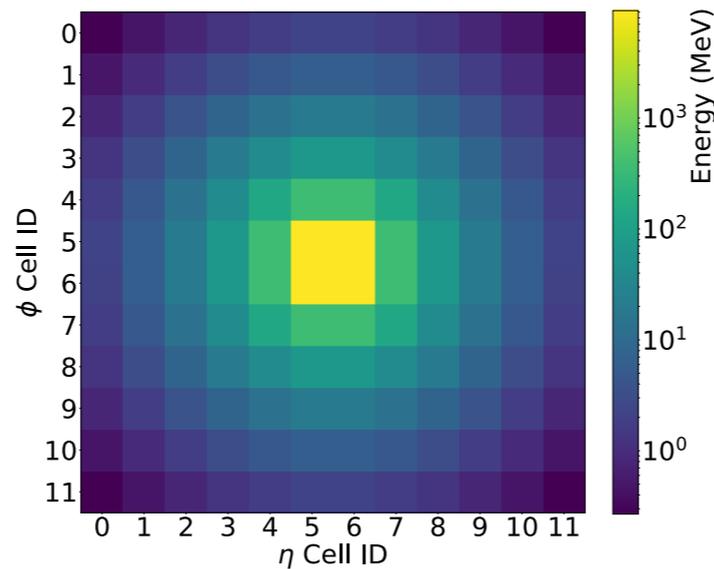
26

Generative Adversarial Networks (GANs):

*A two-network game where one **maps noise to structure** and one **classifies images as fake or real**.*

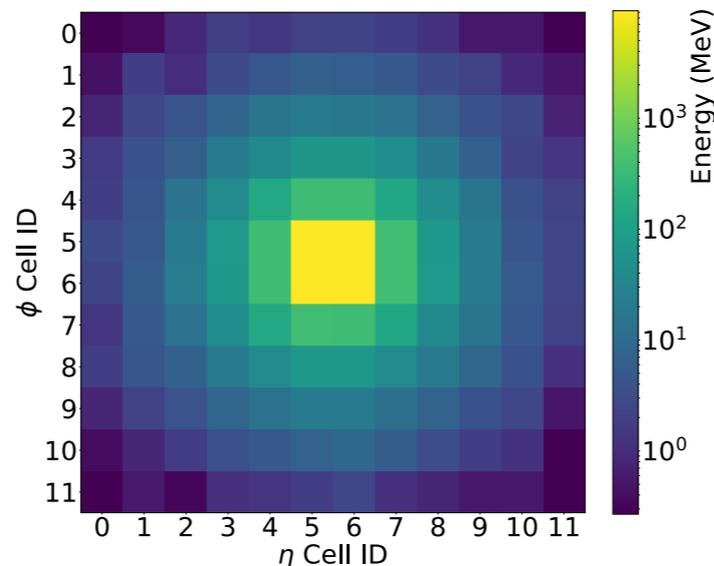


noise

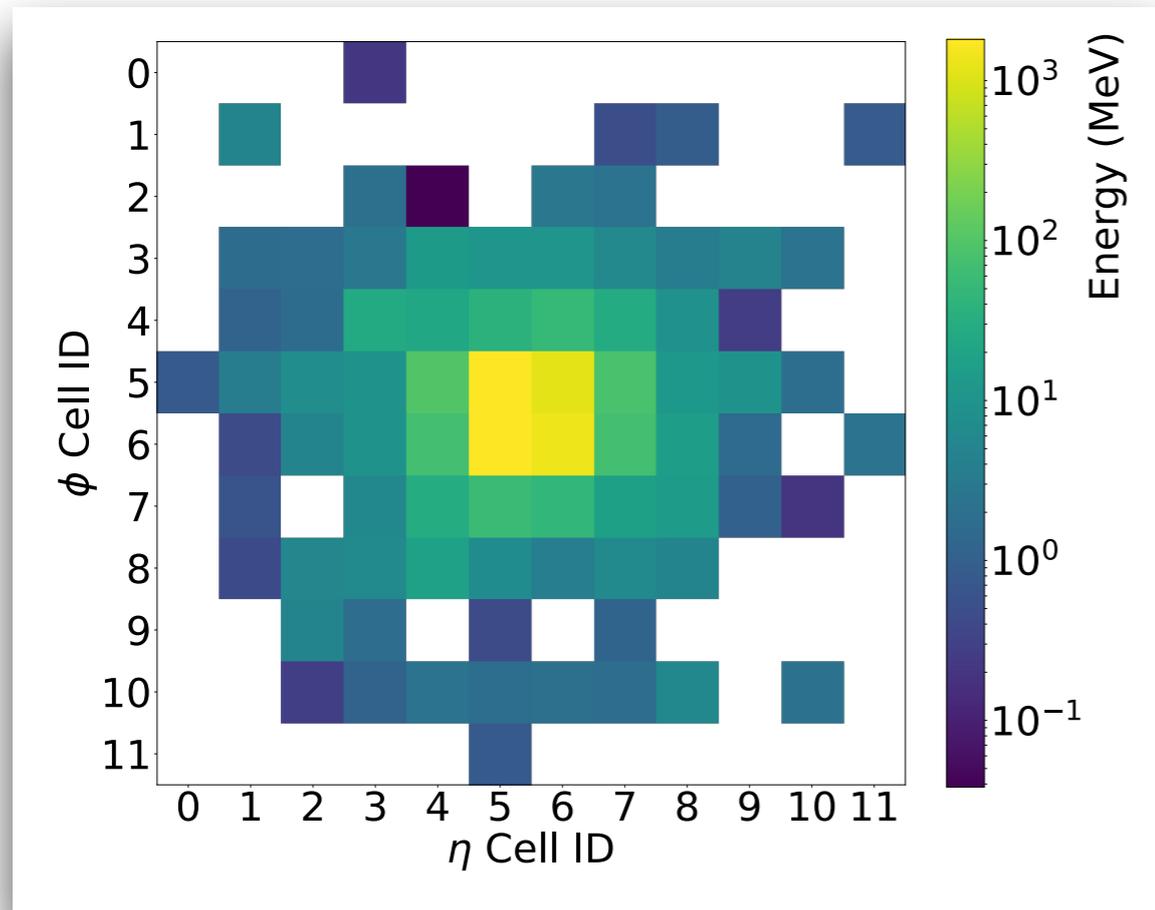


{real, fake}

When **D** is maximally confused, **G** will be a good generator

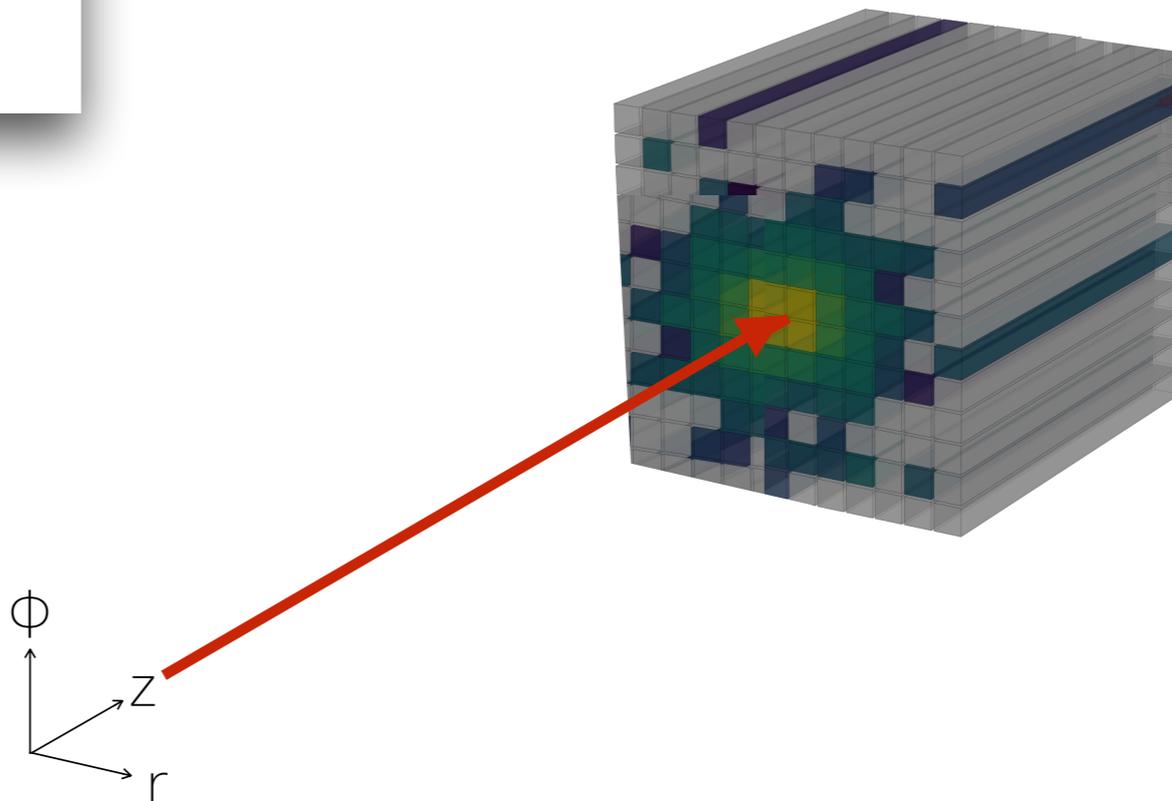


physics-based simulator or data



Calorimeters are often the slowest to simulate
stopping particles requires simulating interactions of all energies

Grayscale images:
pixel intensity
= energy deposited



Solution: CaloGAN

28

GANs and related deep generative models are promising tools for fast approximate simulations

Solution: CaloGAN

29

GANs and related deep generative models are promising tools for fast approximate simulations

These tools are automated, which enables portability

*They are fast, can be readily retrained,
and don't take much disk space*

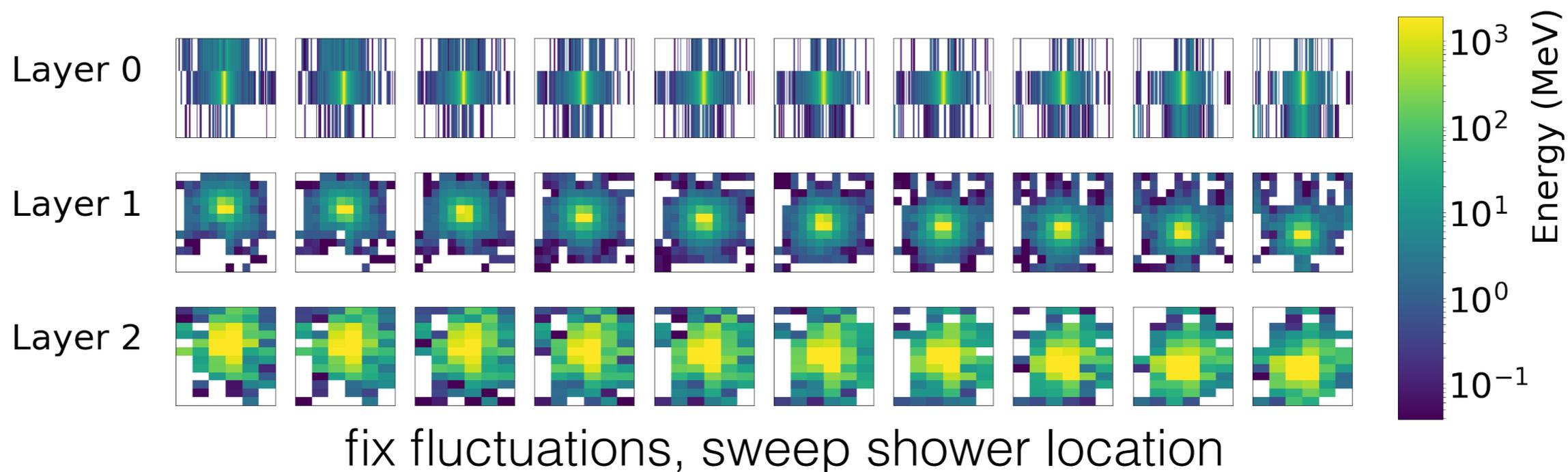
Solution: CaloGAN



GANs and related deep generative models are promising tools for fast approximate simulations

These tools are automated, which enables portability

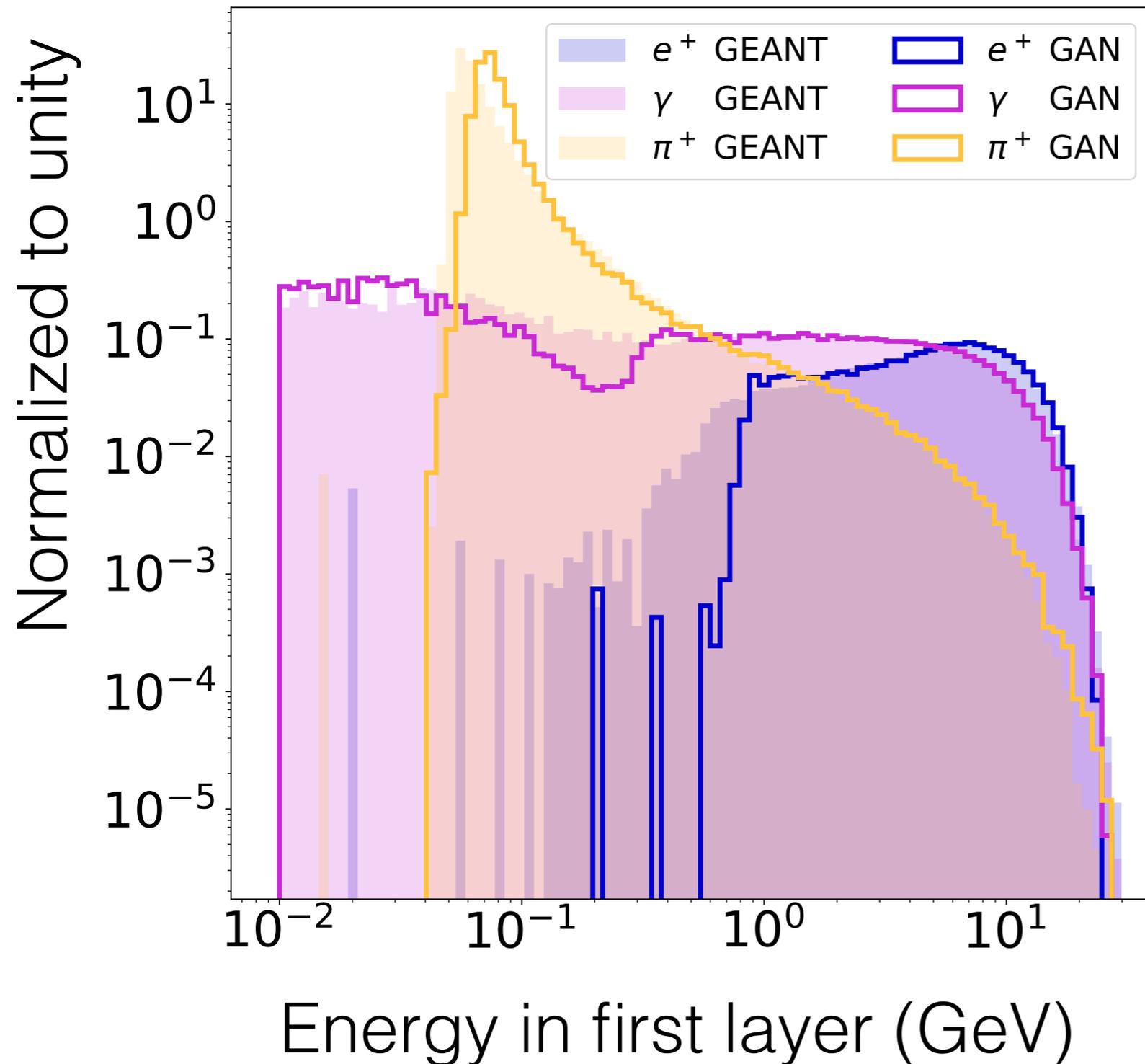
We also have full control over the physics:



Solution: CaloGAN

31

M. Paganini, L. De Oliveira, **BN**, PRL 120 (2018) 042003

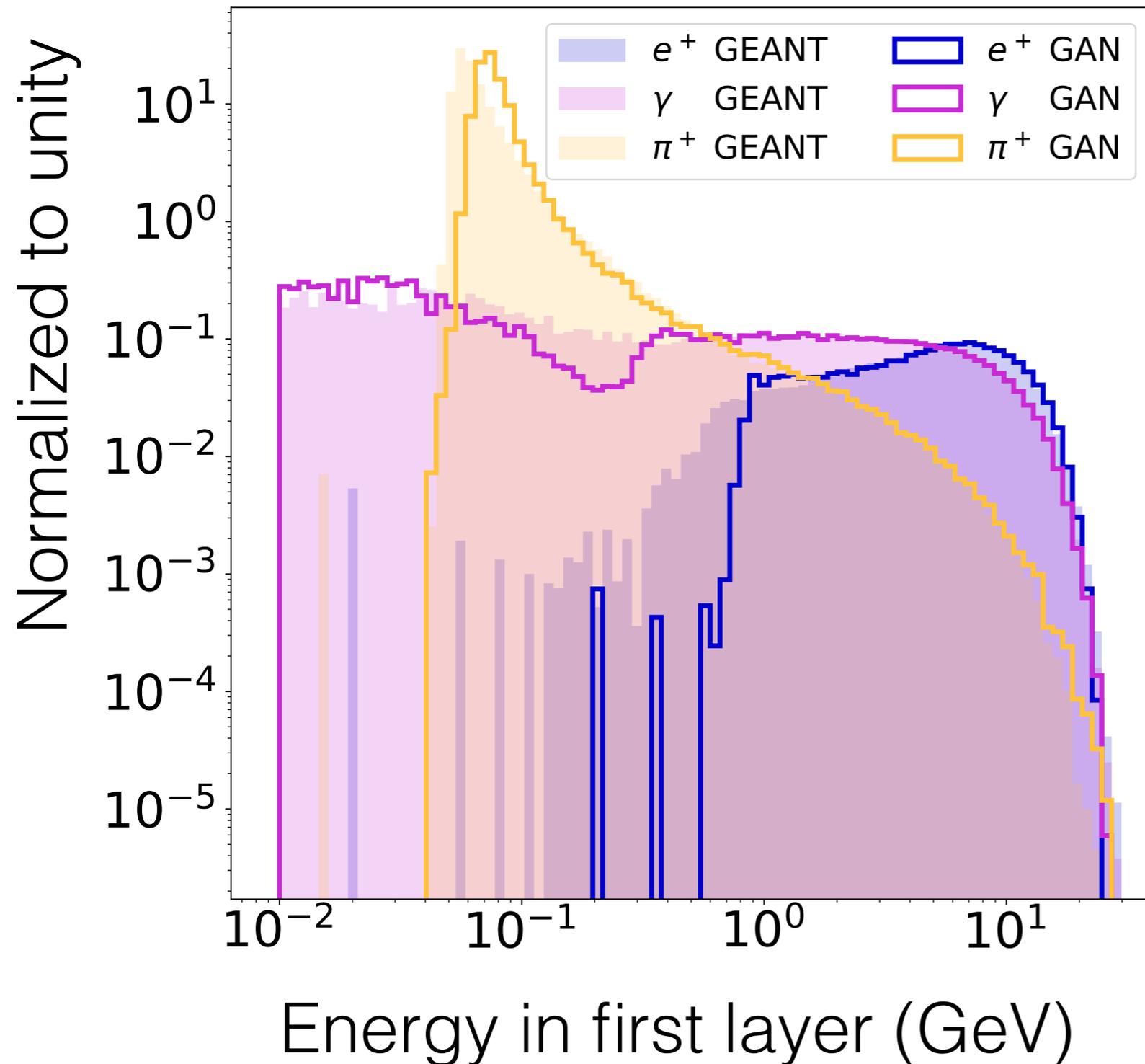


Pions deposit much less energy in the first layers; leave the calorimeter with significant energy

Solution: CaloGAN

32

M. Paganini, L. De Oliveira, **BN**, PRL 120 (2018) 042003



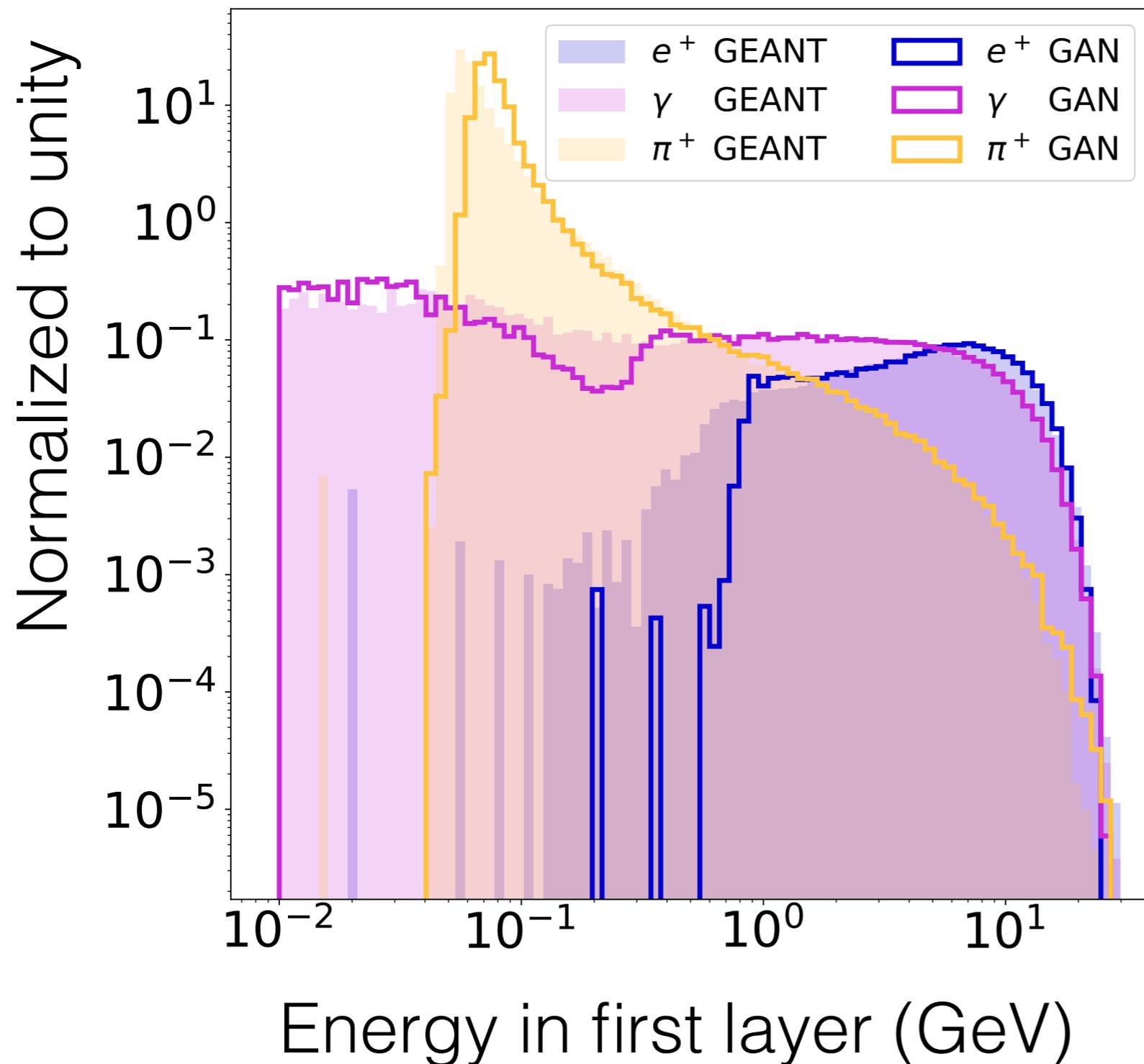
Pions deposit much less energy in the first layers; leave the calorimeter with significant energy

Time to generate an event is orders of magnitude faster than Geant4 and independent of energy

Solution: CaloGAN

33

M. Paganini, L. De Oliveira, **BN**, PRL 120 (2018) 042003



Pions deposit much less energy in the first layers; leave the calorimeter with significant energy

Time to generate an event is orders of magnitude faster than Geant4 and independent of energy

ATLAS now uses a CaloGAN-like approach and will use it to generate **billions of showers!**

**Goal: maintain speed,
improve precision**

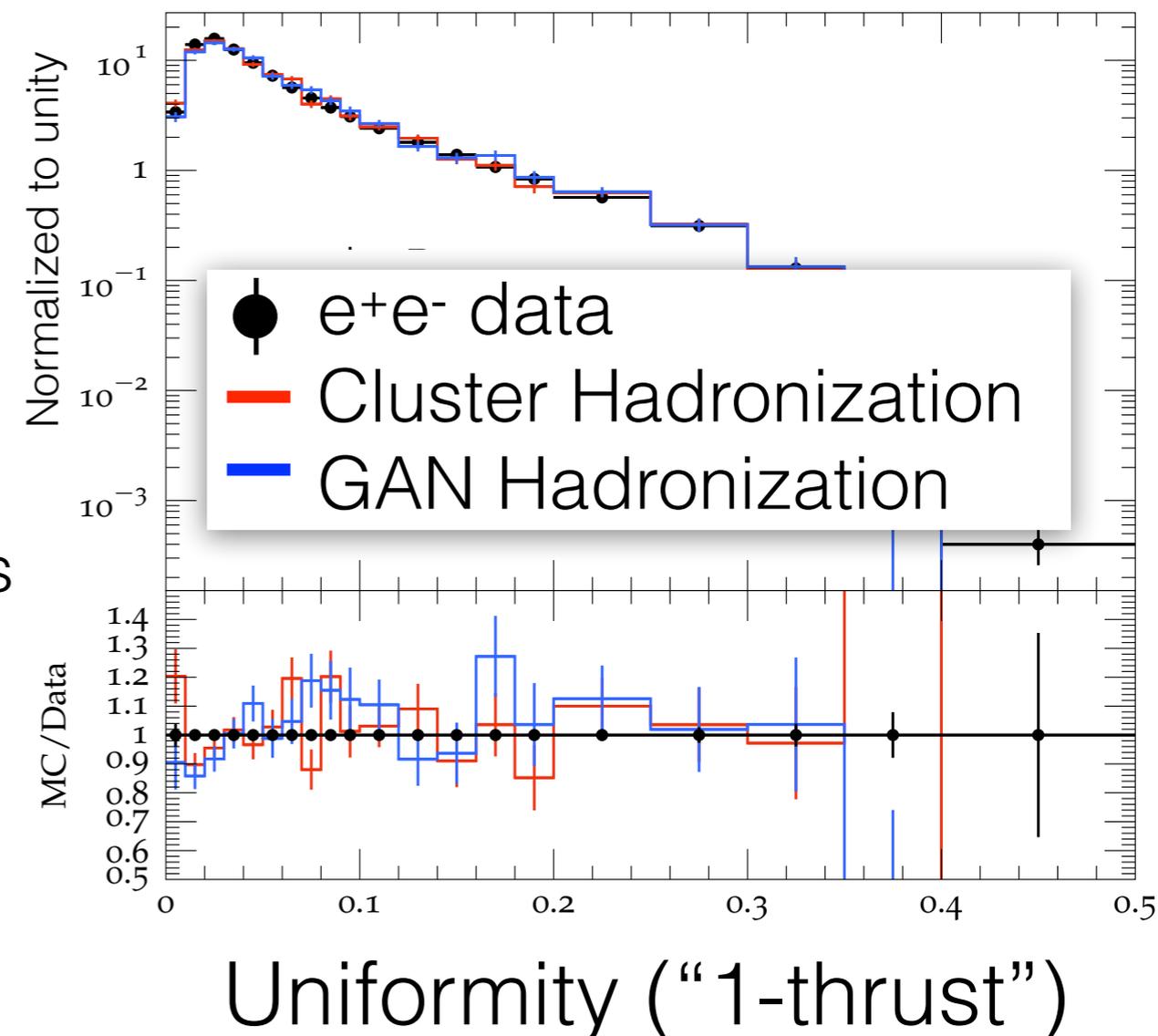
Methods

Next frontier: physics-informed generative models

Science

- Fast simulation for next-gen experiments
- Flexible, “non-parametric” functions for phenomenological models
 - Hadronization (quarks/gluons \rightarrow hadrons)
 - Dark matter N-body \rightarrow baryons

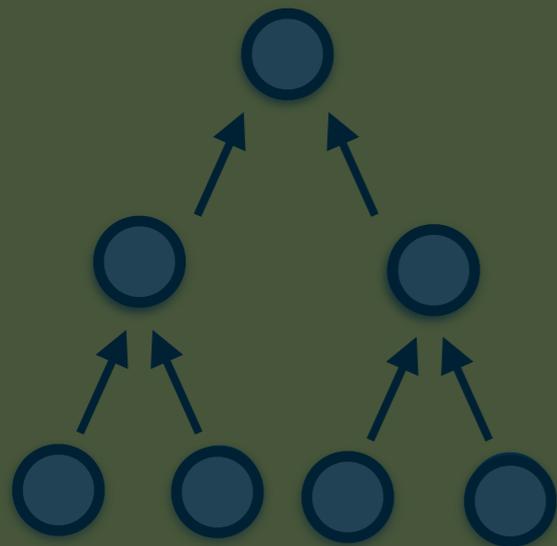
A. Ghosh, X. Ju, **BN**, A. Siodmok, 2203.12660



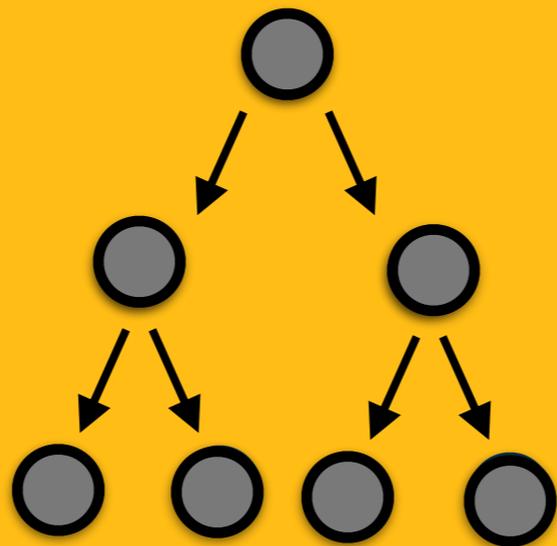
Outline for today

35

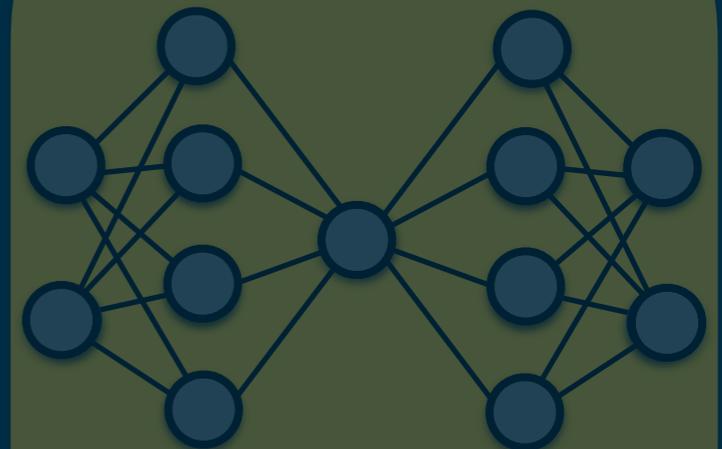
I'll focus on three core, cross-cutting areas of $ML \cap Physics$



Forward Models
(fast simulation)



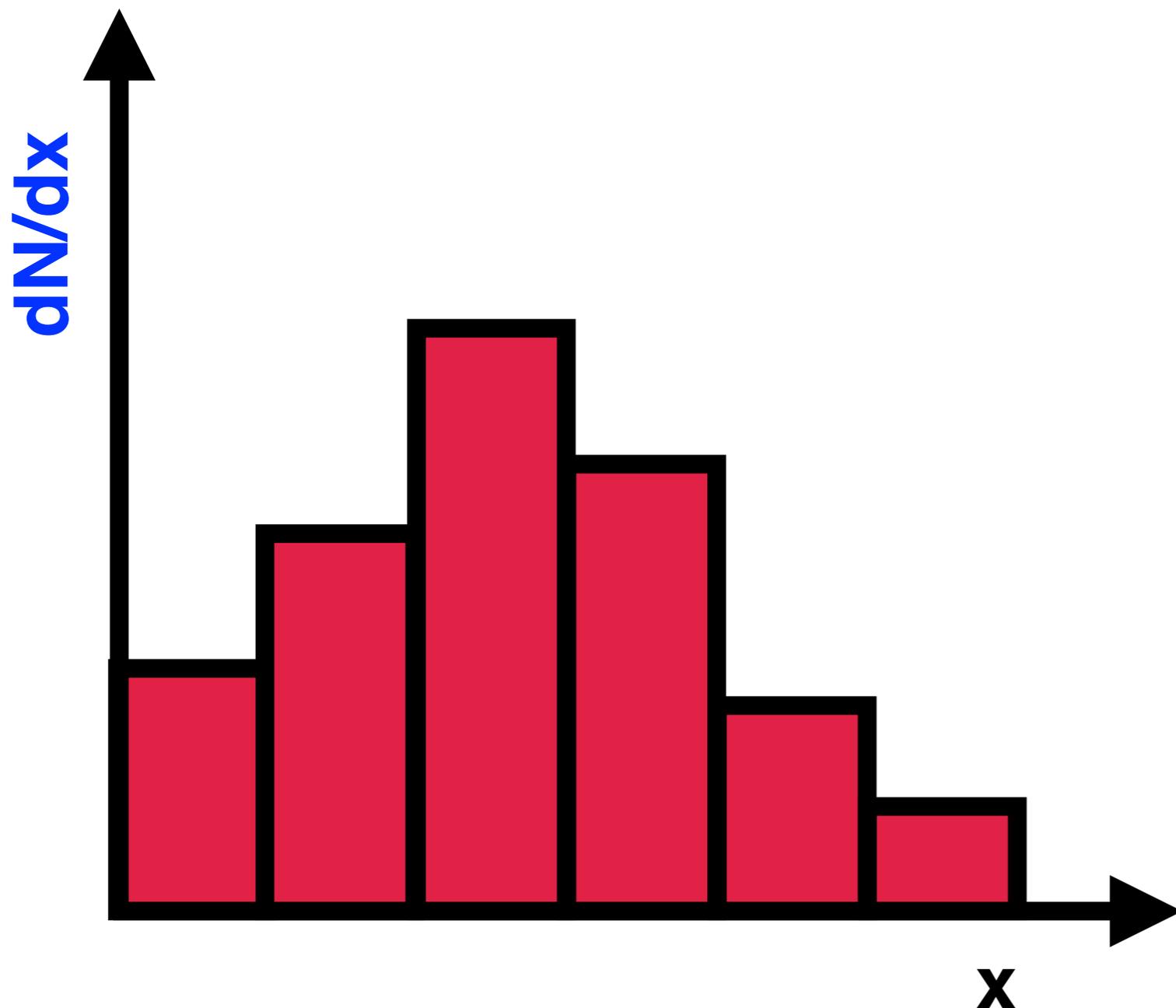
Inverse Models
(unfolding)



Simulation-free
(anomaly detection)

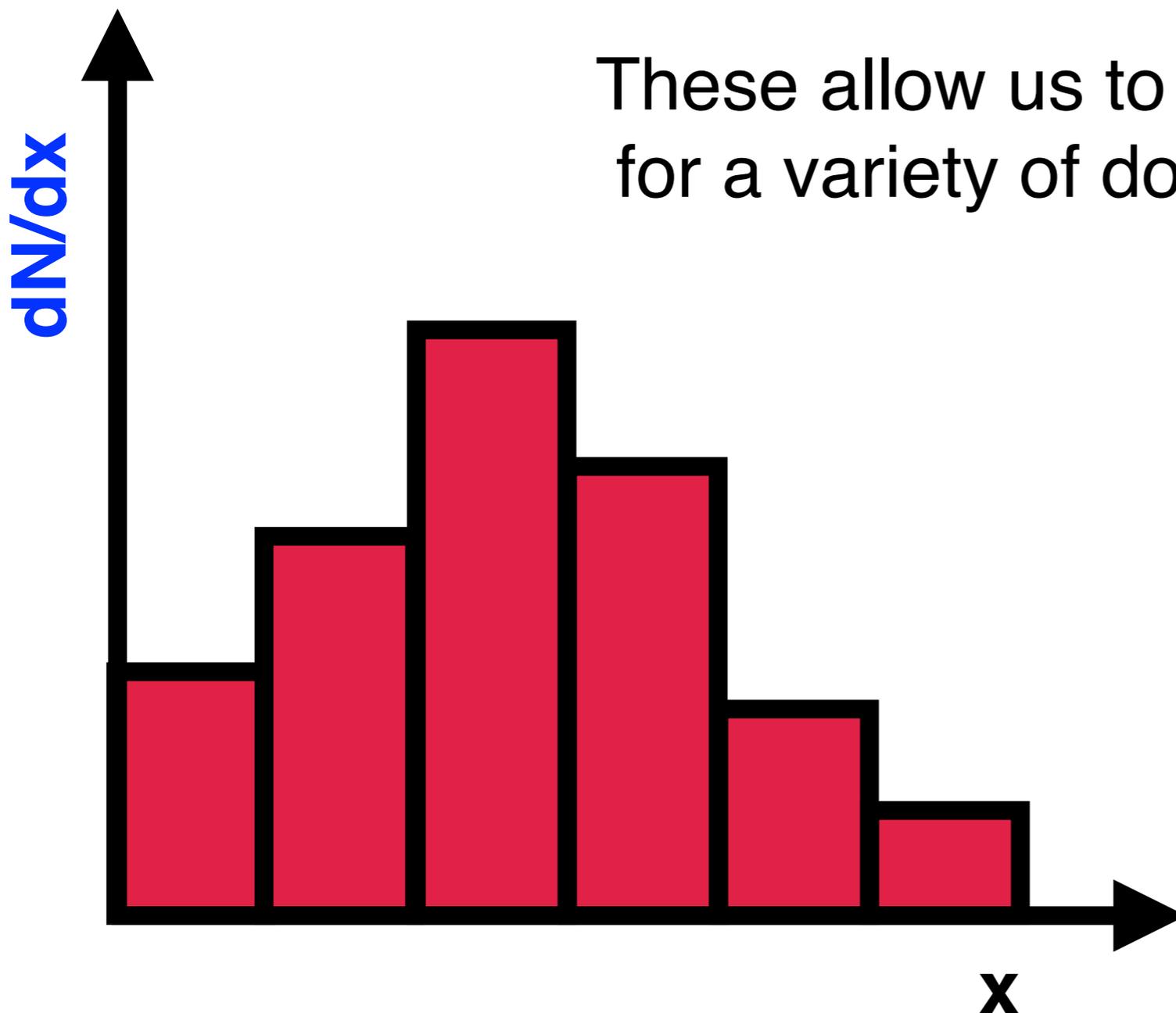
To illustrate these exciting topics, I'll give one vignette per area

Differential cross section measurements are central to collider physics & are increasingly important in neutrino physics

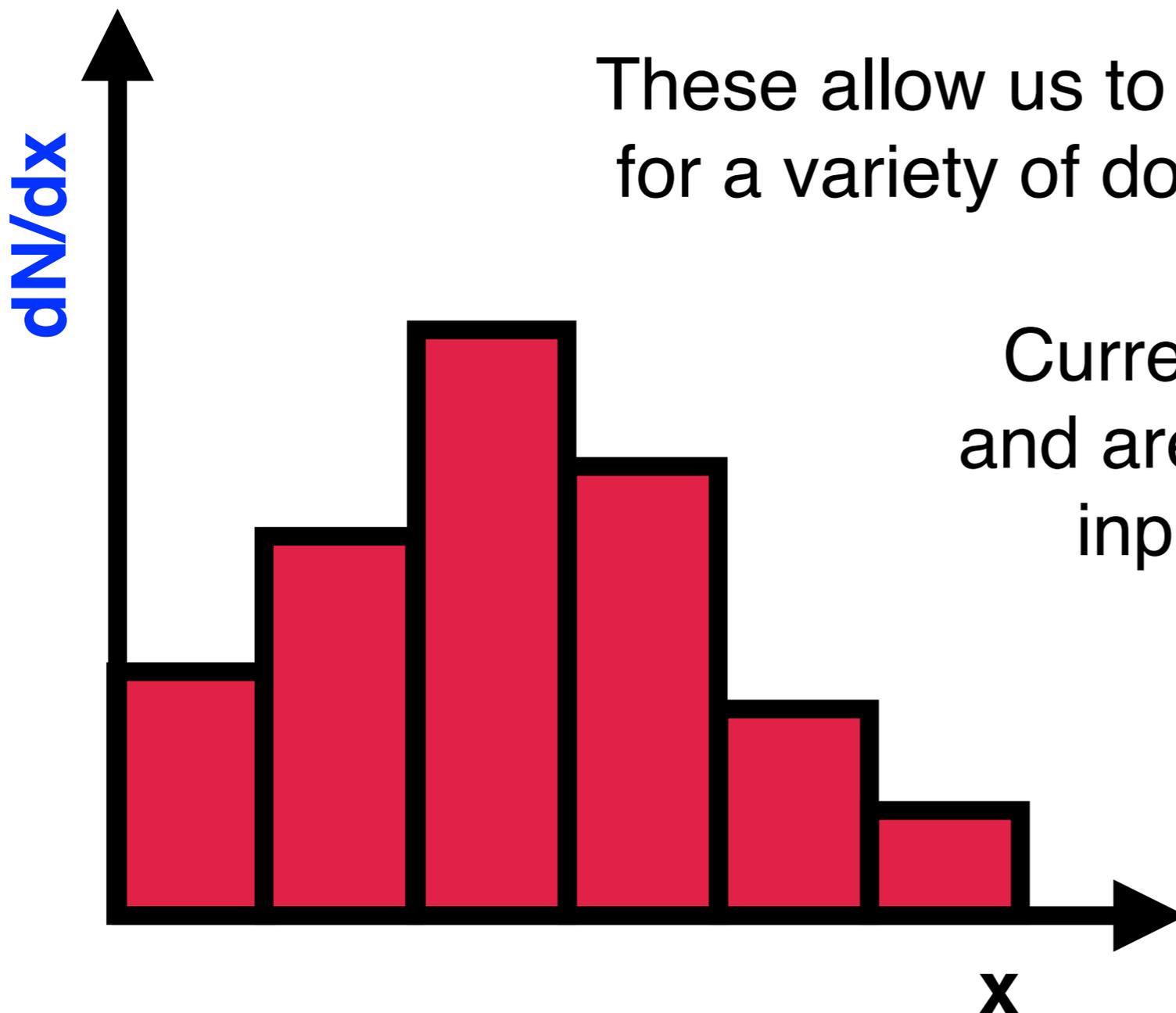


Differential cross section measurements are central to collider physics & are increasingly important in neutrino physics

These allow us to compare data with theory for a variety of down-stream science goals



Differential cross section measurements are central to collider physics & are increasingly important in neutrino physics

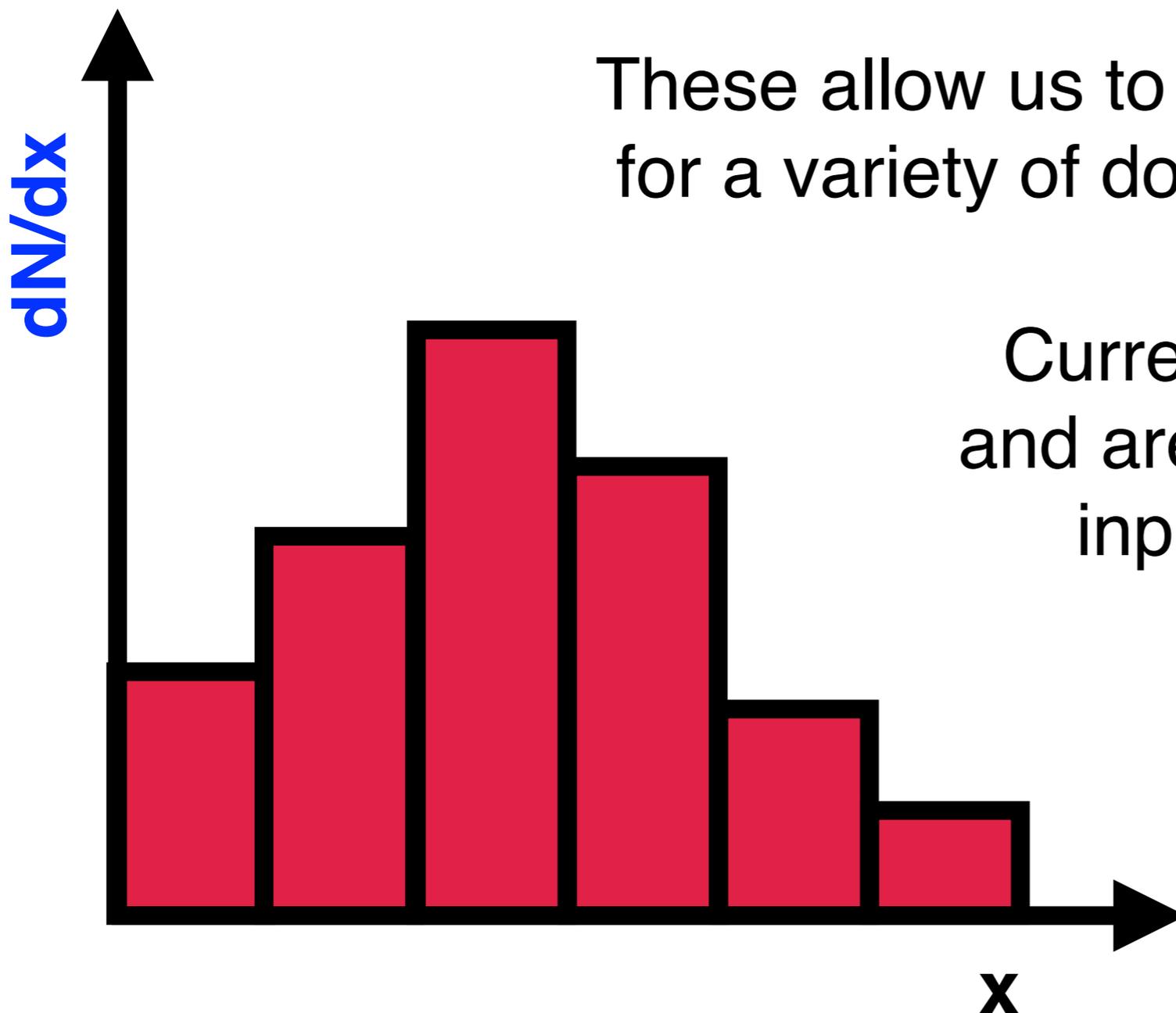


These allow us to compare data with theory for a variety of down-stream science goals

Current approaches use bins and are limited in the number of input/output dimensions.

Differential cross section measurements are central to collider physics & are increasingly important in neutrino physics

These allow us to compare data with theory for a variety of down-stream science goals



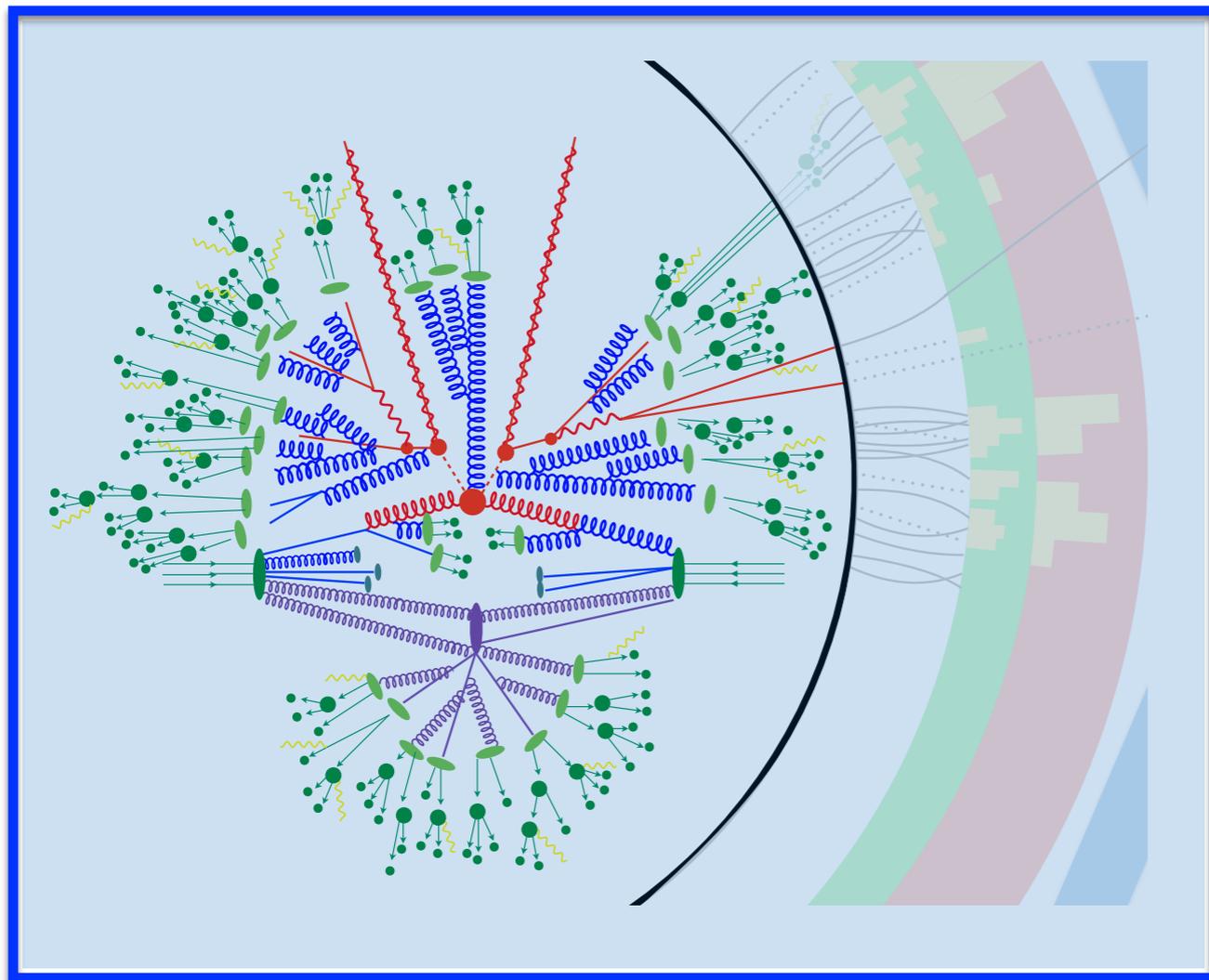
Current approaches use bins and are limited in the number of input/output dimensions.

Can we go unbinned and high-dimensional?

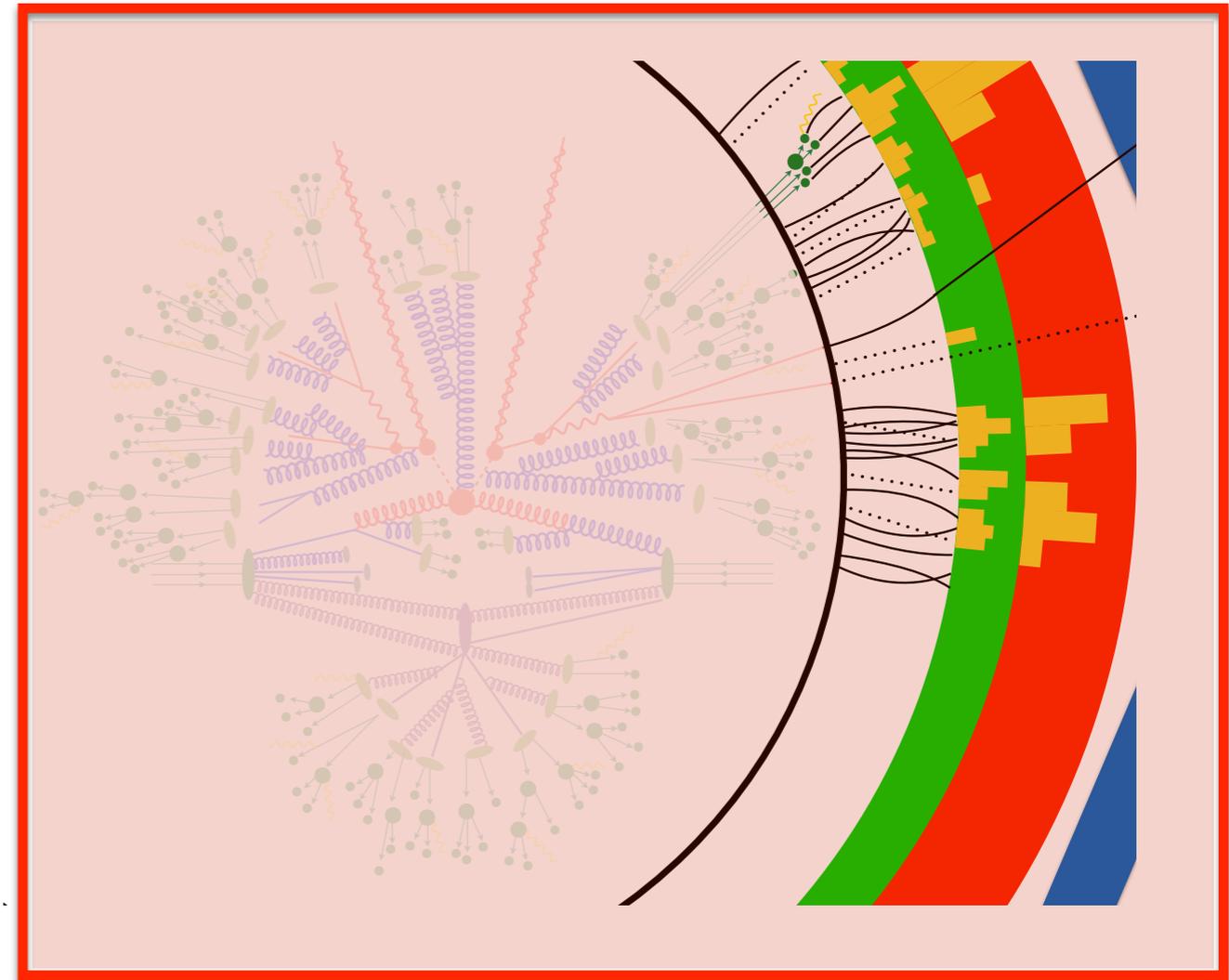
Deconvolution/Unfolding

40

Want this



Measure this



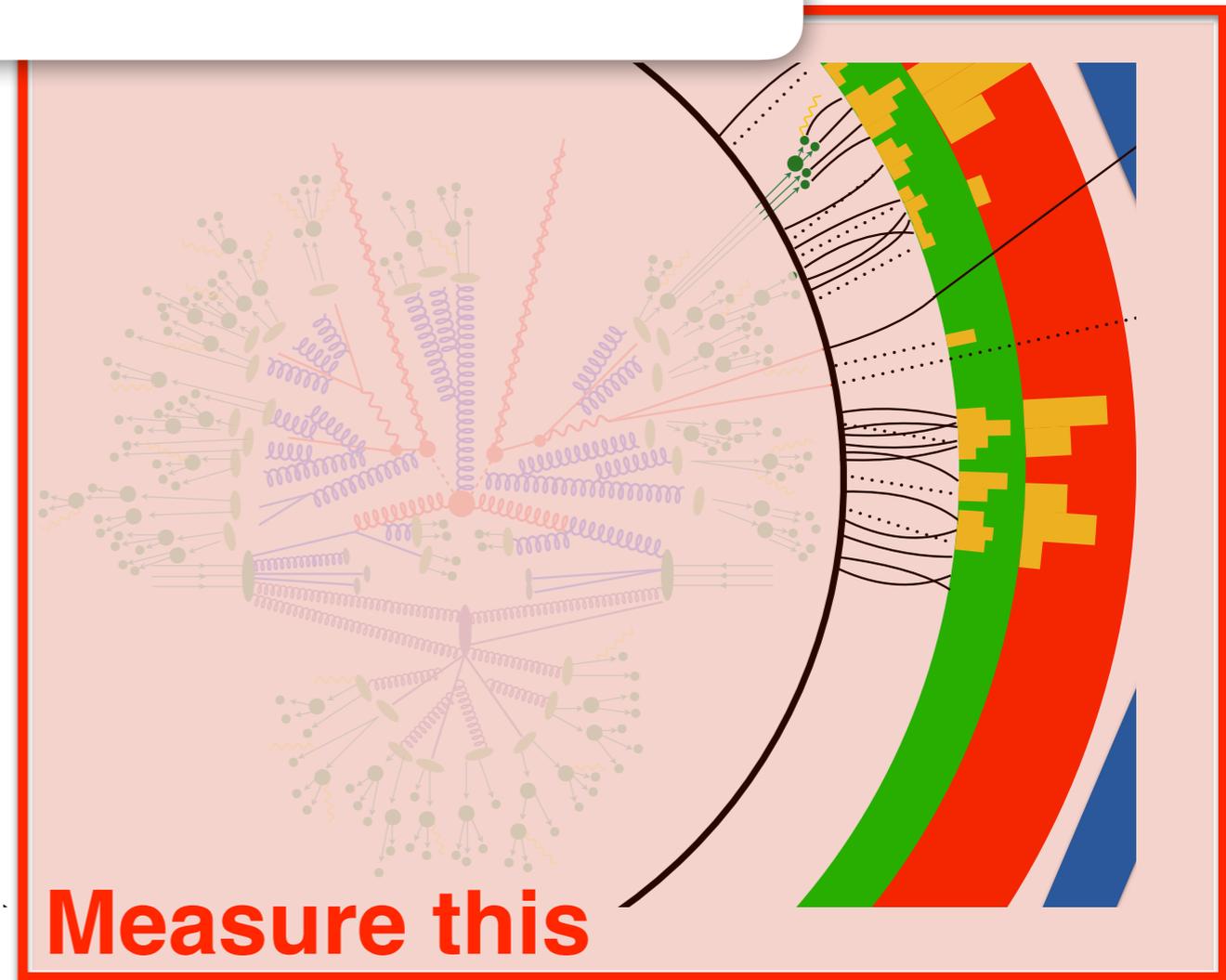
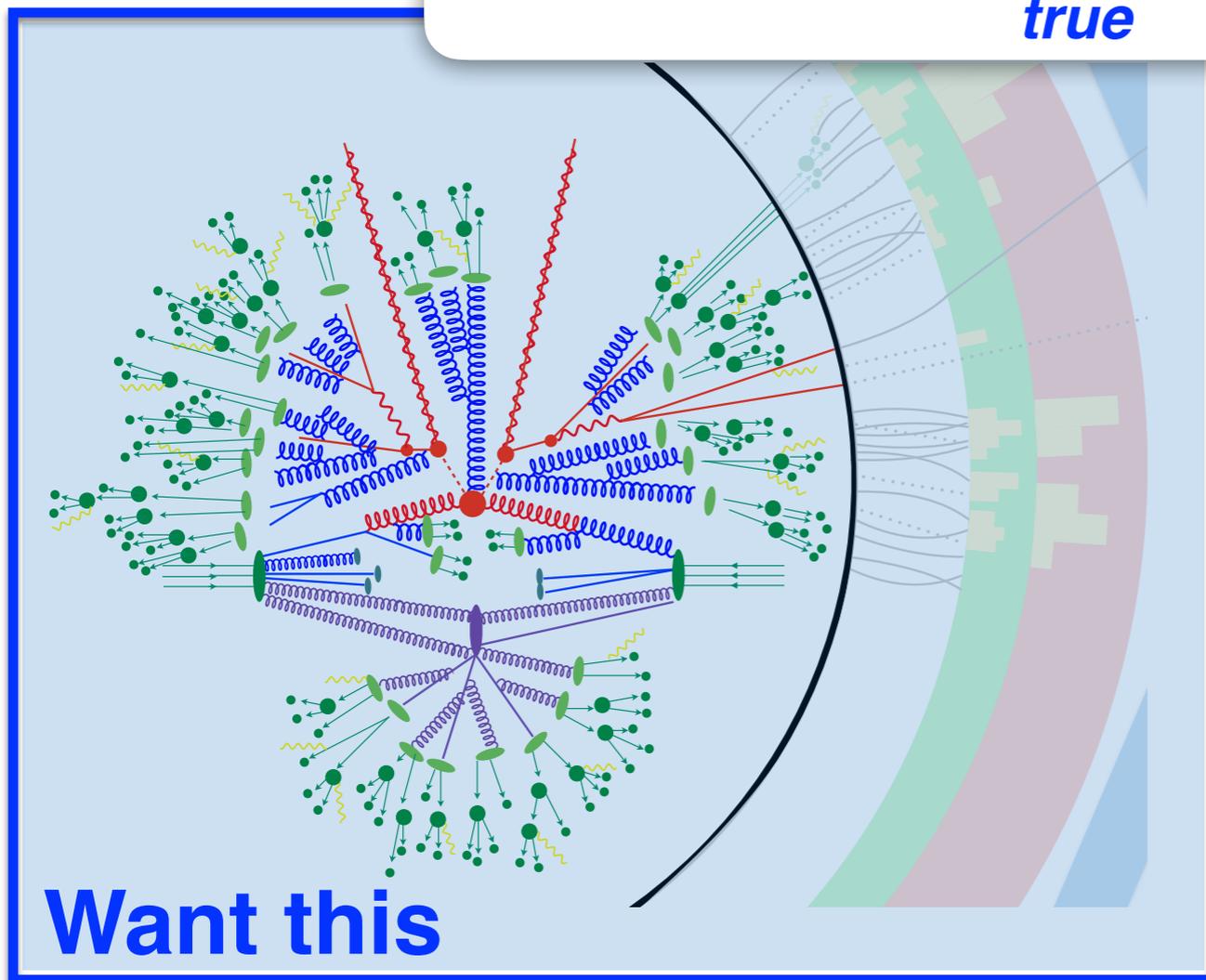
i.e. remove detector distortions

Deconvolution/Unfolding

41

If you know $p(\textit{meas.} / \textit{true})$, could do maximum likelihood, i.e.

$$\textit{unfolded} = \underset{\textit{true}}{\operatorname{argmax}} p(\textit{measured} / \textit{true})$$



$p(\textit{meas.} / \textit{true})$ = “response matrix” or “point spread function”

Deconvolution/Unfolding

42

If you know $p(\textit{meas.} \mid \textit{true})$, could do maximum likelihood, i.e.

$$\textit{unfolded} = \underset{\textit{true}}{\operatorname{argmax}} p(\textit{measured} \mid \textit{true})$$



Challenge: **measured** is hyperspectral and **true** is hypervariate ... $p(\textit{meas.} \mid \textit{true})$ is **intractable** !

$p(\textit{meas.} \mid \textit{true})$ = “response matrix” or “point spread function”

If you know $p(\textit{meas.} \mid \textit{true})$, could do maximum likelihood, i.e.

$$\textit{unfolded} = \underset{\textit{true}}{\operatorname{argmax}} p(\textit{measured} \mid \textit{true})$$



Challenge: **measured** is hyperspectral and **true** is hypervariate ... $p(\textit{meas.} \mid \textit{true})$ is **intractable** !

However: we have **simulators** that we can use to sample from $p(\textit{meas.} \mid \textit{true})$

→ **Likelihood-free inference**

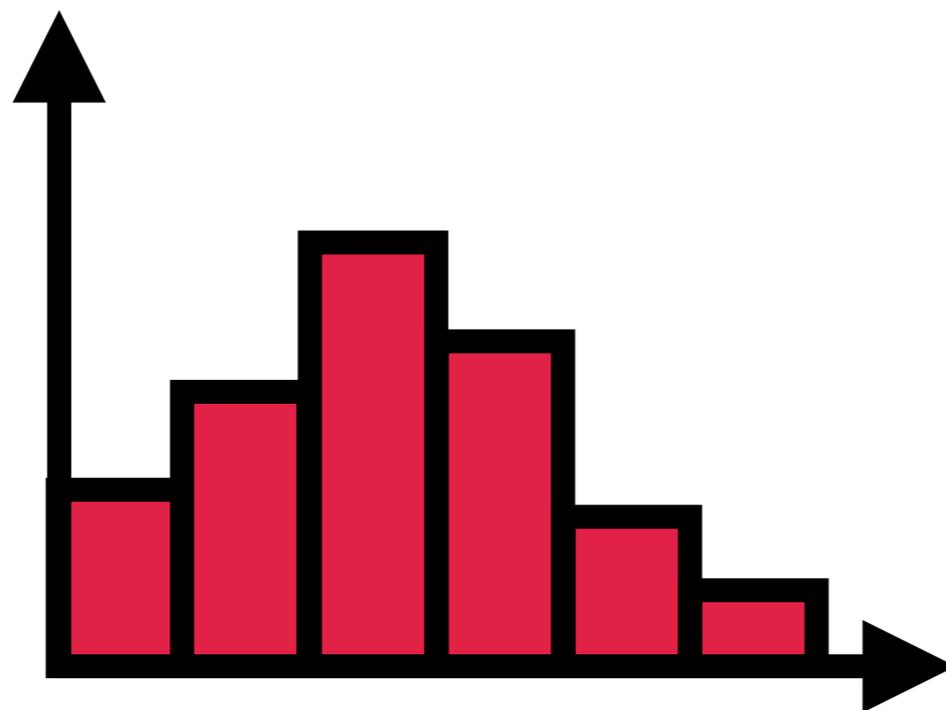
$p(\textit{meas.} \mid \textit{true})$ = “response matrix” or “point spread function”

Solution: ML-based Unfolding

44

We have introduced new machine learning methods capable of **unbinned, high-dimensional** unfolding.

This will radically change the cross section measurement programs of collider and neutrino physics.

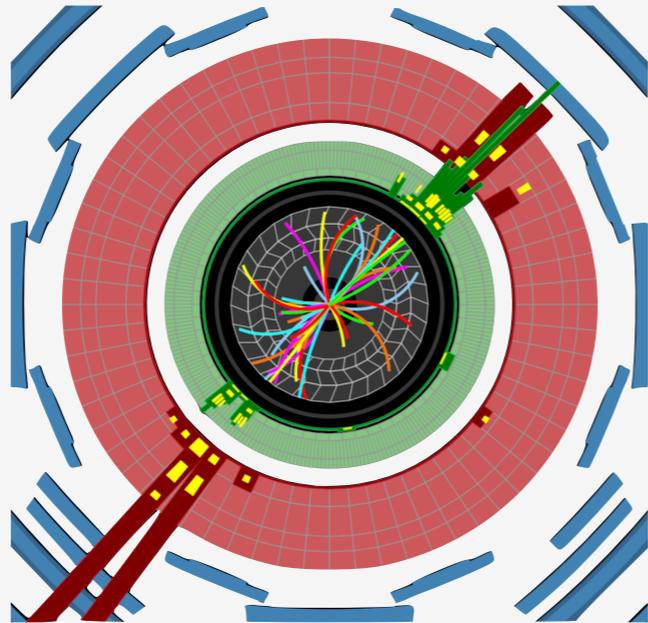


A brief introduction to OmniFold

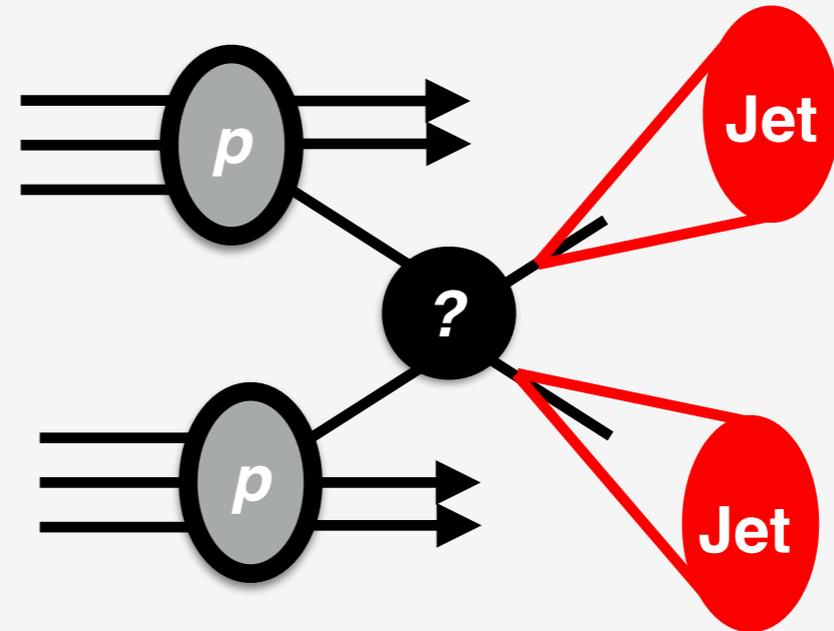
45

Nature

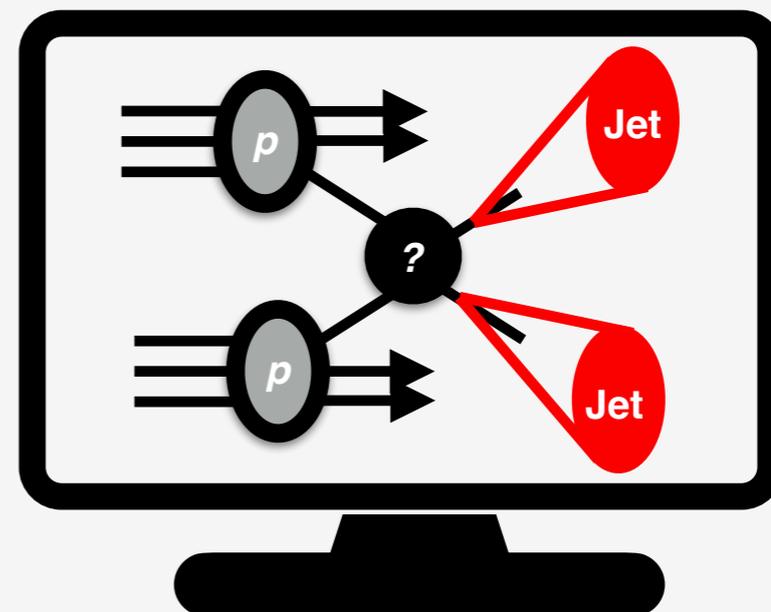
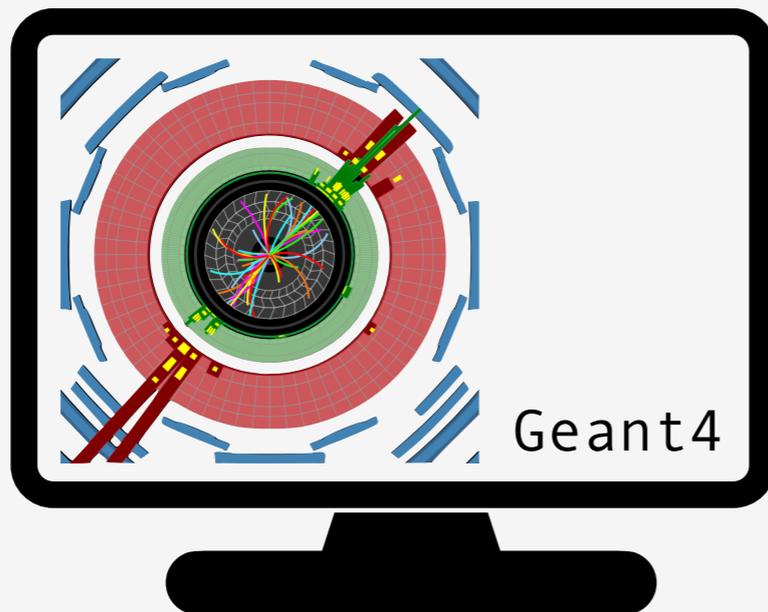
Detector-level



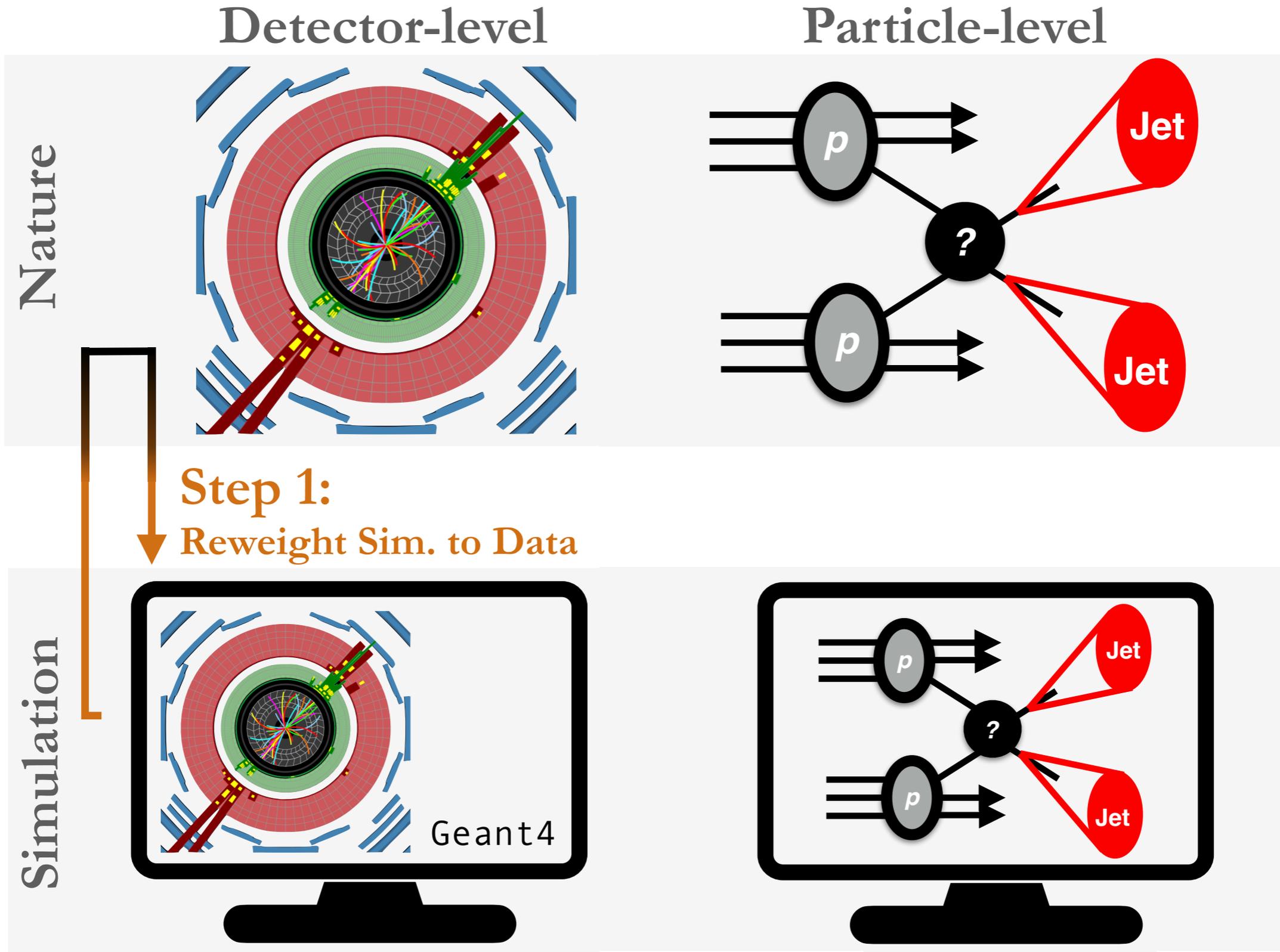
Particle-level



Simulation

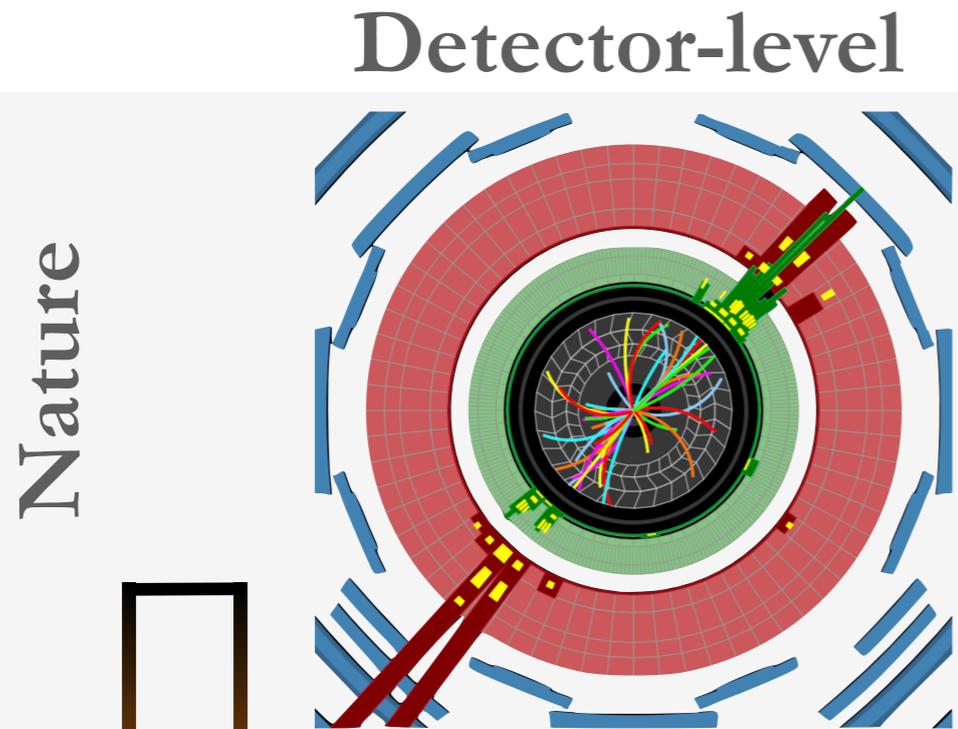


A brief introduction to OmniFold



A brief introduction to OmniFold

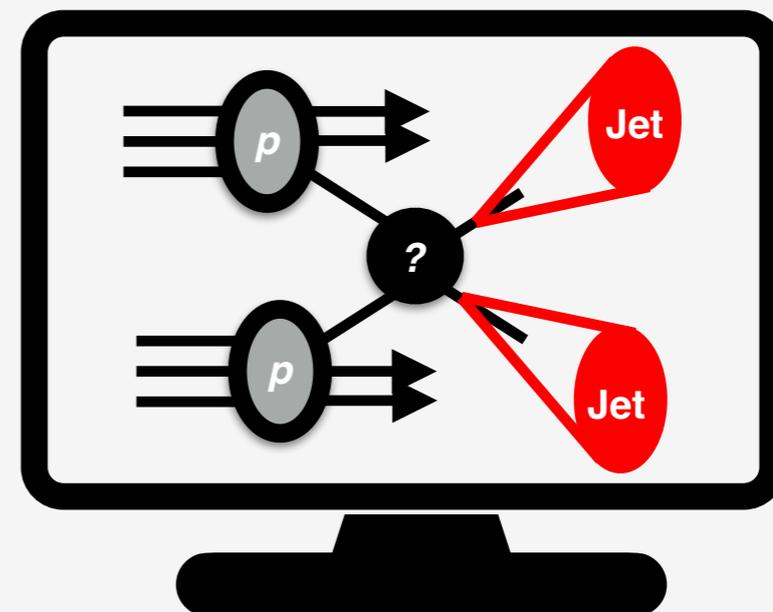
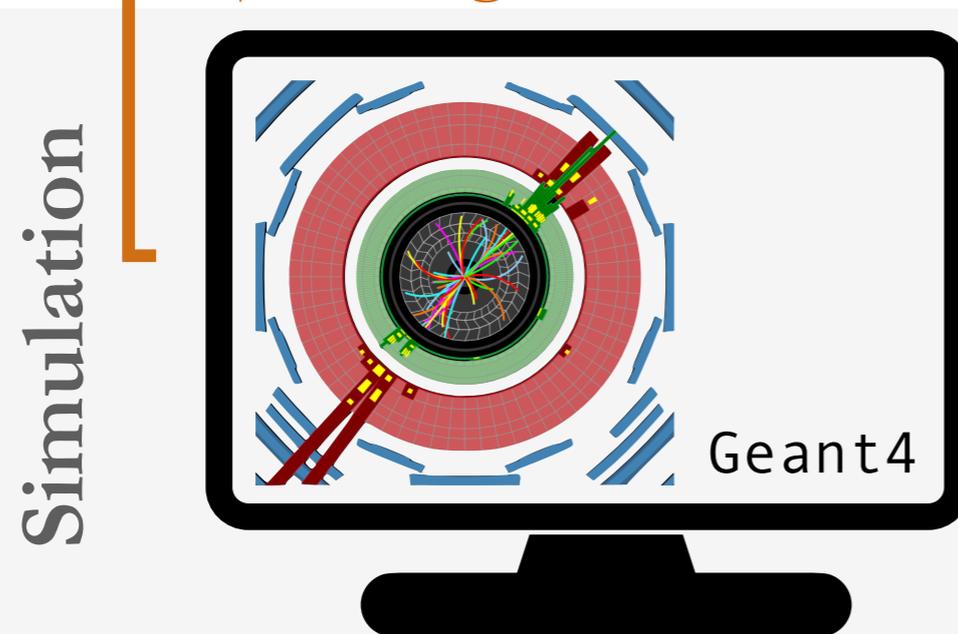
47



Particle-level

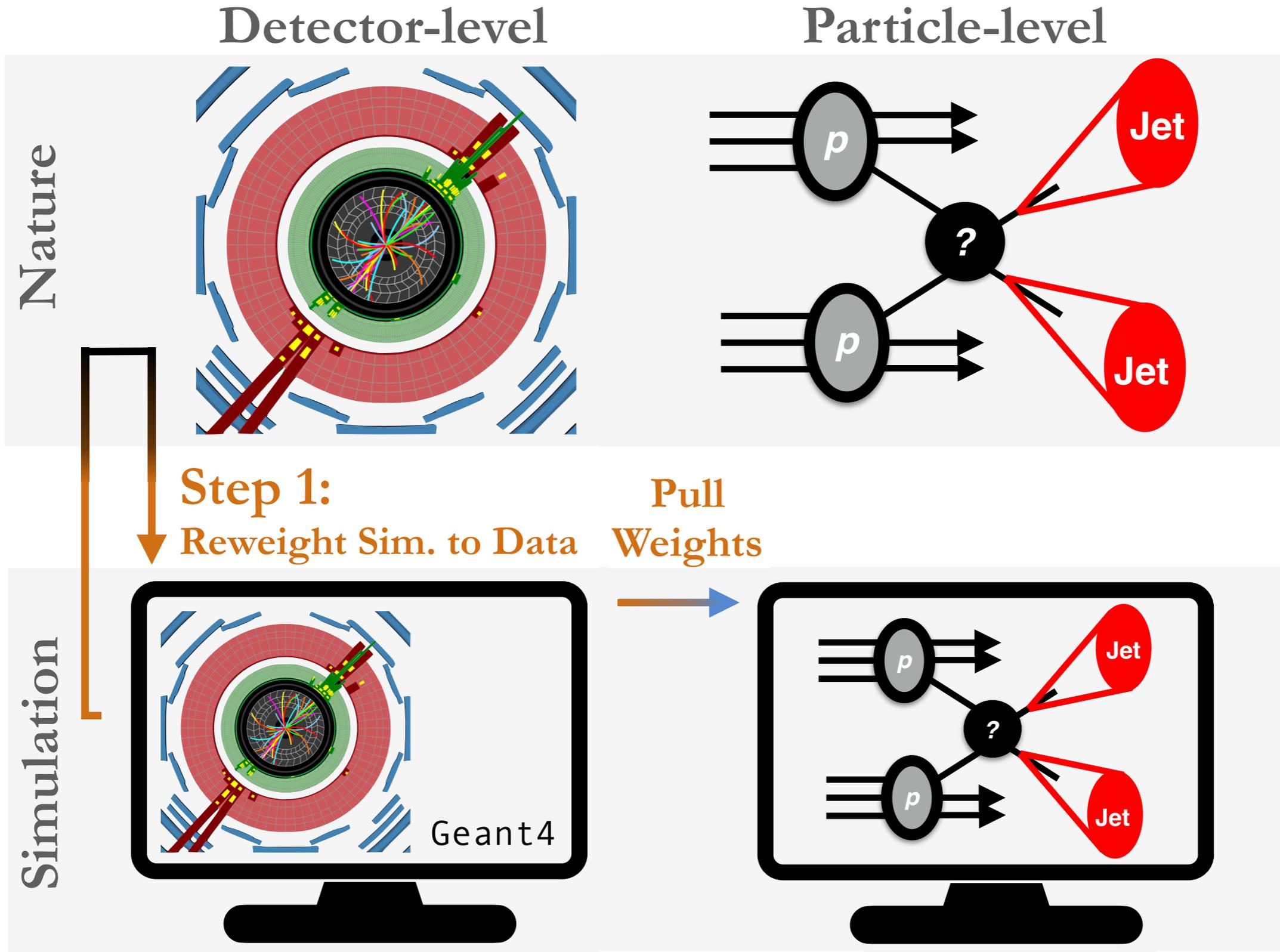
Unbinned, high-dimensional reweighting performed with neural networks

Step 1:
Reweight Sim. to Data



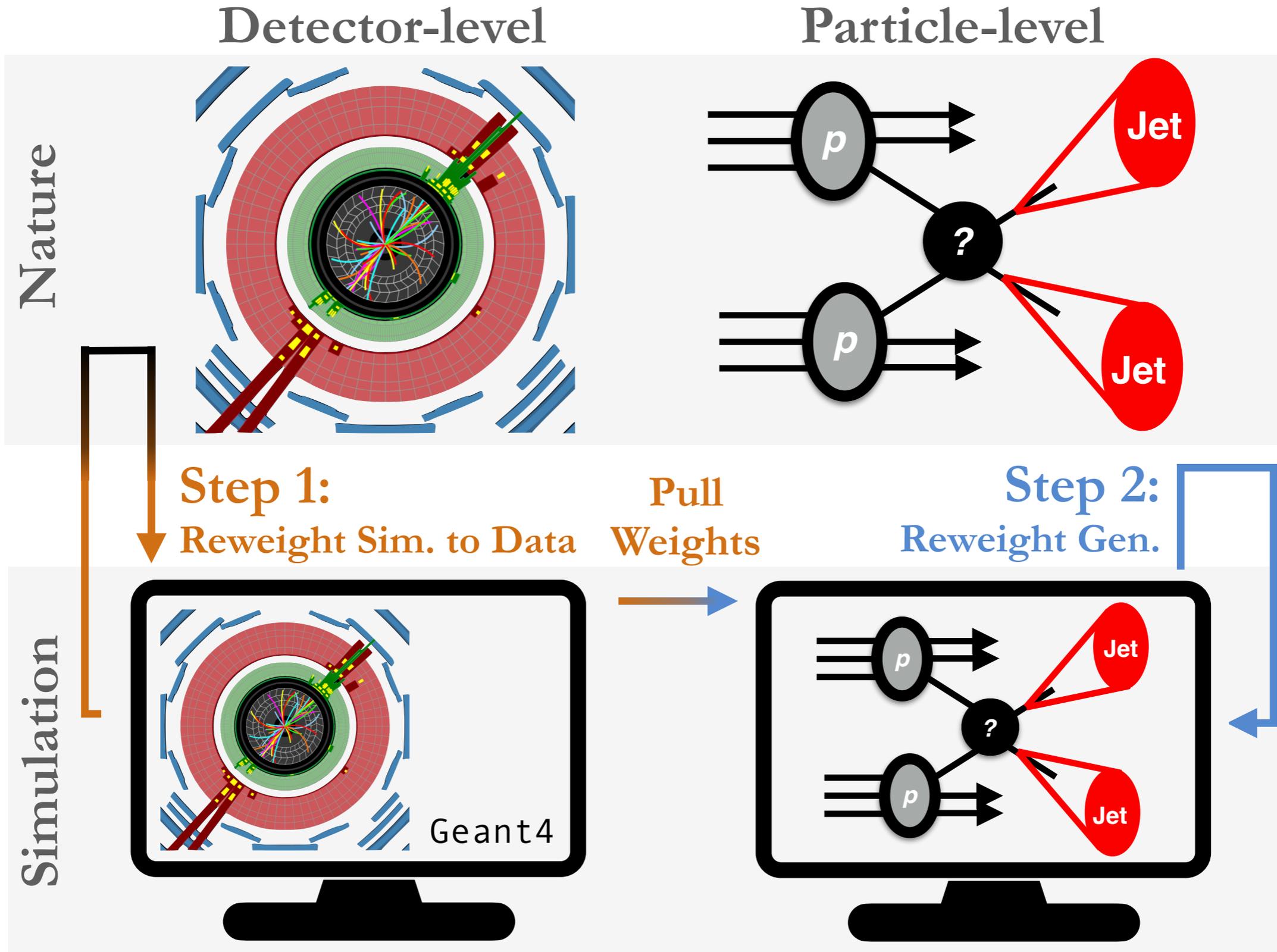
A brief introduction to OmniFold

48



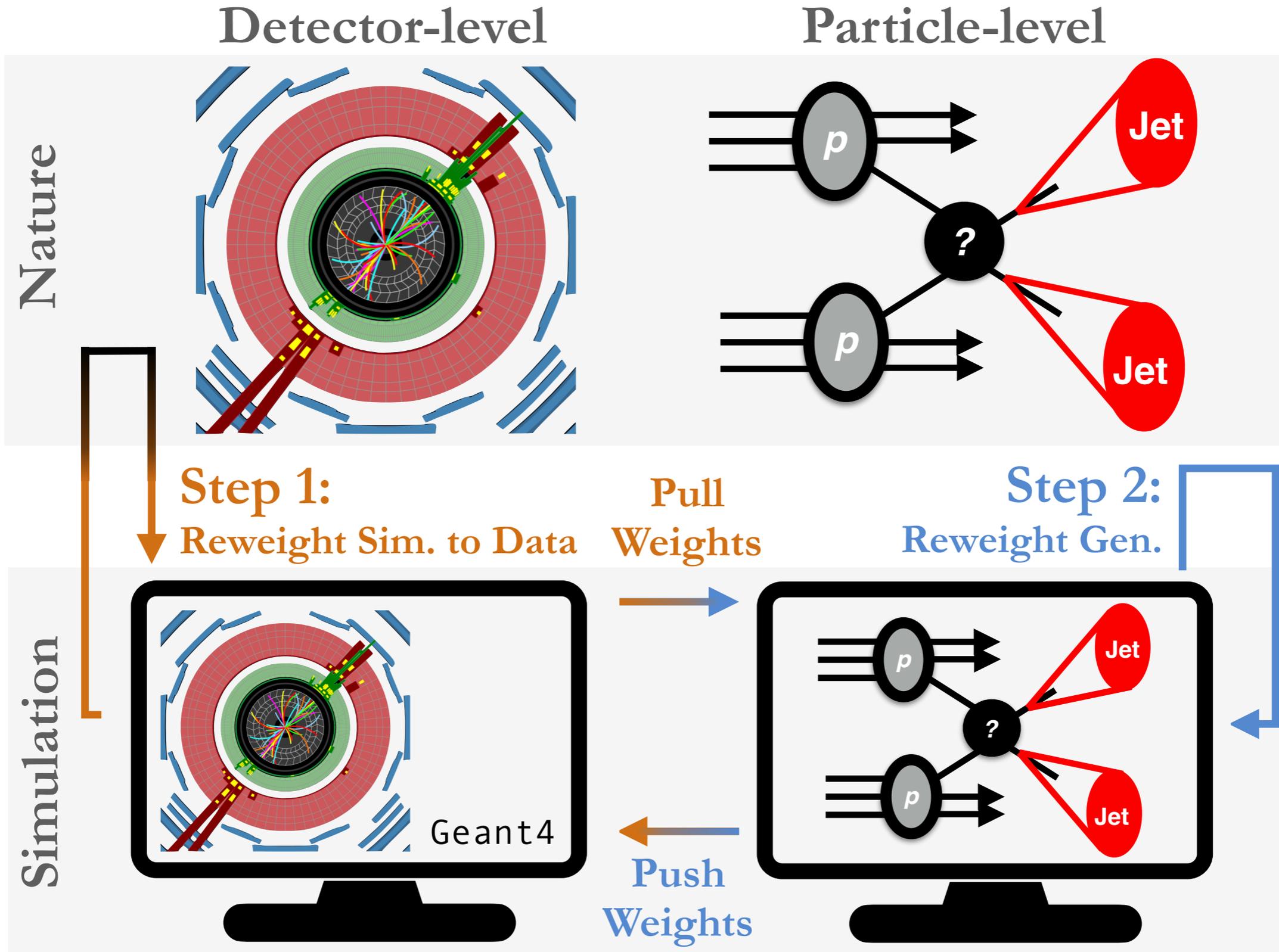
A brief introduction to OmniFold

49



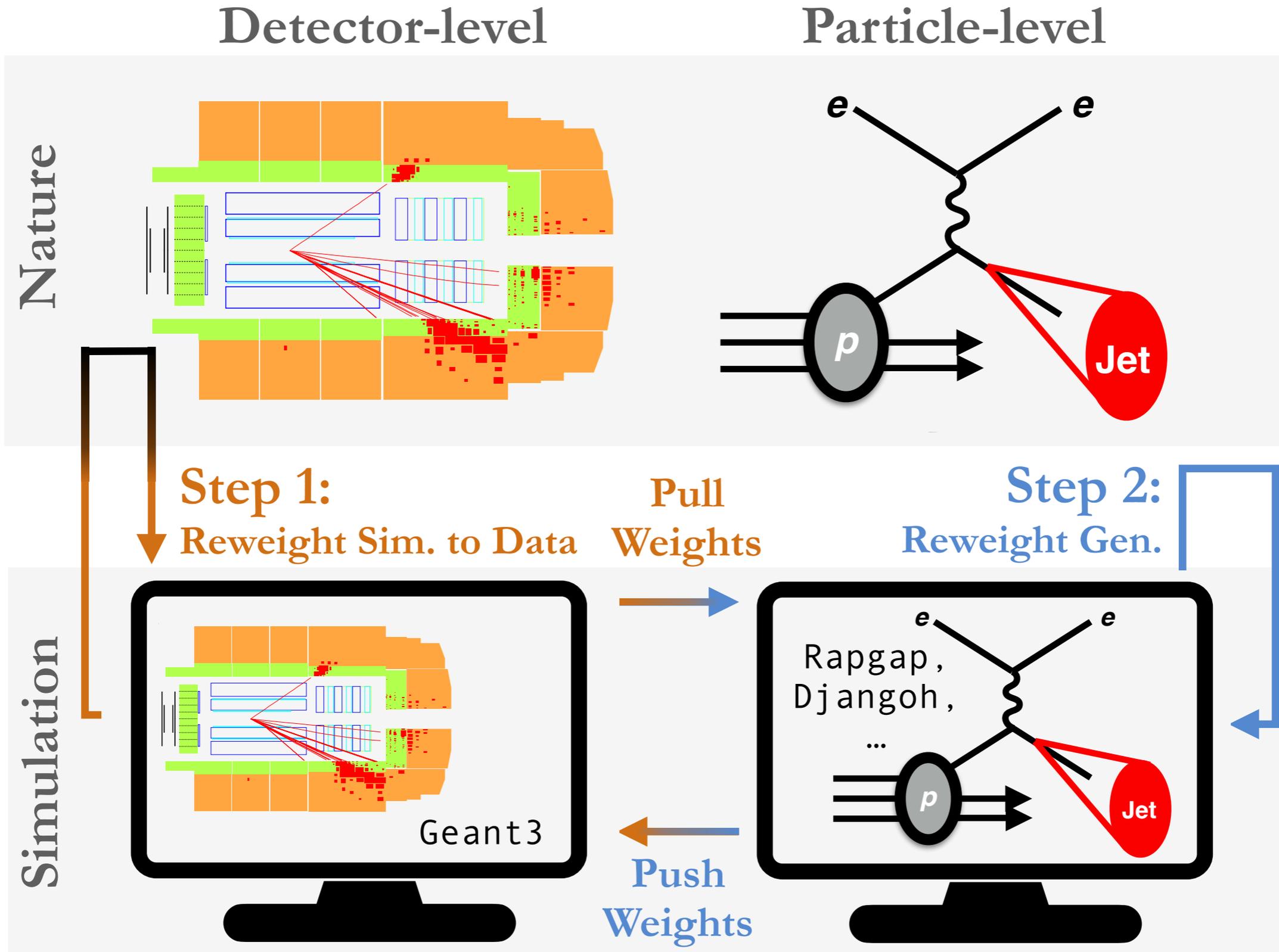
A brief introduction to OmniFold

50



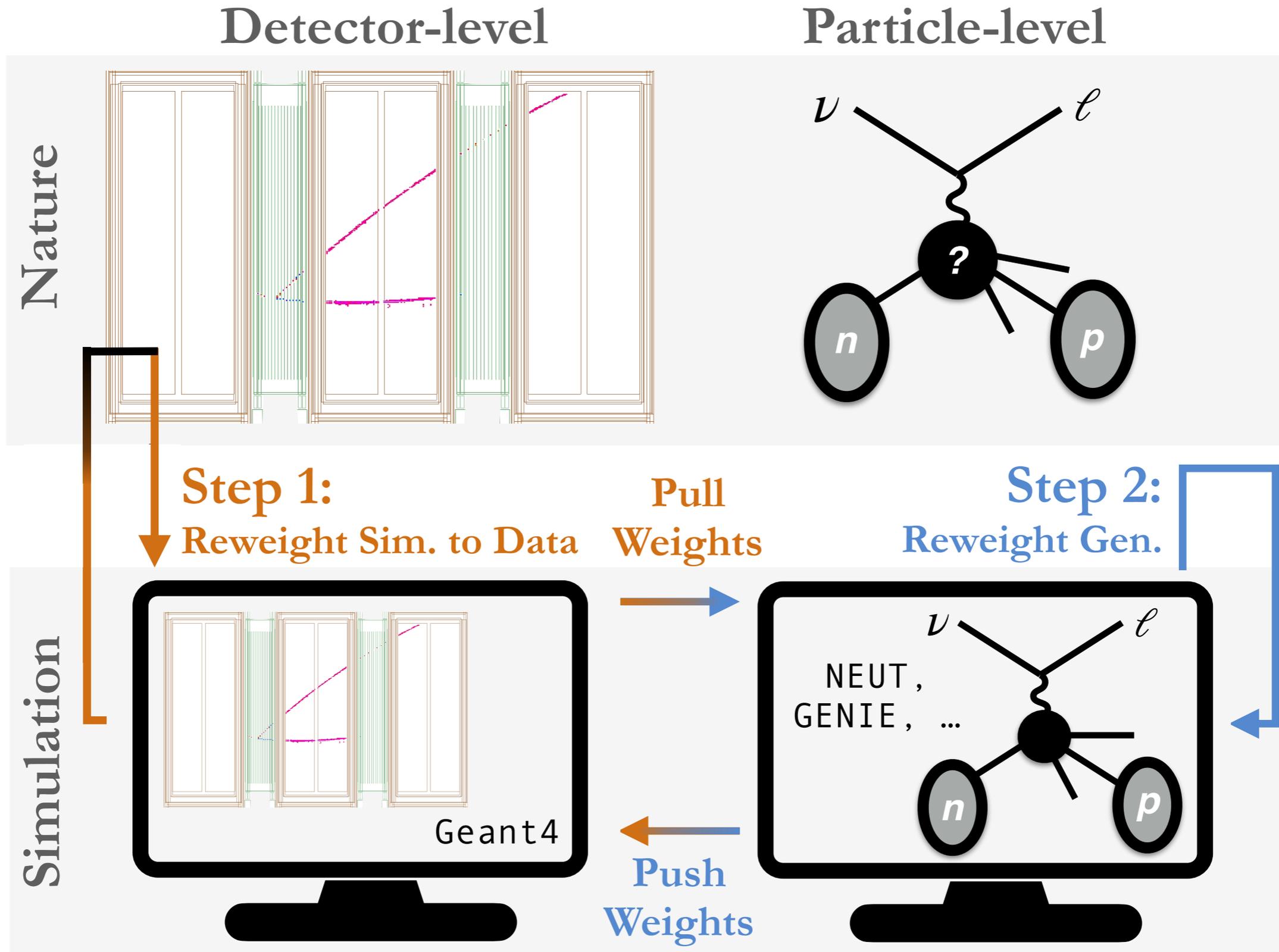
A brief introduction to OmniFold

51



A brief introduction to OmniFold

52



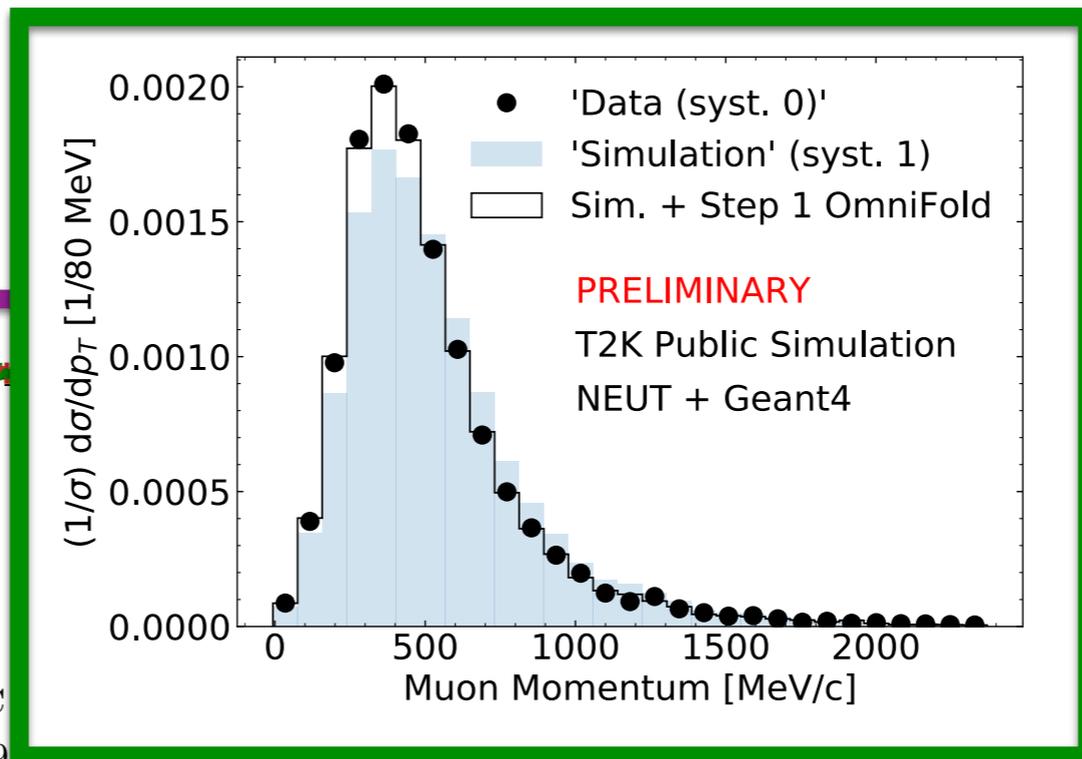
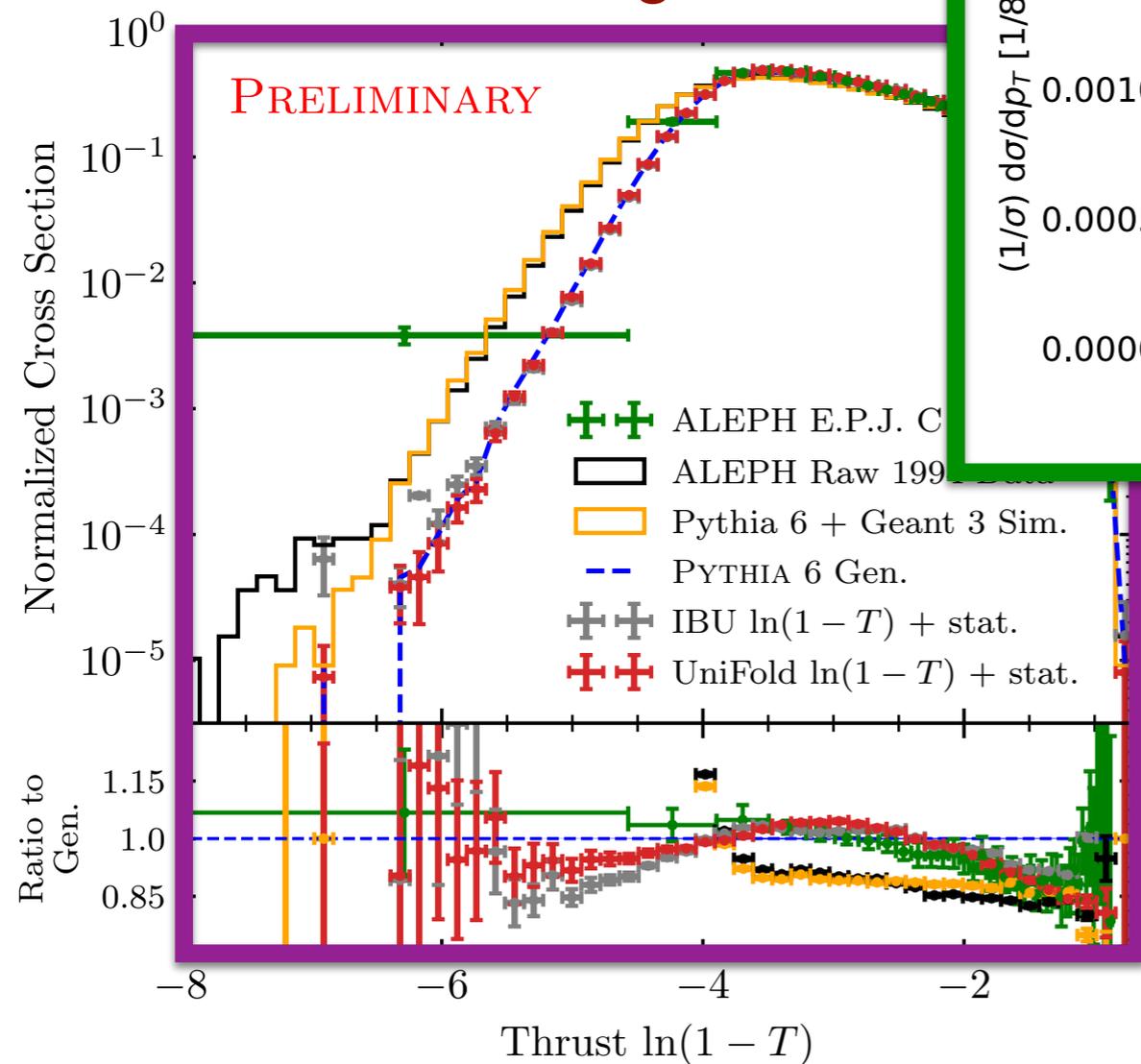
ML-based Unfolding: Science



We are already delivering science results with this methodology (more on the way!); R&D is required to extract the full benefits

ask Jing Pan ↗

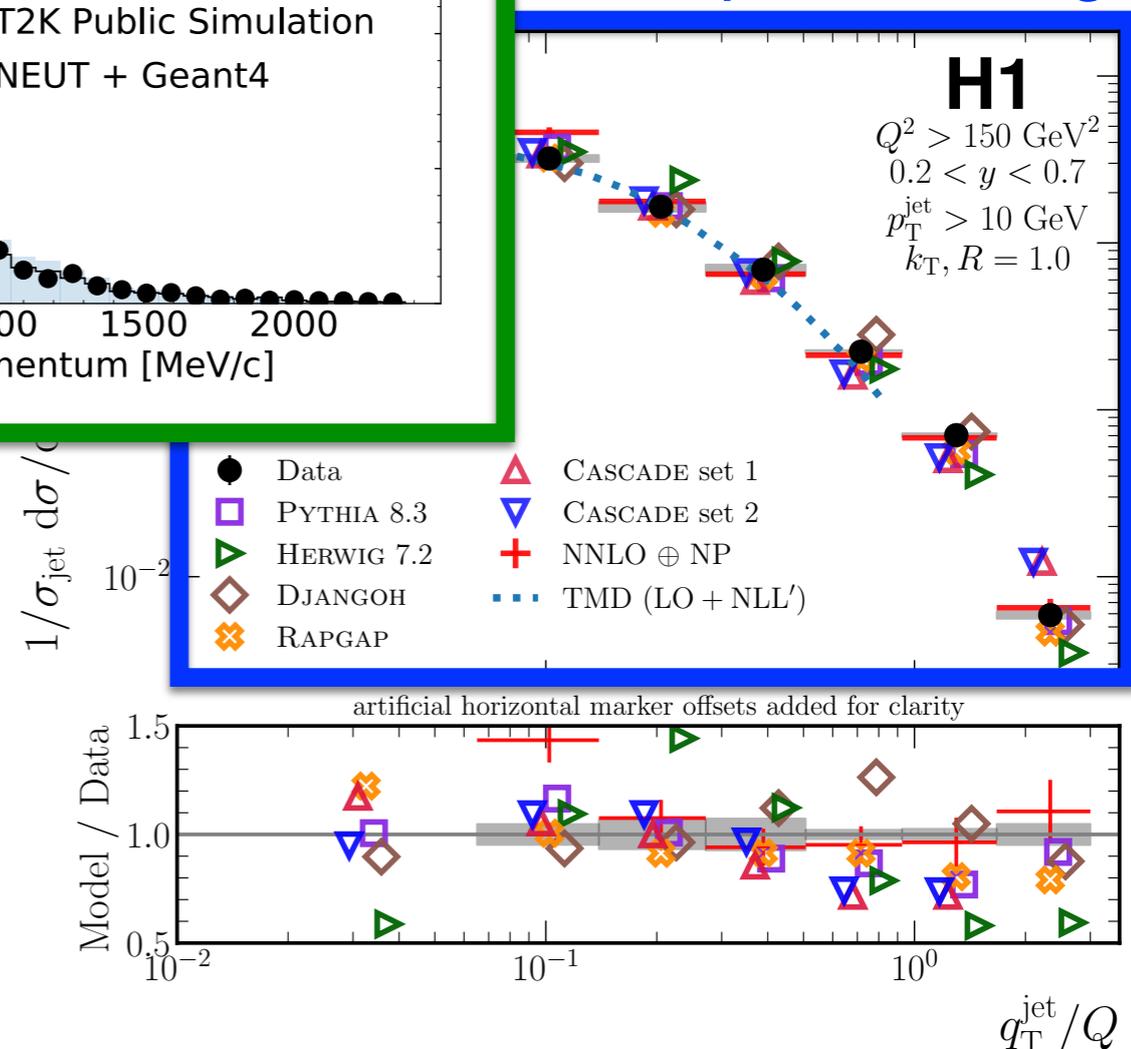
e⁺e⁻ scattering



neutrino scattering

Data points = machine learning

ep scattering

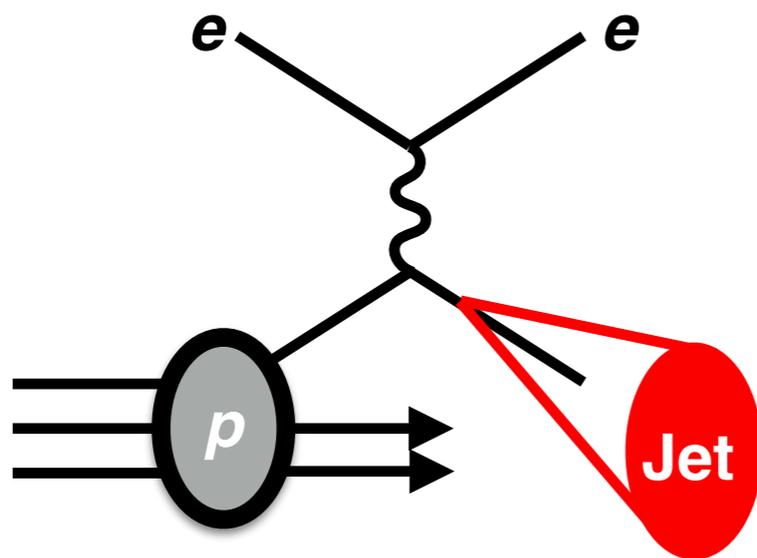


ML-based Unfolding: Science

54

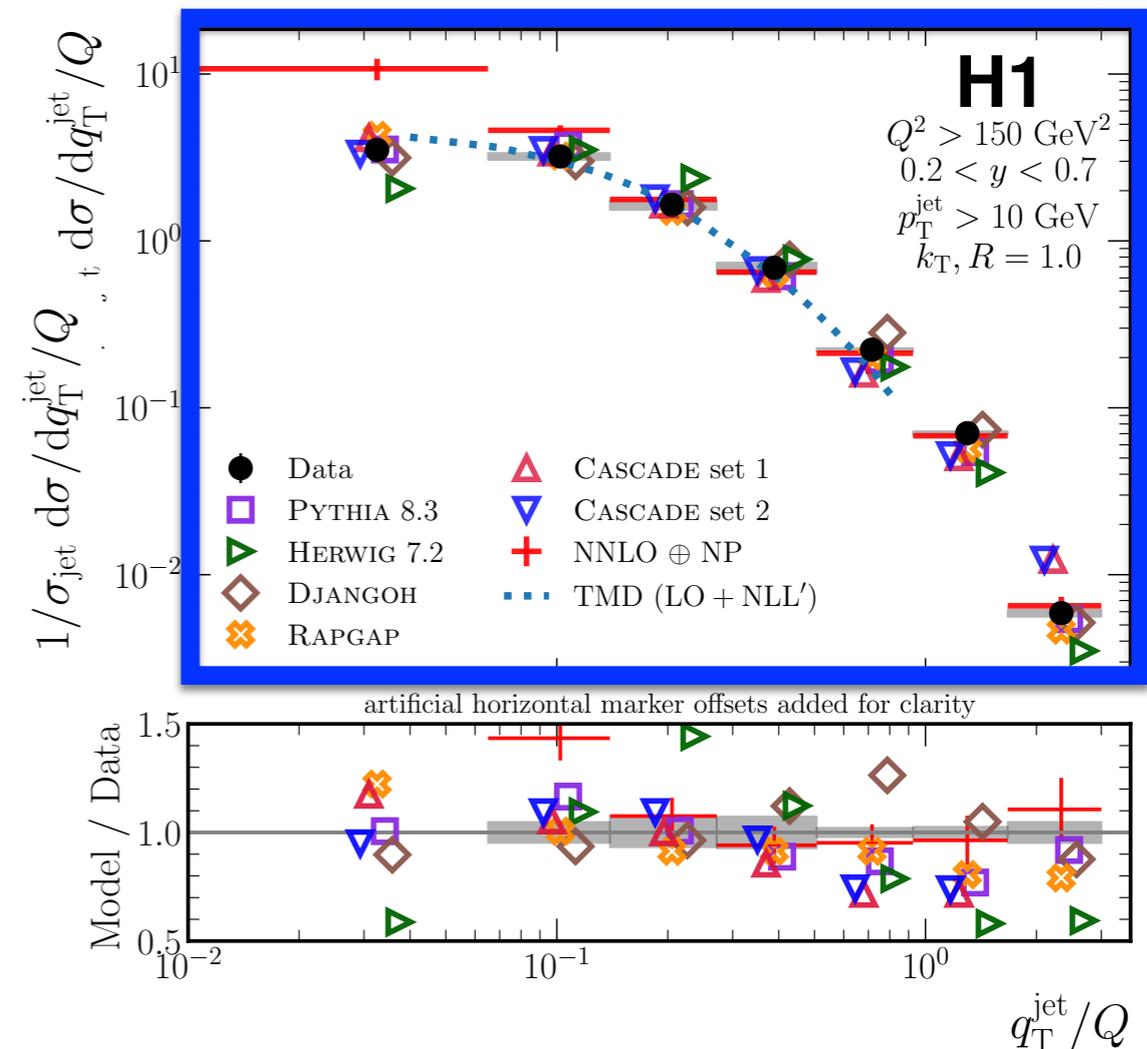
We are already delivering science results with this methodology (more on the way!); R&D is required to extract the full benefits

8-dimensional phase space for exploring proton structure & universality (“factorization”)



Data points = machine learning

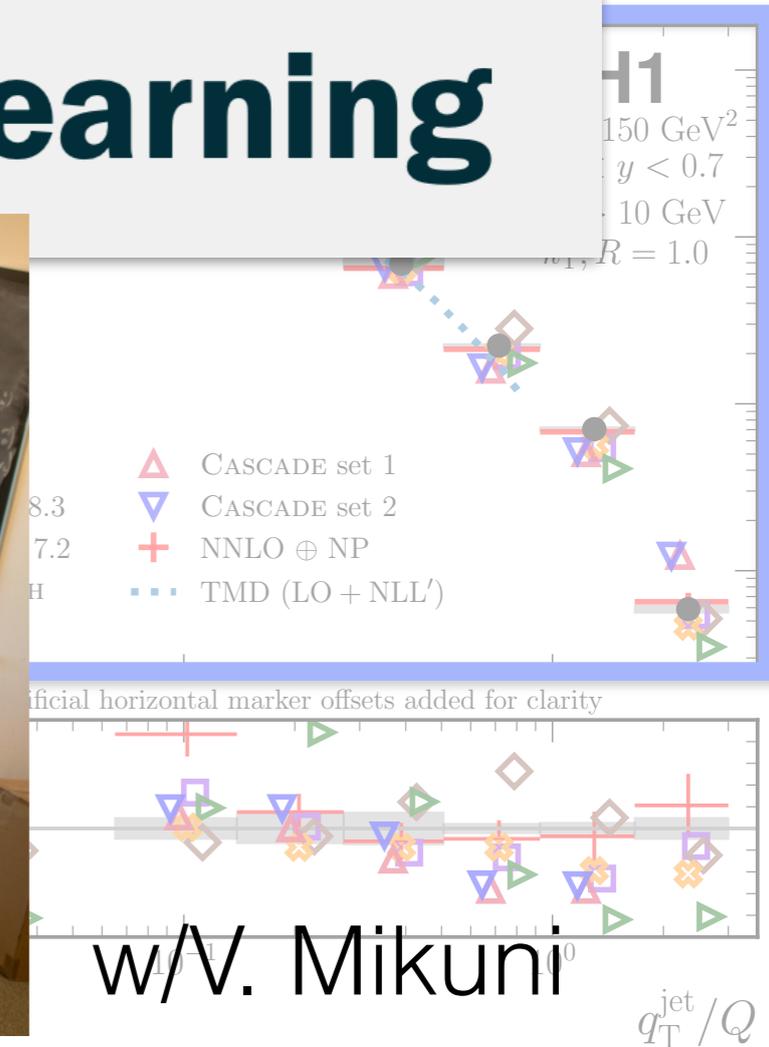
ep scattering



ARTICLE • MYSTERIES OF MATTER

By Theresa Duque
October 25, 2022

How Do You Solve a Problem Like a Proton? You Smash It to Smitherreens – Then Build It Back Together With Machine Learning



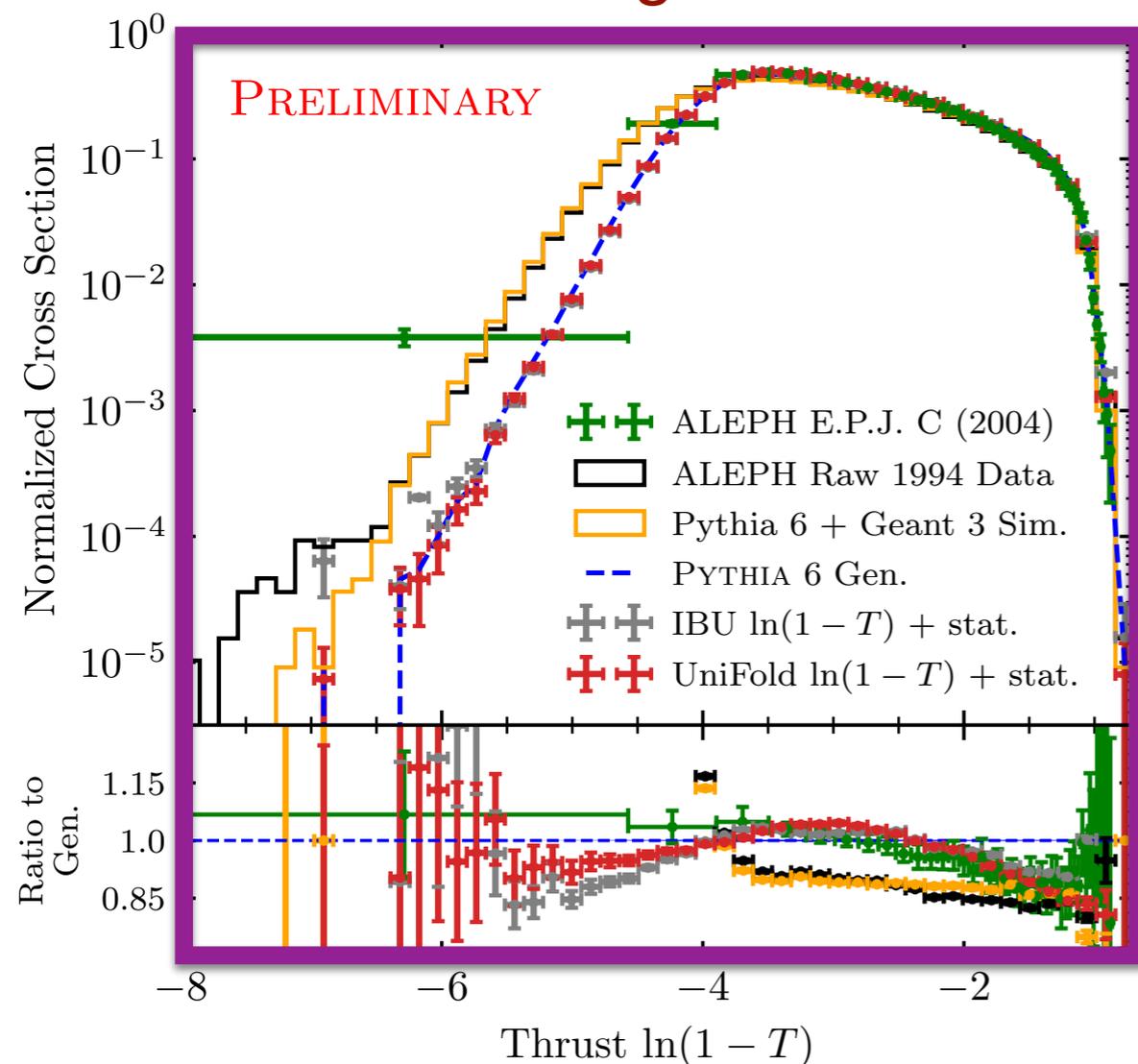
ML-based Unfolding: Science

56

We are already delivering science results with this methodology (more on the way!); R&D is required to extract the full benefits

**Data points =
machine learning**

e⁺e⁻ scattering



Long-standing tension ($\sim 3\sigma$) between methods for measuring the strong coupling constant.

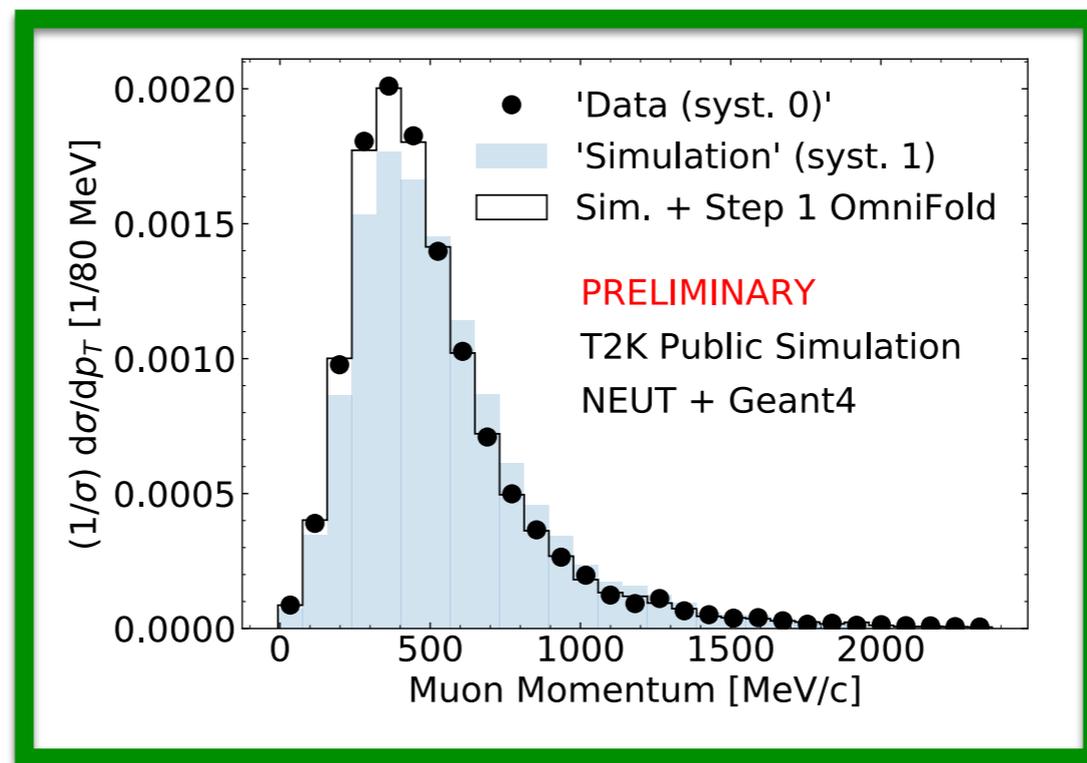
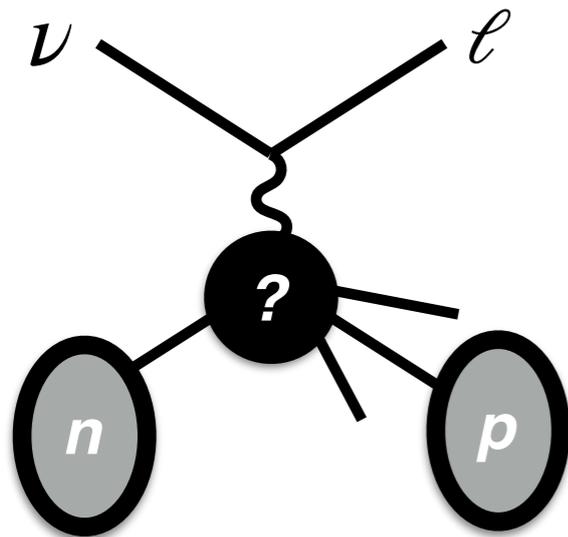
Goal: Use ML to shed light on this issue.

w/A. Badea, Y.-J. Lee, J. Thaler

ML-based Unfolding: Science

57

We are already delivering science results with this methodology (more on the way!); R&D is required to extract the full benefits



*neutrino
scattering*

**Data points =
machine learning**

Highly-variable detector response in T2K detector can be addressed with ML unfolding.

w/C. Wilkinson and T. Kikawa

The future of likelihood-free Inference

58

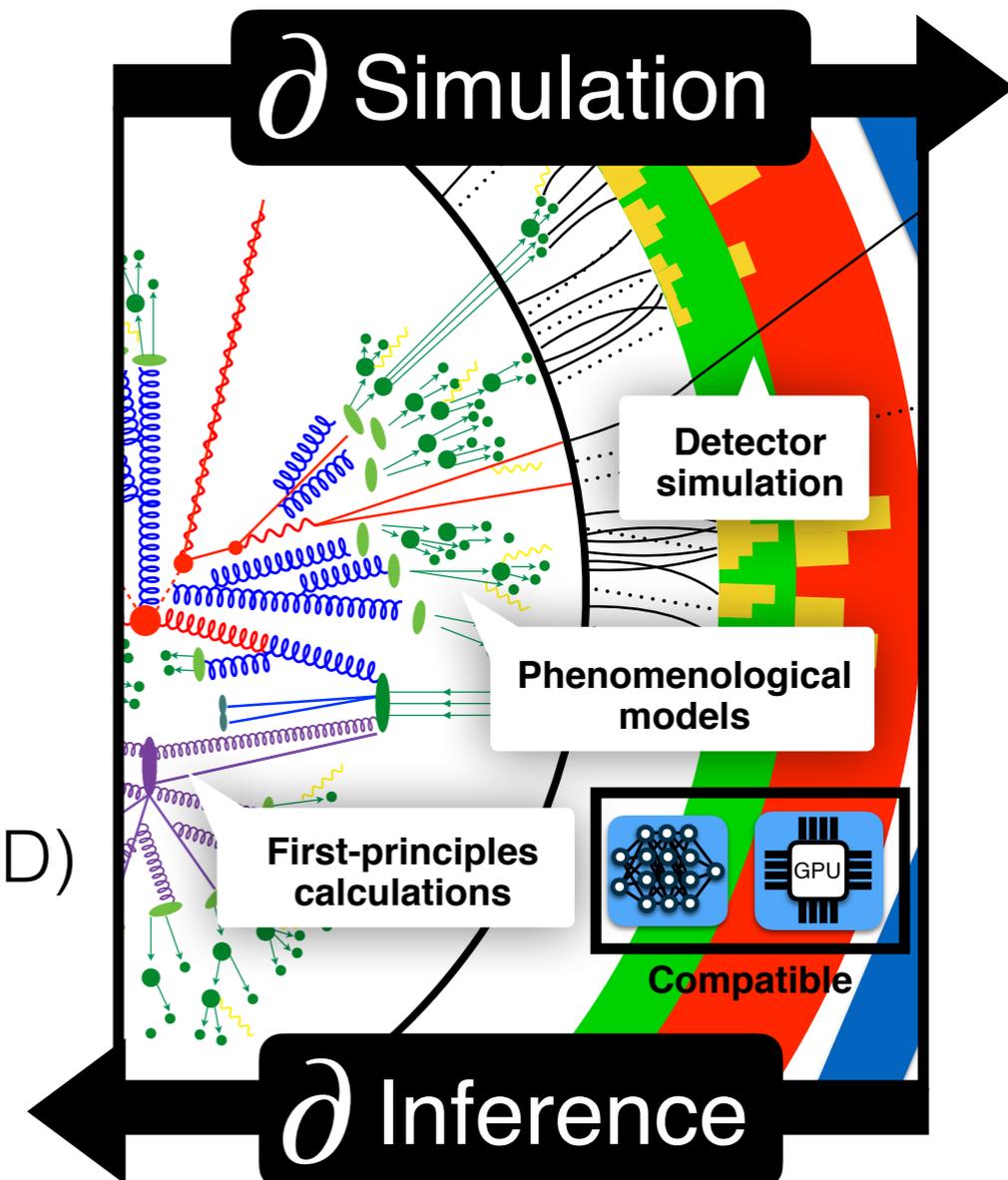
Goal: optimal combination of simulations & machine learning

Methods

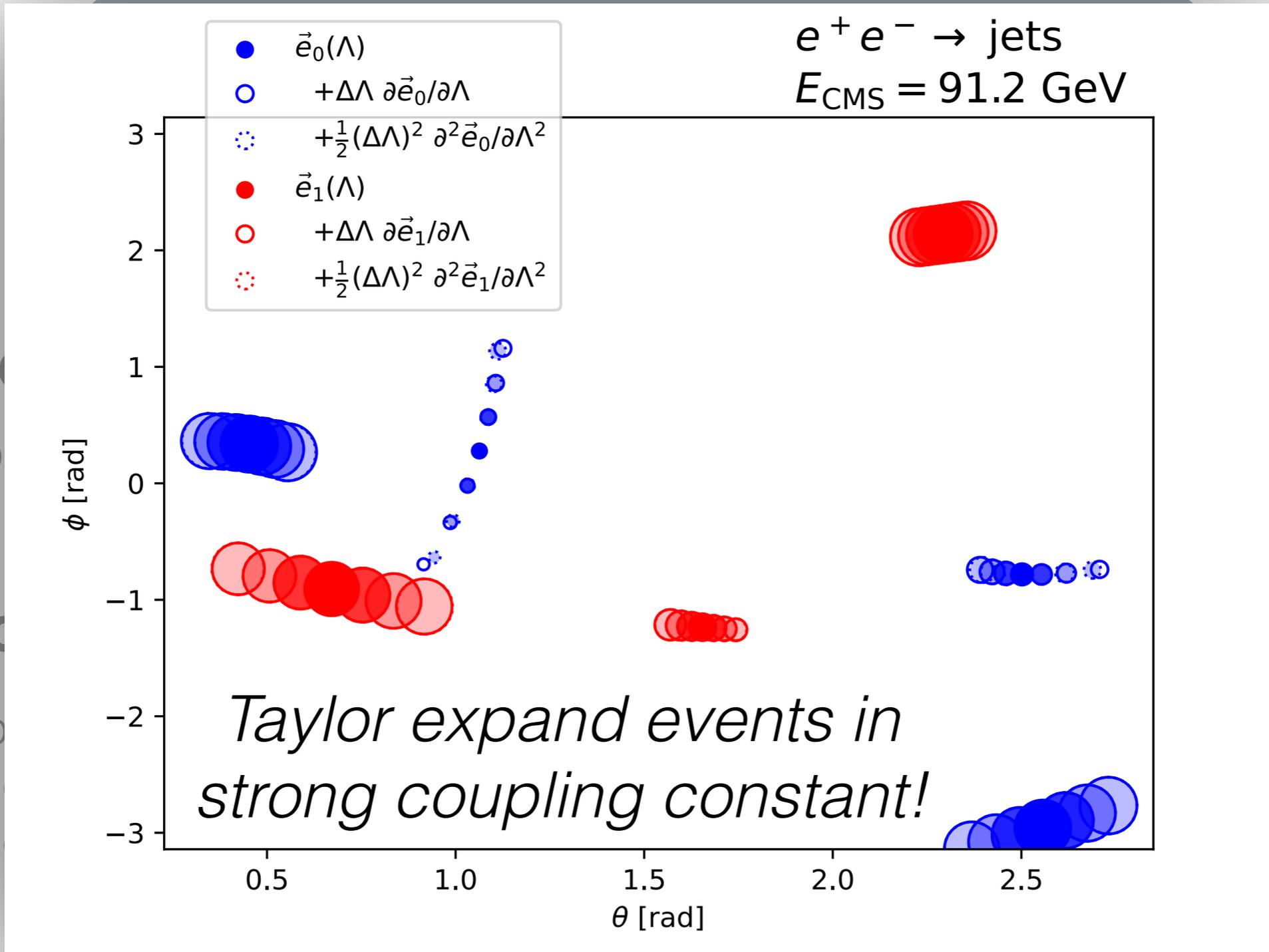
Next frontier: **differentiable simulations**

Science

- Detector optimization
- Cross sections from ATLAS and T2K/LArTPC
- Cross sections from legacy data (HERA/LEP/SLD)



The future of likelihood-free Inference

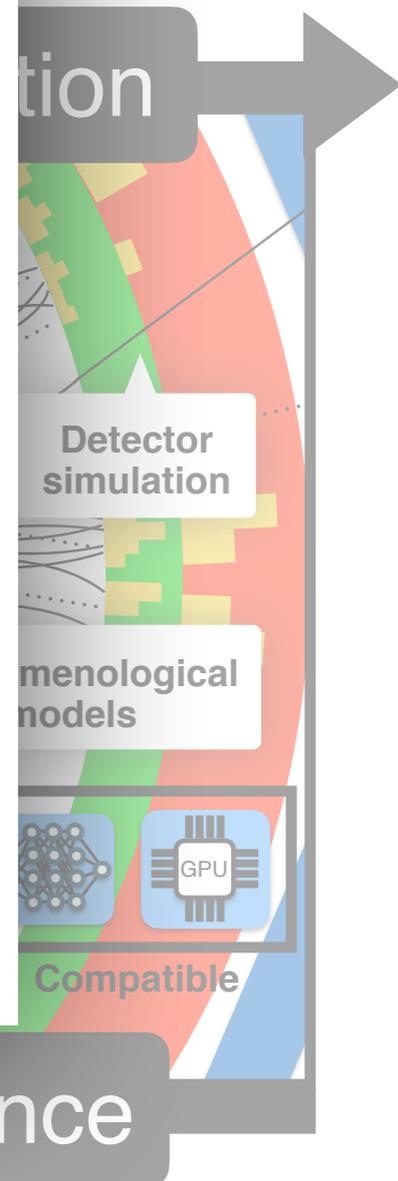


Method

Next from

Science

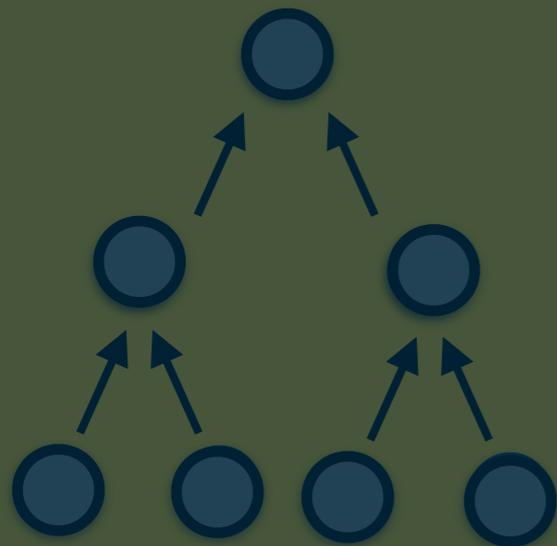
- Detector
- Cross s
- Cross s



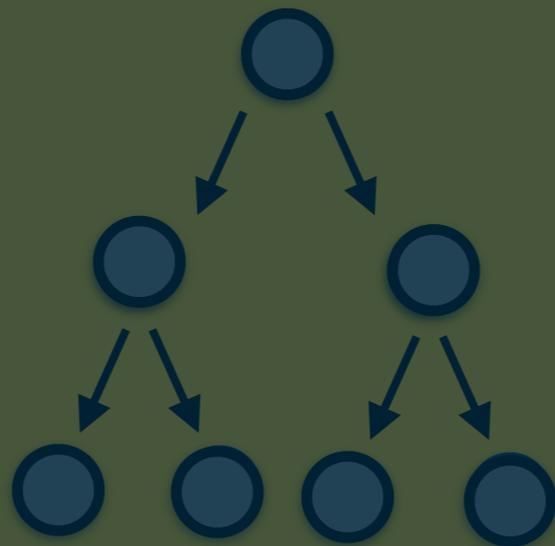
Outline for today

60

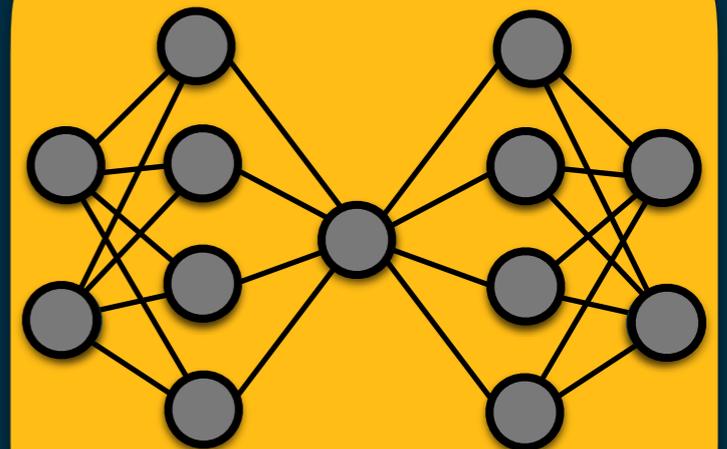
I'll focus on three core, cross-cutting areas of $ML \cap Physics$



Forward Models
(fast simulation)



Inverse Models
(unfolding)

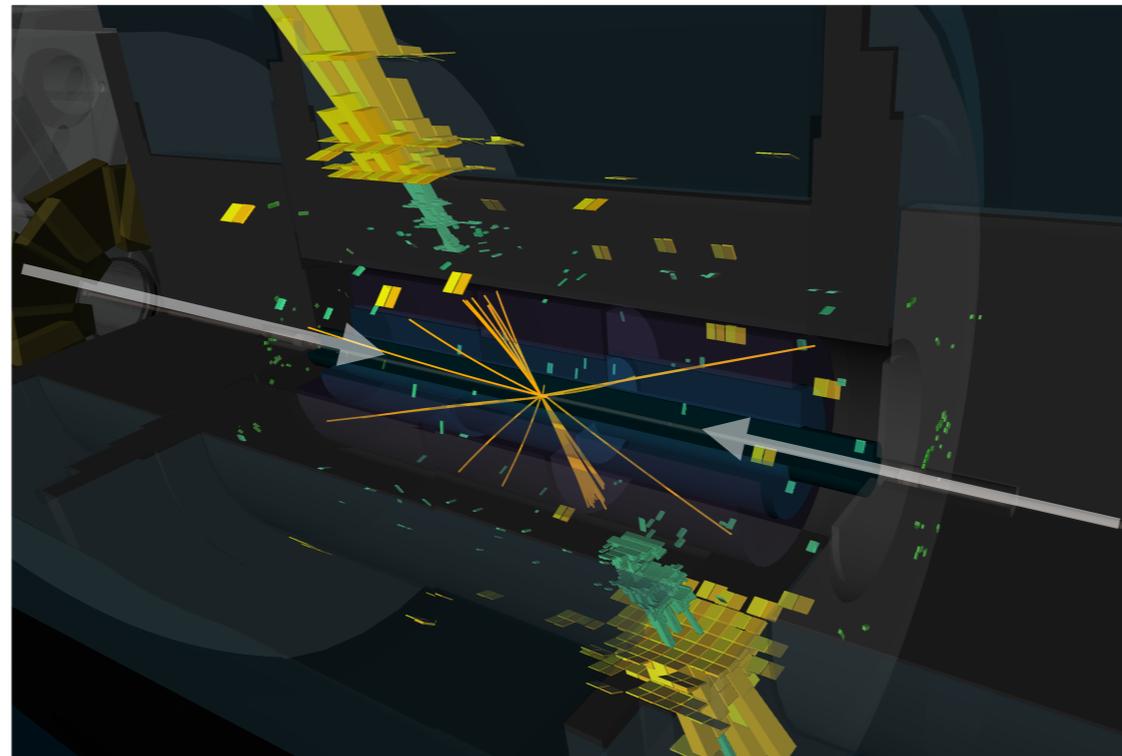


Simulation-free
(anomaly detection)

To illustrate these exciting topics, I'll give one vignette per area

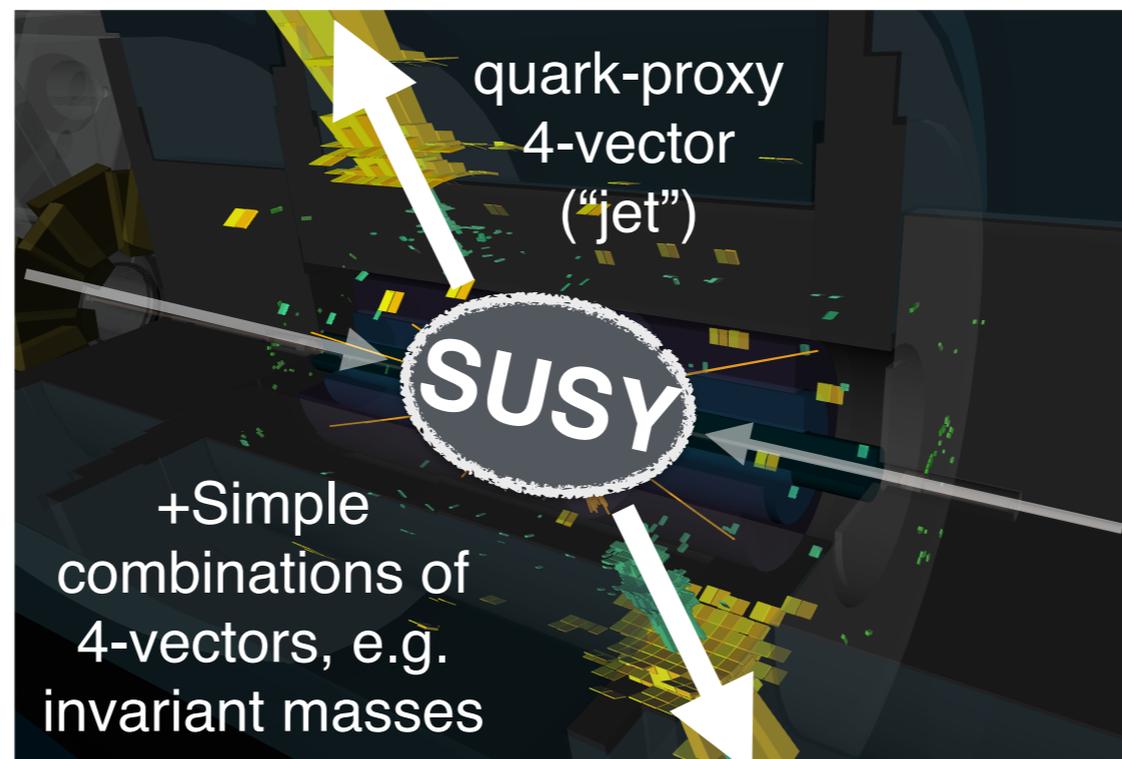
Nearly all searches for new particles are signal-model driven. We have introduced a new model agnostic program.

AD in fundamental physics is inherently different than other areas of science and industry - we need new approaches.



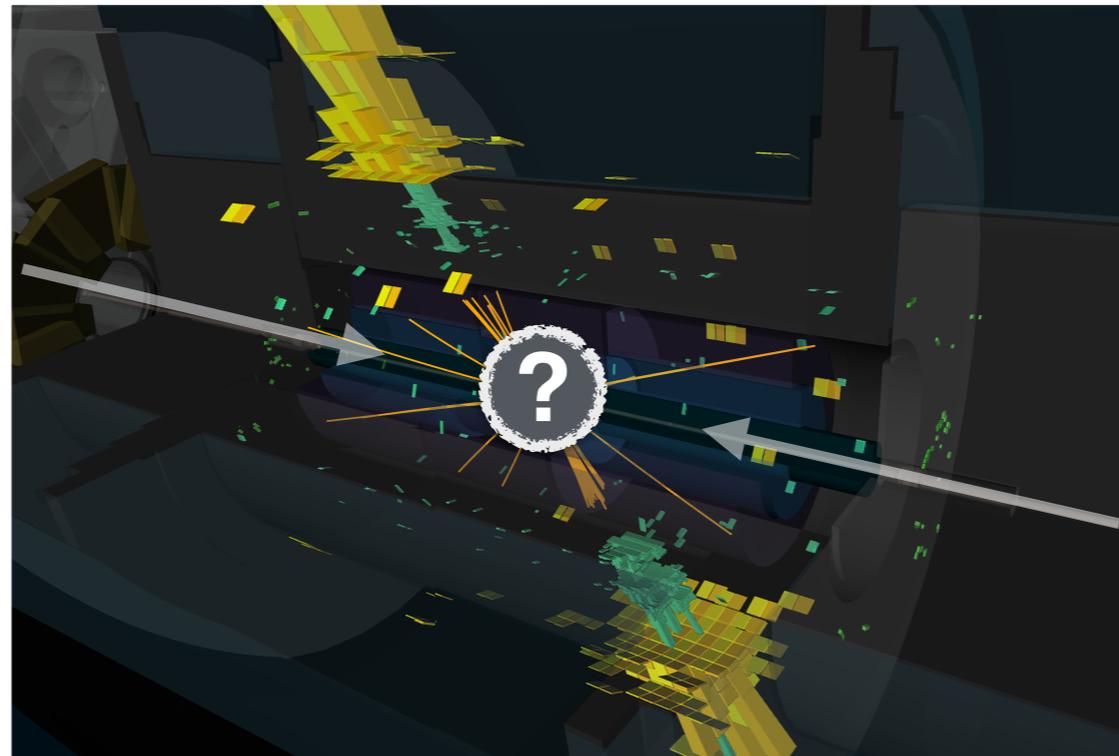
Nearly all searches for new particles are signal-model driven. We have introduced a new model agnostic program.

AD in fundamental physics is inherently different than other areas of science and industry - we need new approaches.



Nearly all searches for new particles are signal-model driven. We have introduced a new model agnostic program.

AD in fundamental physics is inherently different than other areas of science and industry - we need new approaches.



I like to categorize new ideas based on the core assumption about the new physics, which is intimately related to the technique ***supervision***

Unsupervised = no labels

Weakly-supervised = noisy labels

Semi-supervised = partial labels

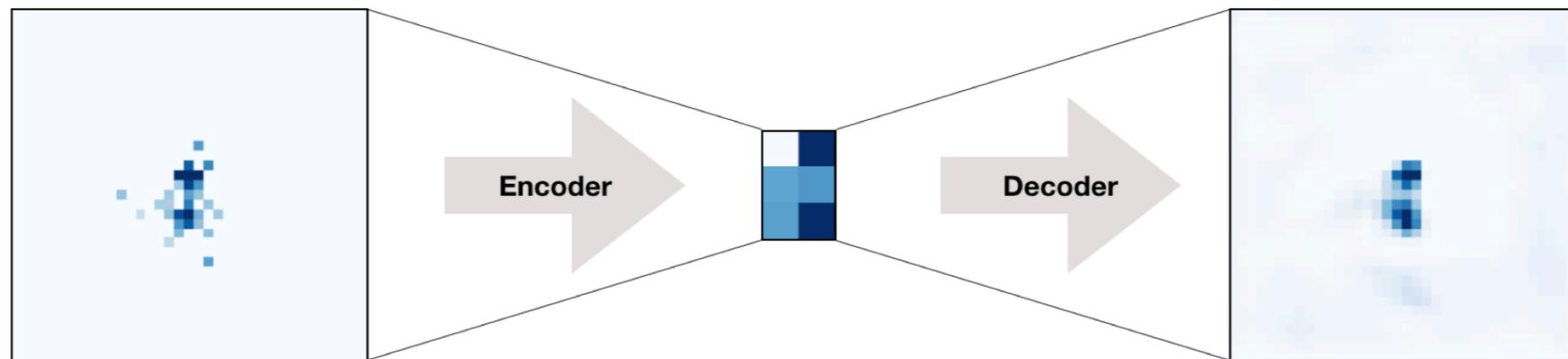
Supervised = full label information



This is most searches. You simulate the signal (label = 1), simulate the background (label = 0) and “train” a classifier to distinguish the 1’s from the 0’s.

Unsupervised = no labels

Typically, the goal of these methods is to look for events with **low $p(\text{background})$**

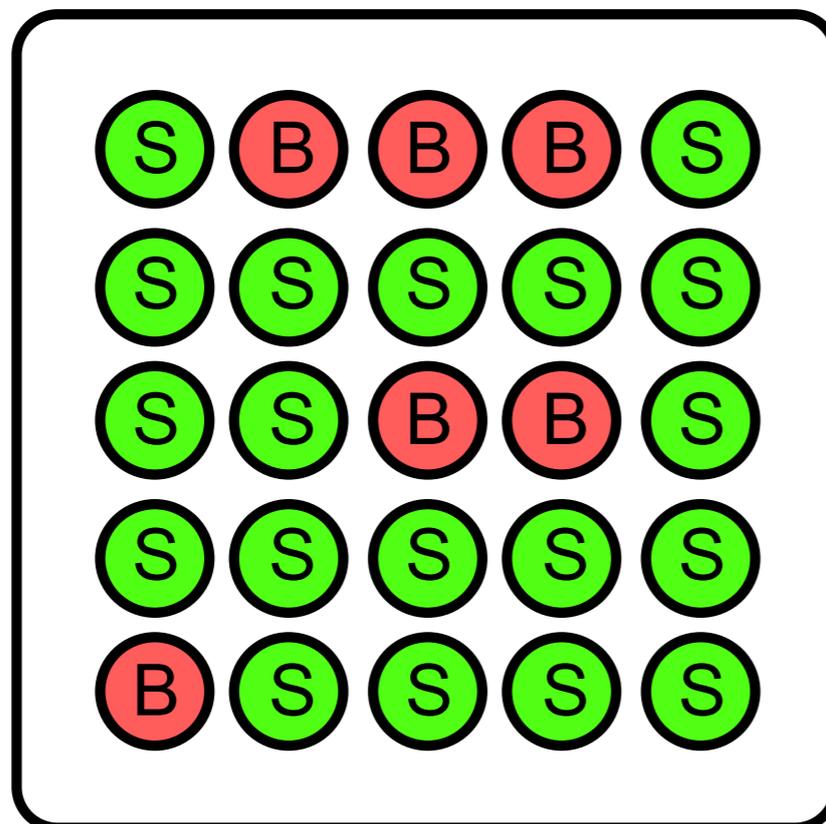


One strategy (autoencoders) is to try to compress events and then uncompress them. When $x = \text{uncompress}(\text{compress}(x))$, then x probably has low $p(x)$.

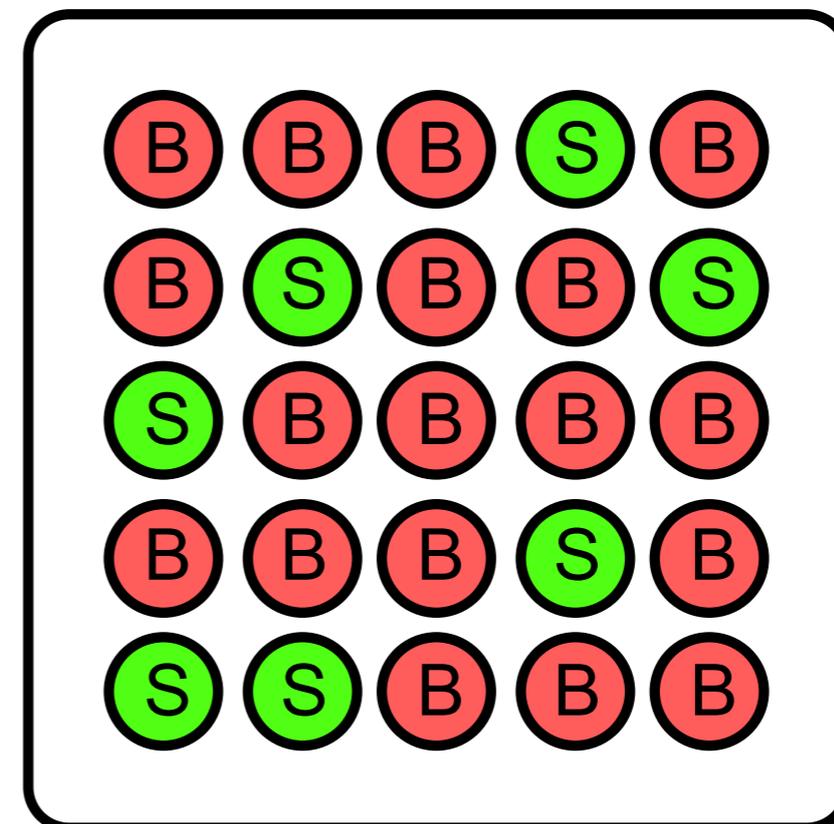
Weakly-supervised = noisy labels

Typically, the goal of these methods is to look for events with high $p(\text{possibly signal-enriched})/p(\text{possibly signal-depleted})$

Signal enriched



Signal depleted



Semi-supervised

67

Semi-supervised = partial labels

Typically, these methods use some signal simulations to build signal sensitivity



vs



e.g. SM background versus many signals

Approach:	Unsupervised	Weakly supervised
BSM assumption	Signal is rare (low p)	Signal is an over density (high p ratio)
Main drawback	rare is not invariant* under coordinate transformations!	need two samples

*for a detailed discussion about this, see G. Kasieczka et al., 2209.06225

Approach:

Unsupervised

Weakly supervised

BSM assumption

Signal is rare
(low p)

Signal is an
over density
(high p ratio)

Main drawback

rare is not invariant*
under coordinate
transformations!

need two samples

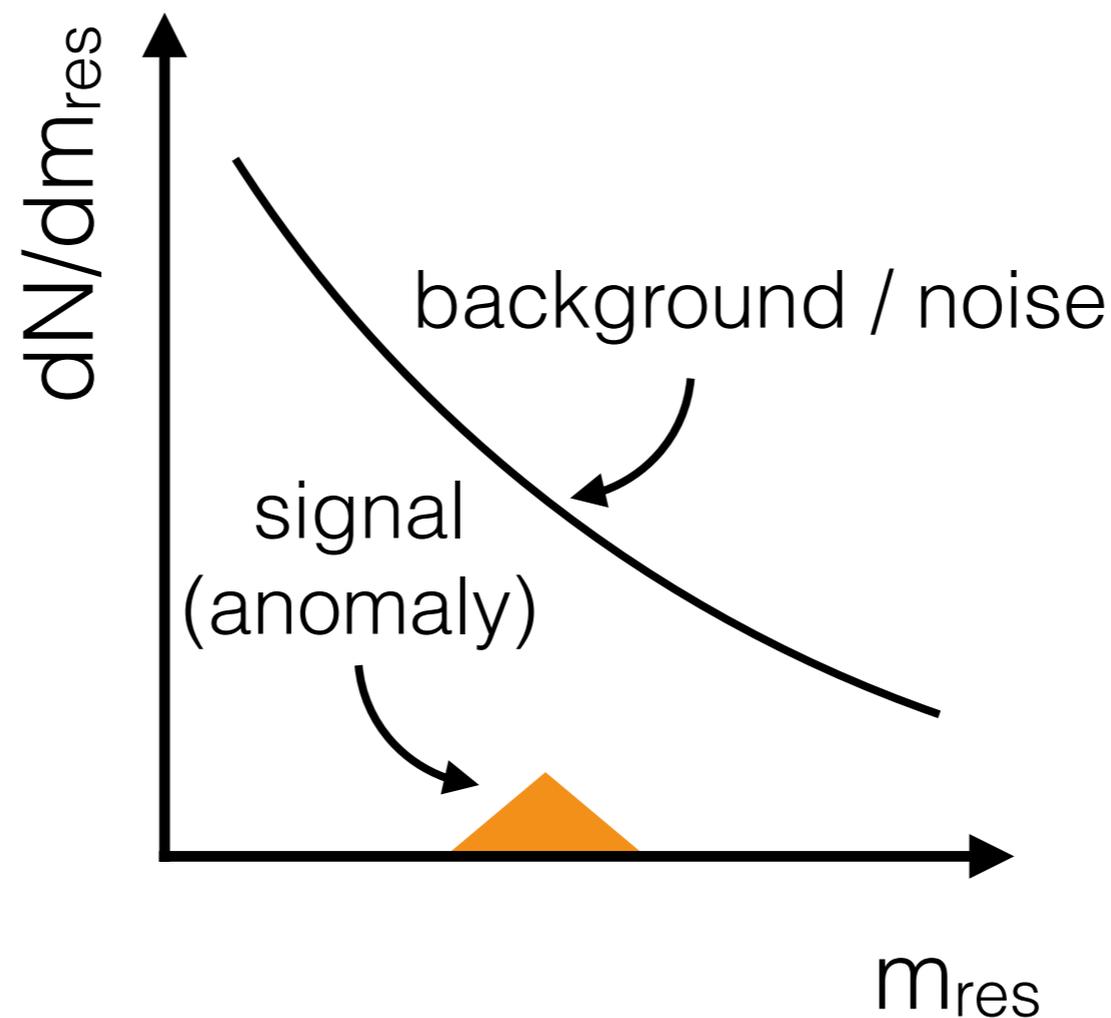
**Cannonical example:
resonances!**

*for a detailed discussion about this, see G. Kasieczka et al., 2209.06225

Resonant Anomalies

70

A relatively general, but powerful assumption is that the anomaly is localized somewhere in phase space.

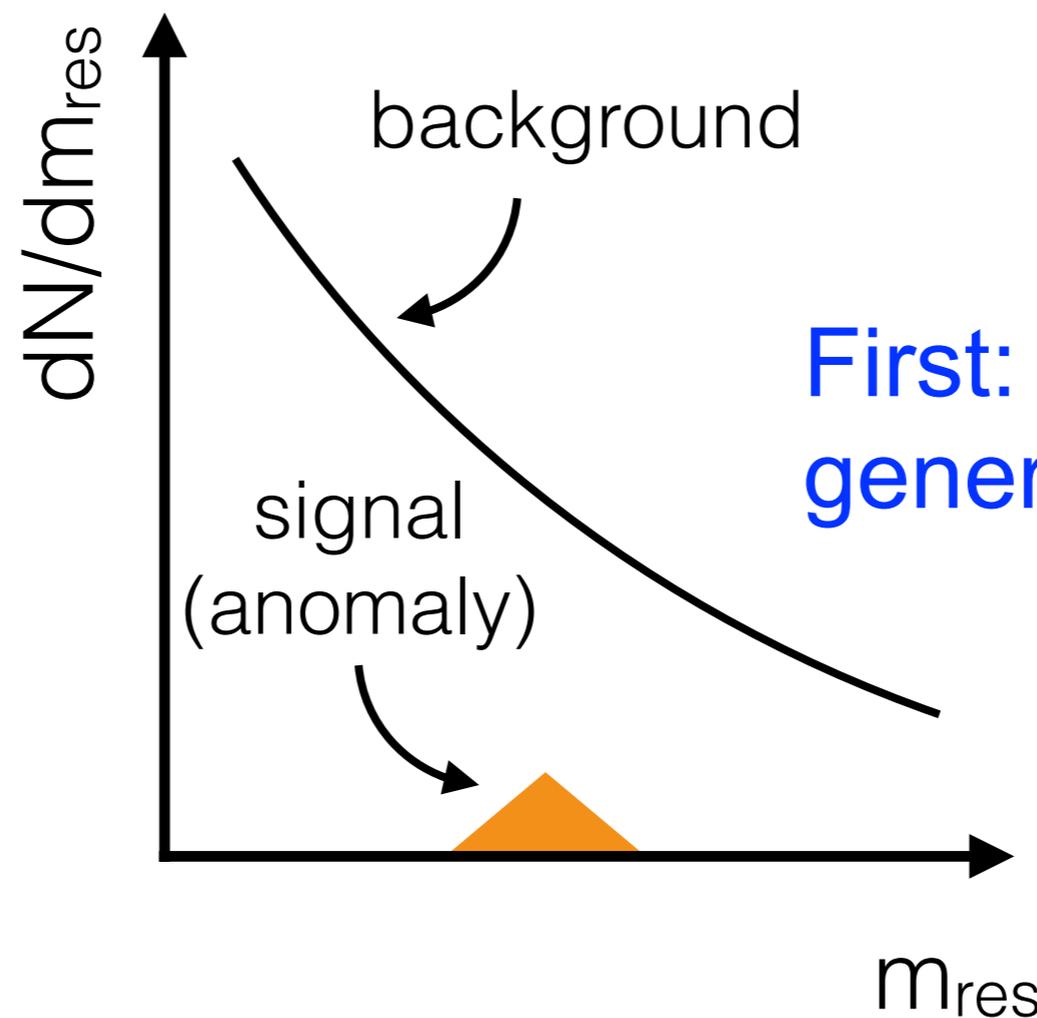


Generically true when there are on-shell new particles or transient phenomena in time series data

Resonant Anomalies

71

A relatively general, but powerful assumption is that the anomaly is localized somewhere in phase space.

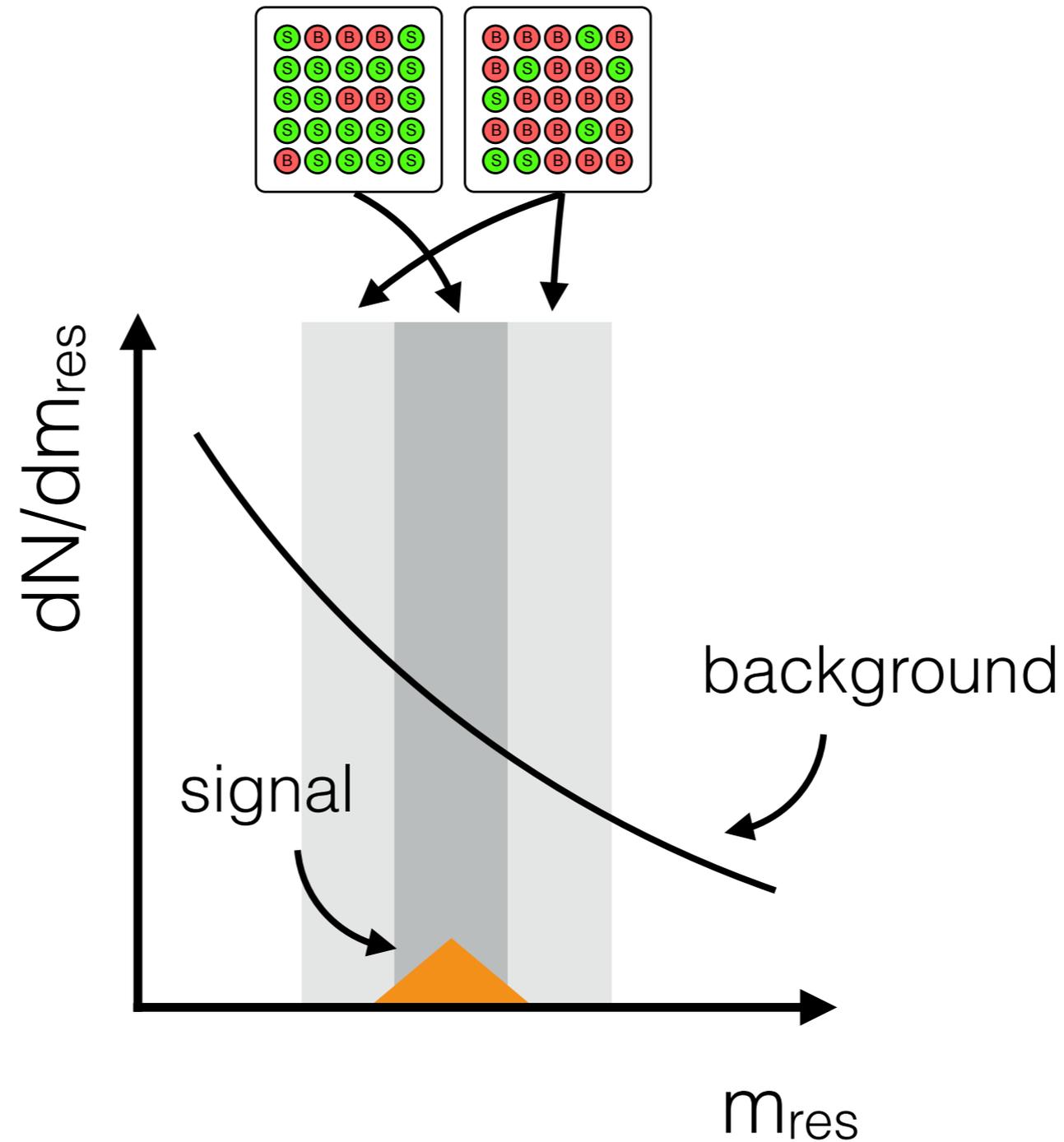


First: we will need to generate noisy labels.

Generically true when there are on-shell new particles or transient phenomena in time series data

Resonant Anomalies

72

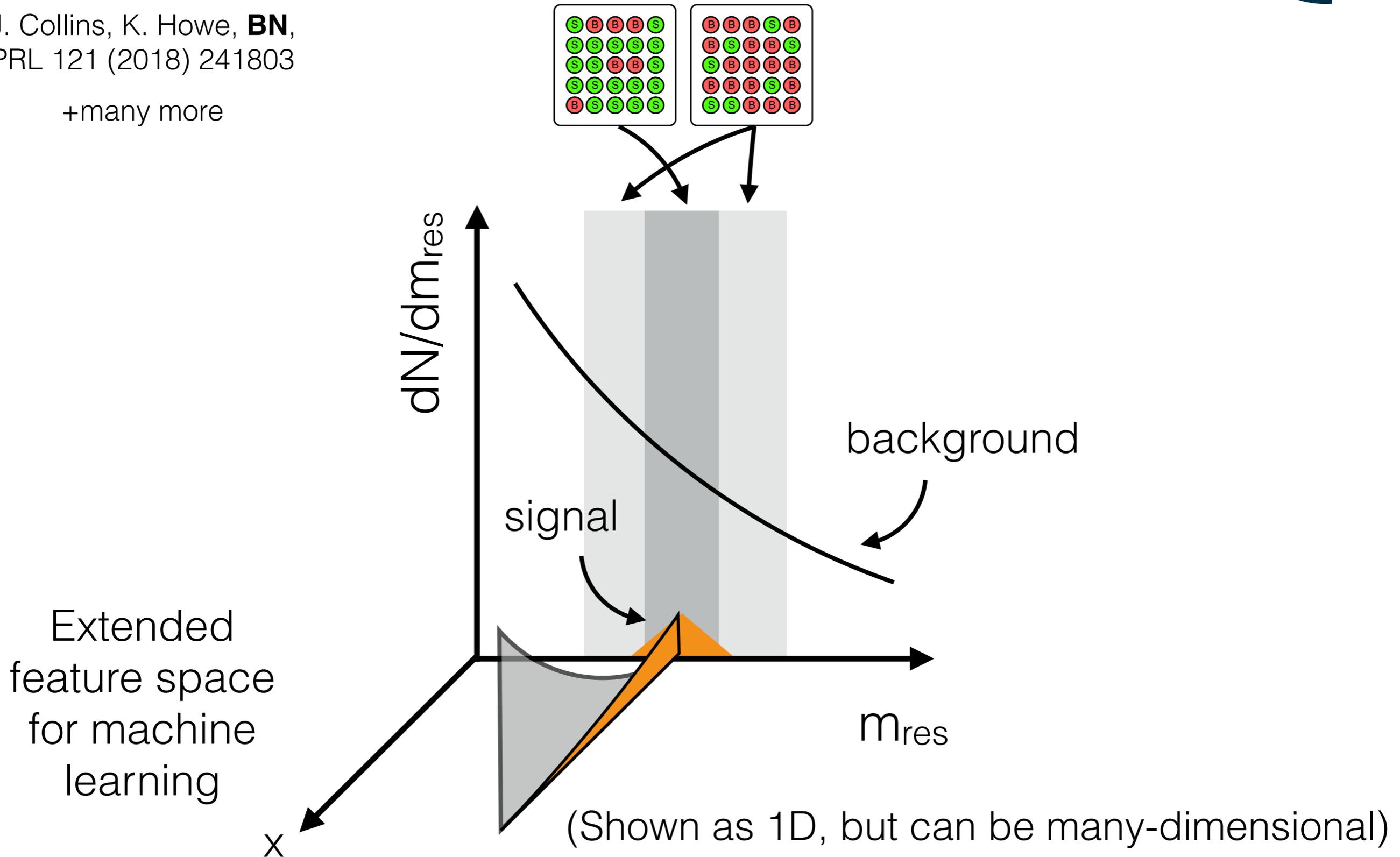


First: we will need to generate noisy labels.

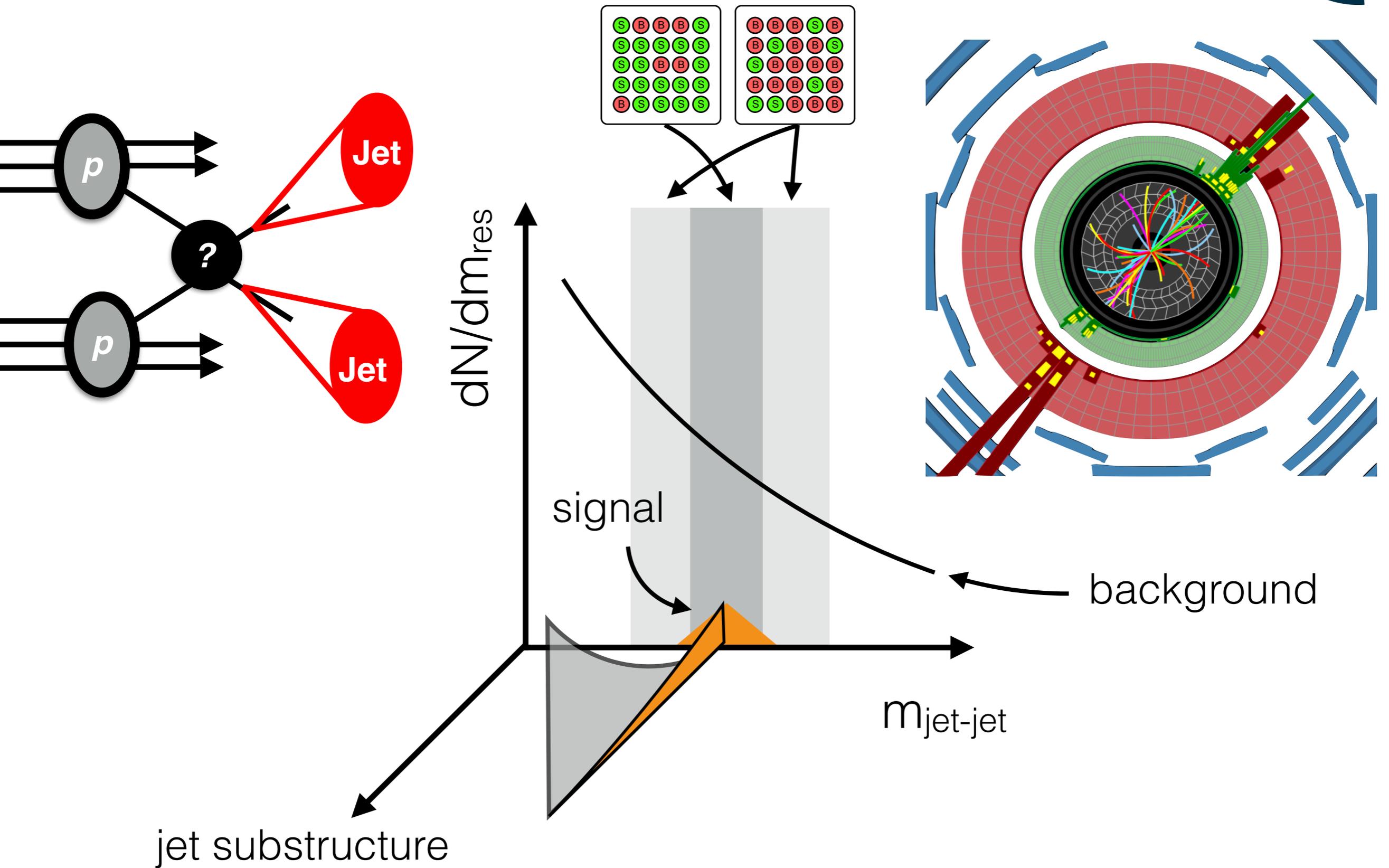
Resonant Anomalies

J. Collins, K. Howe, **BN**,
PRL 121 (2018) 241803

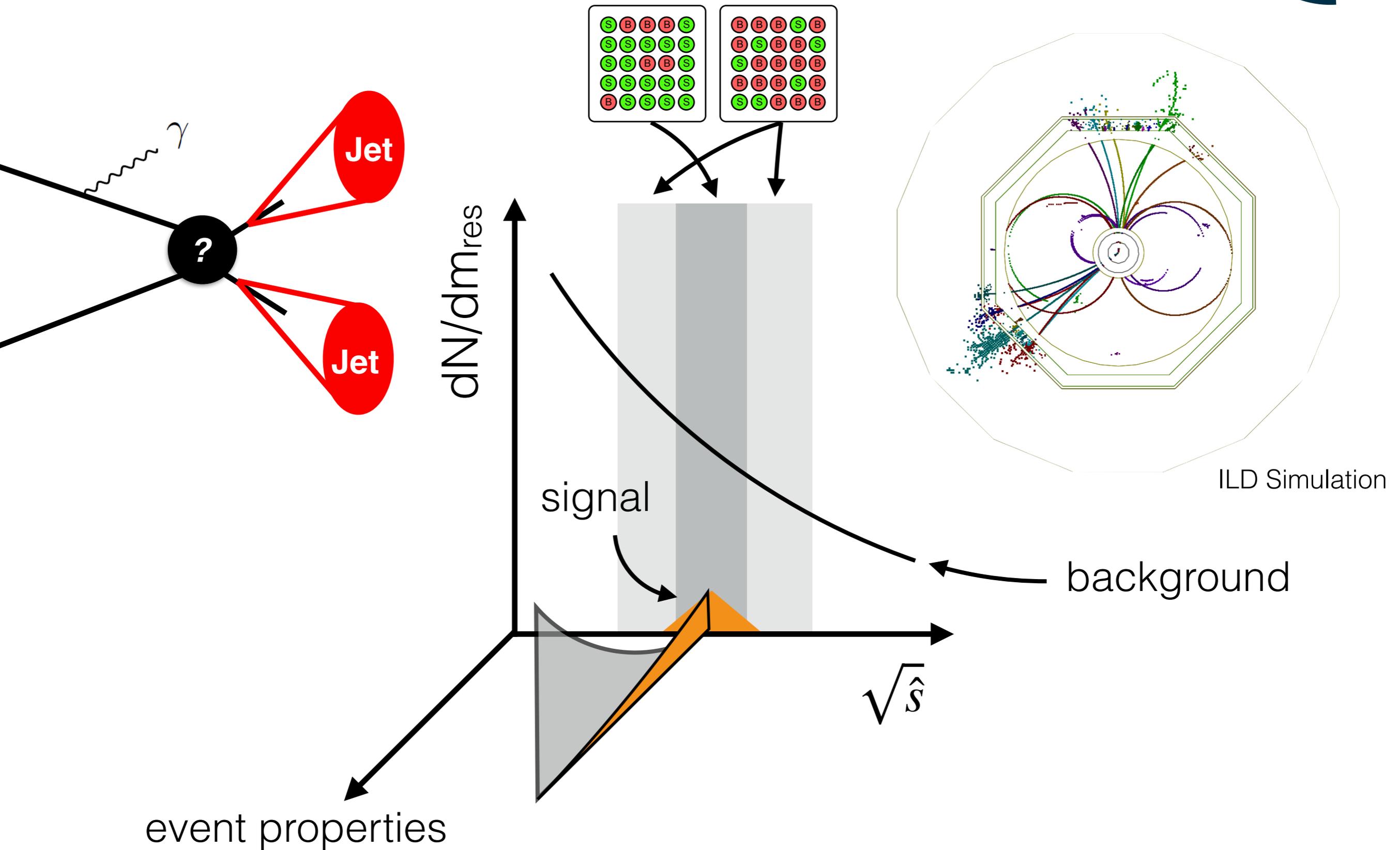
+many more



Resonant Anomalies

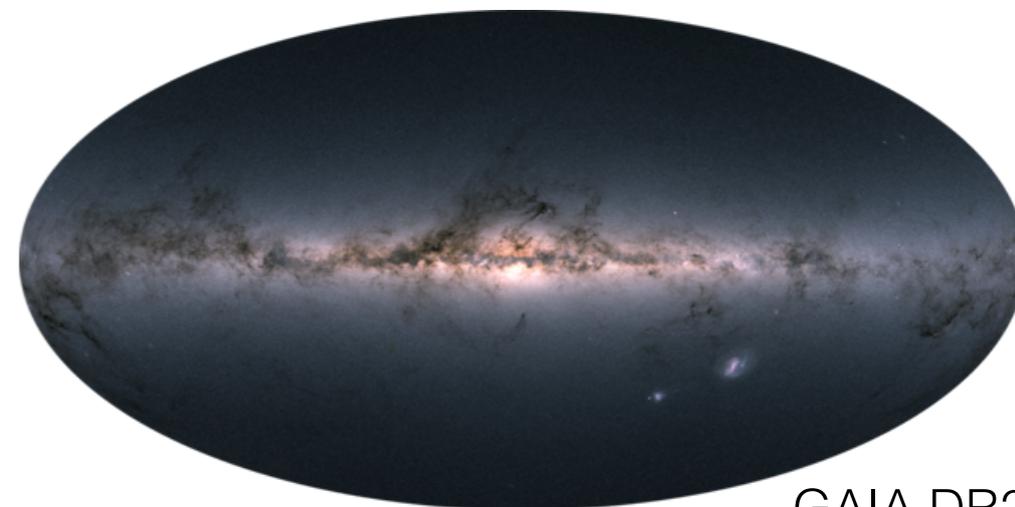
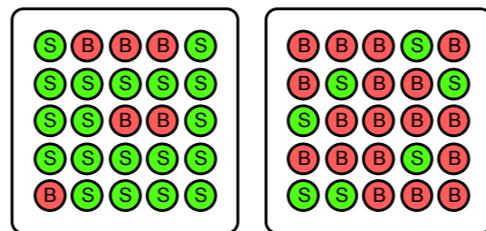
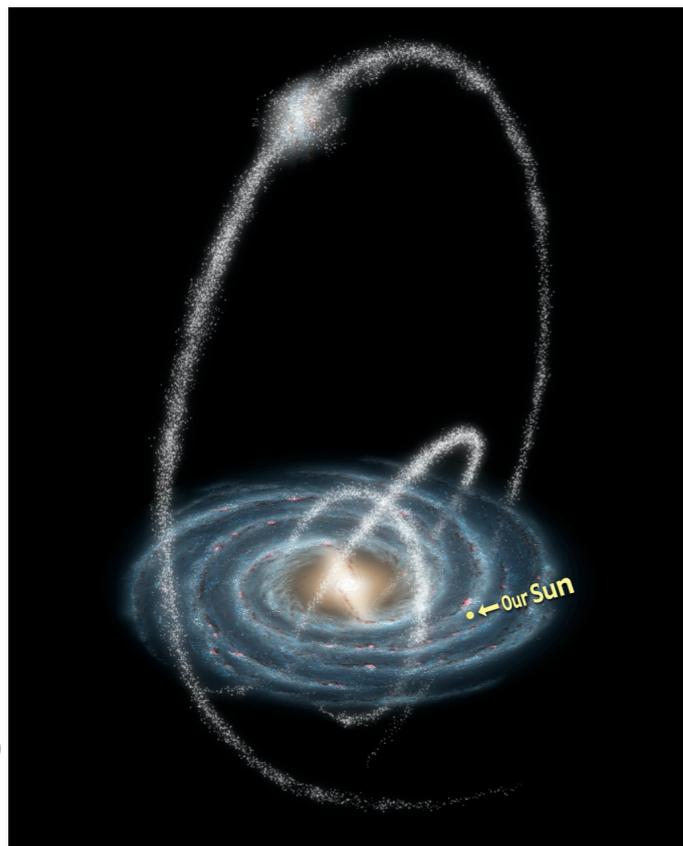


Resonant Anomalies

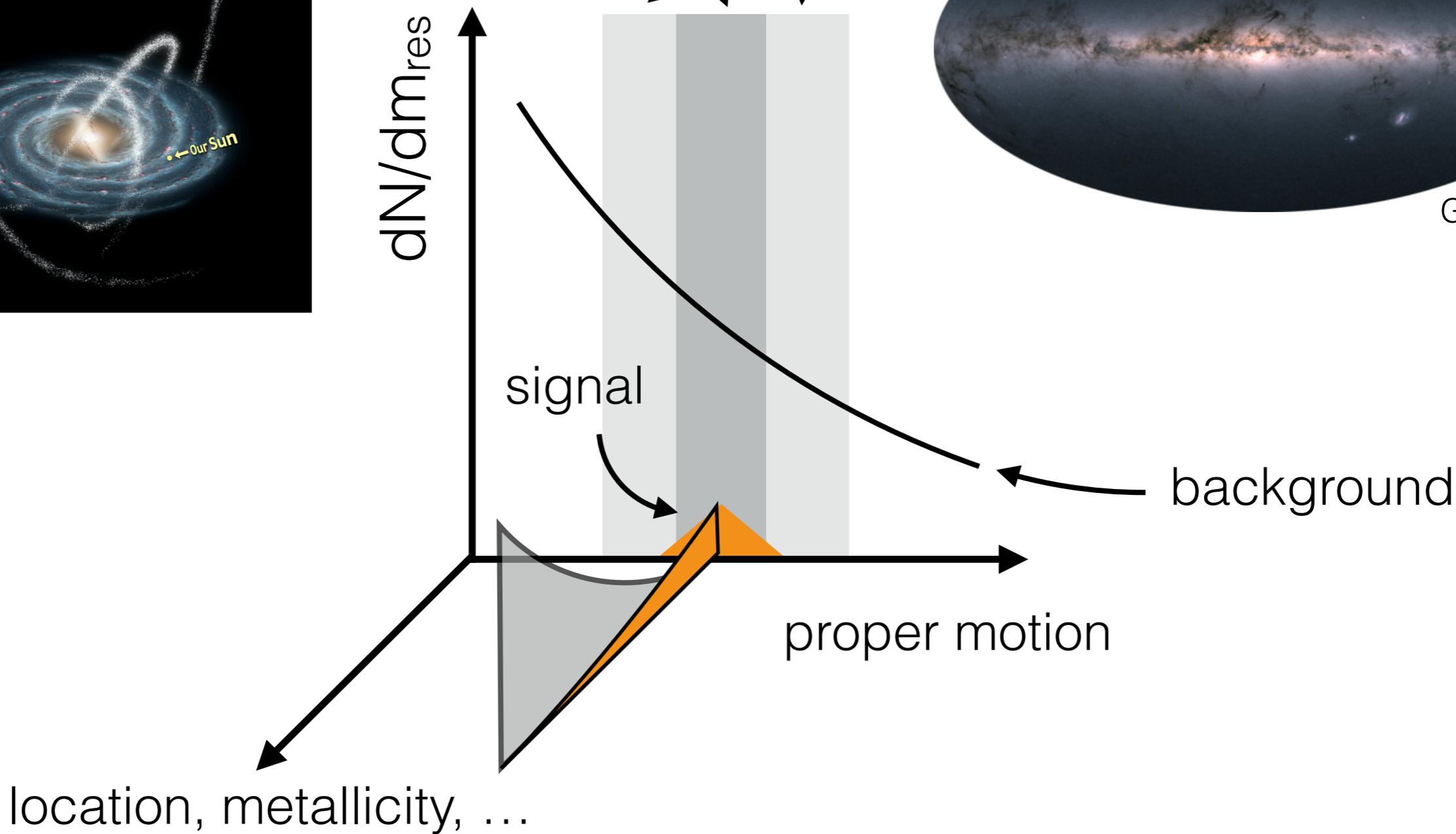


Resonant Anomalies

Image: NASA



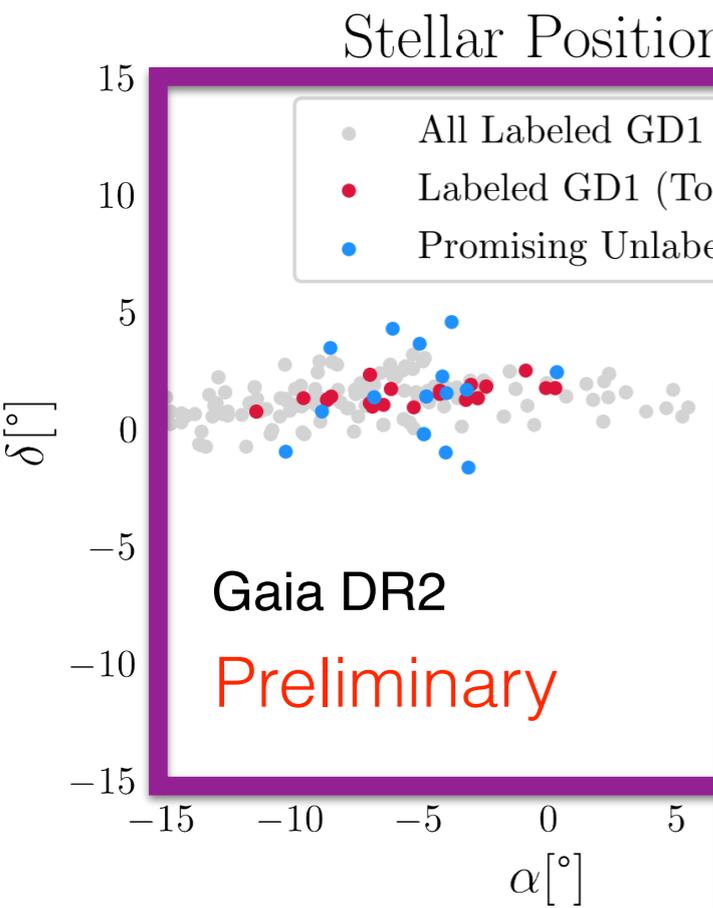
GAIA DR2



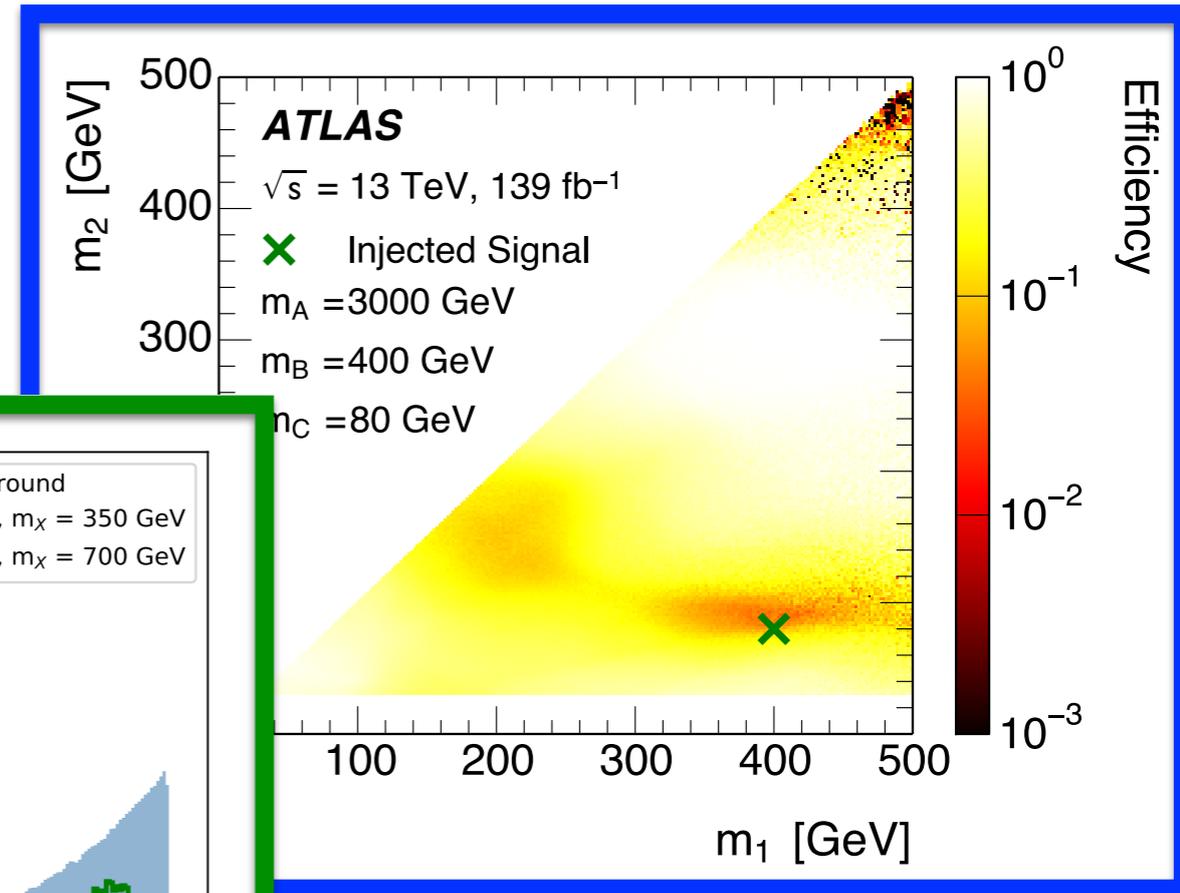
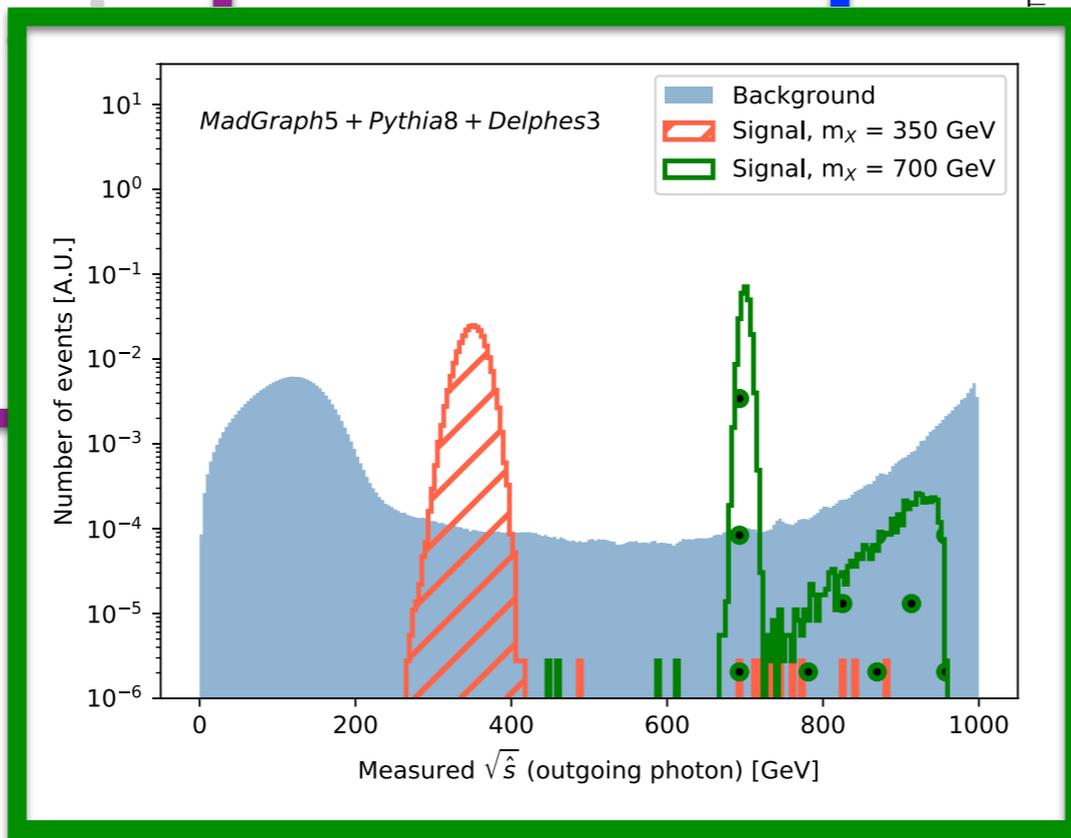
Anomaly Detection: Science



This program is really just getting started - there are many challenges to scale up (methods and computing*), but the early studies are exciting and cross-cutting



Future e^+e^-



LHC

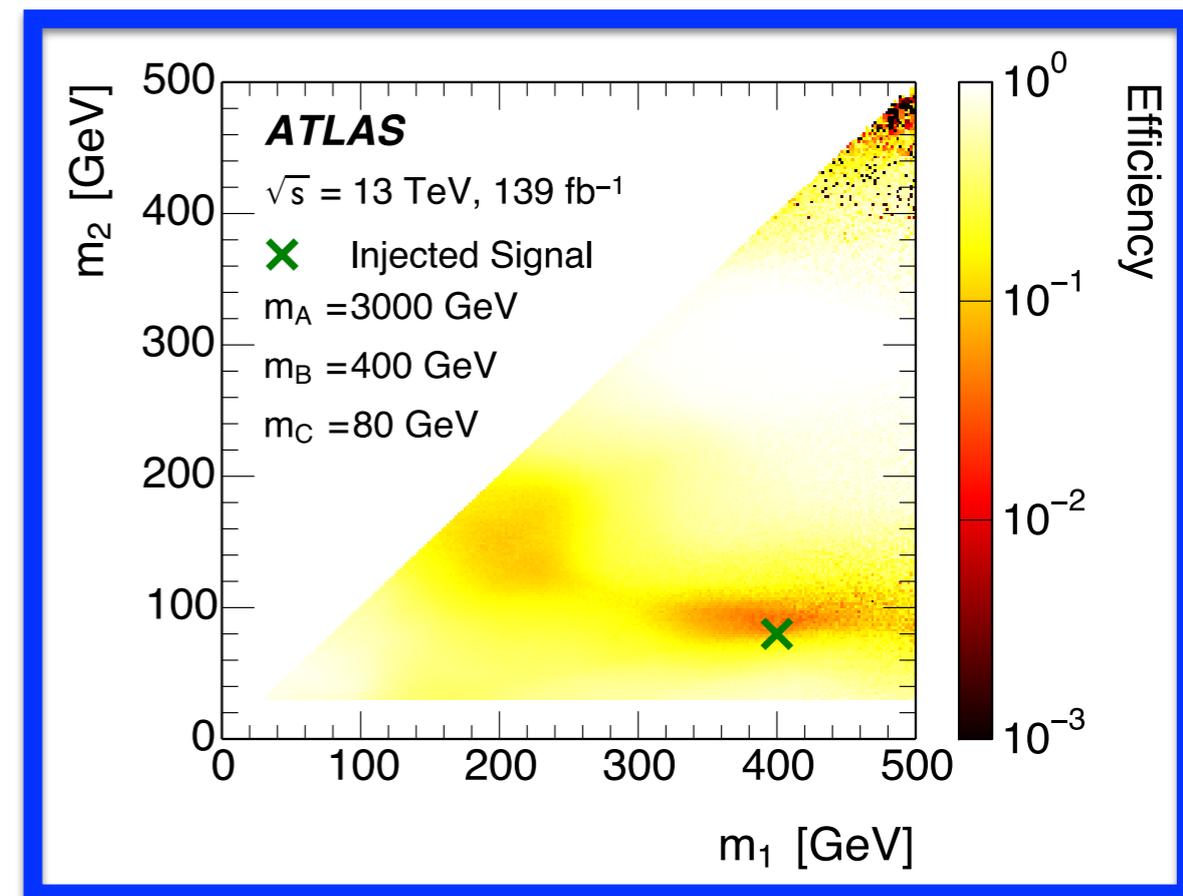
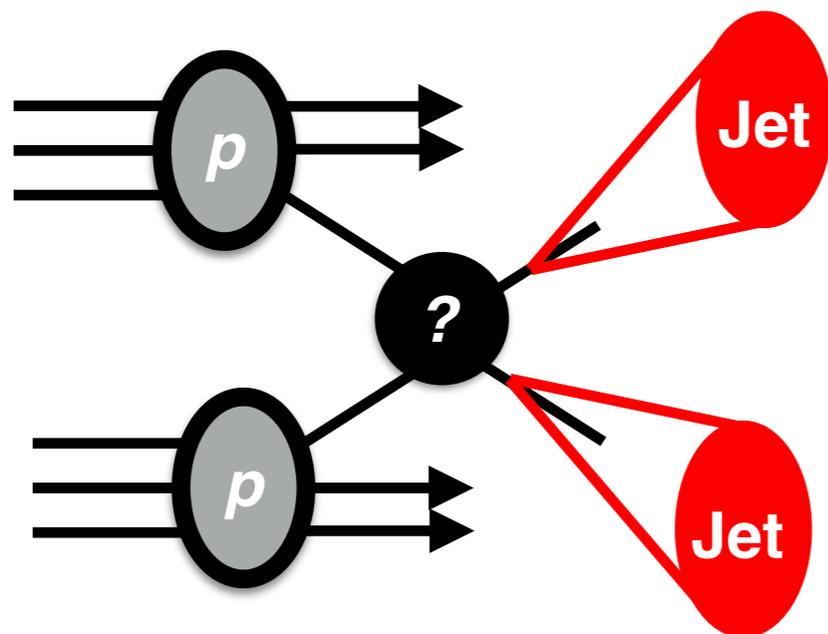
*LHC result shown above required training 20k NNs!

Anomaly Detection: Science

78

This program is really just getting started - there are many challenges to scale up (methods and computing*), but the early studies are exciting and cross-cutting

No new physics (yet),
but significantly
extended sensitivity



LHC

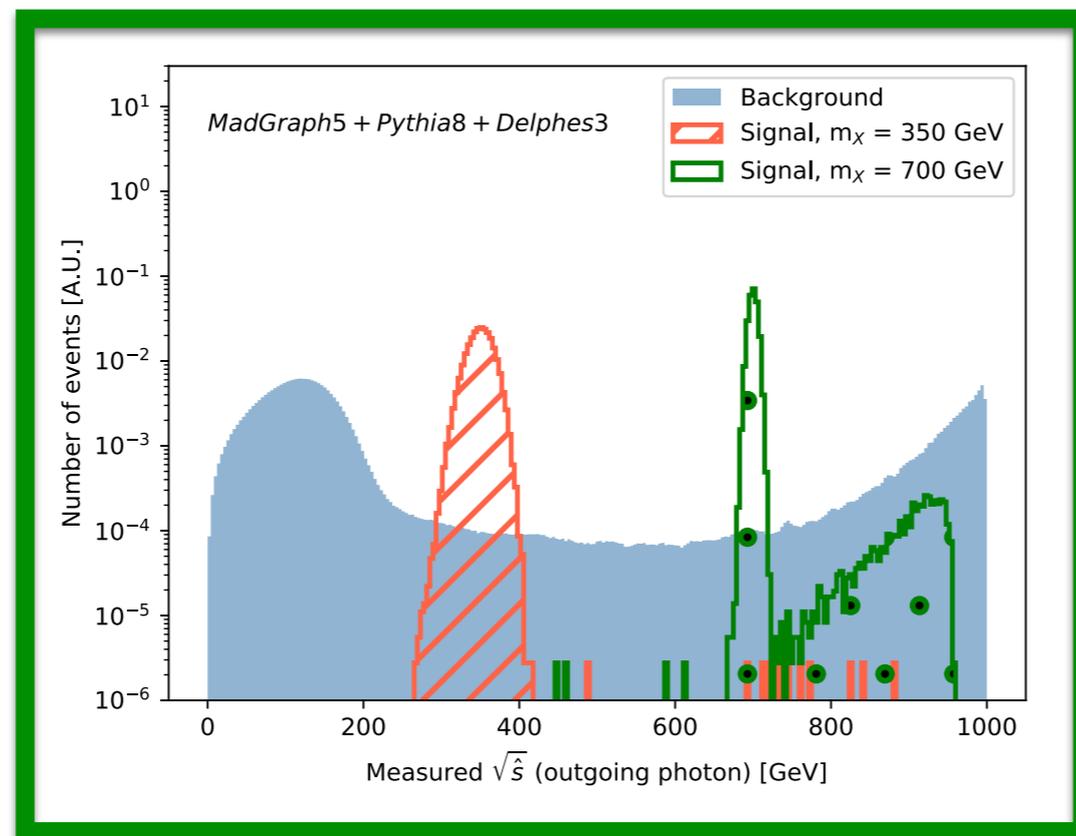
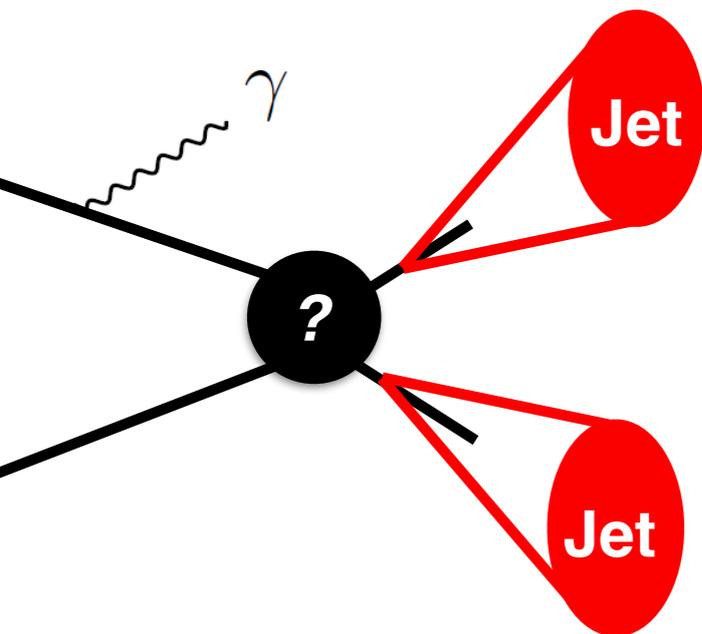
Anomaly Detection: Science

79

This program is really just getting started - there are many challenges to scale up (methods and computing*), but the early studies are exciting and cross-cutting

J. Gonski, J. Lai, **BN**, I Ochoa, JHEP (2022)

Future e^+e^-

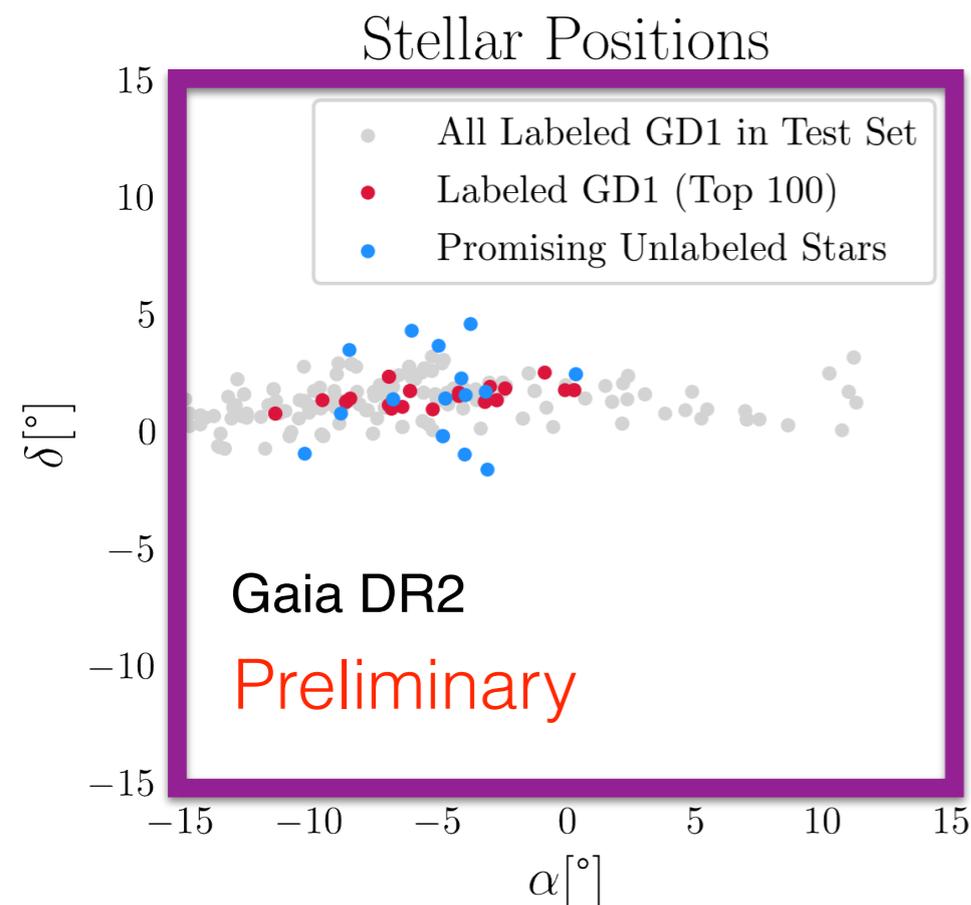


May have important implications for the design of future colliders

Anomaly Detection: Science



This program is really just getting started - there are many challenges to scale up (methods and computing*), but the early studies are exciting and cross-cutting



We have shown that we can find known streams

Will we be able to find new streams? Can weakly supervised learning help us categorize known streams?

Cold, stellar streams

Goal: develop, deploy, and interpret anomaly detection

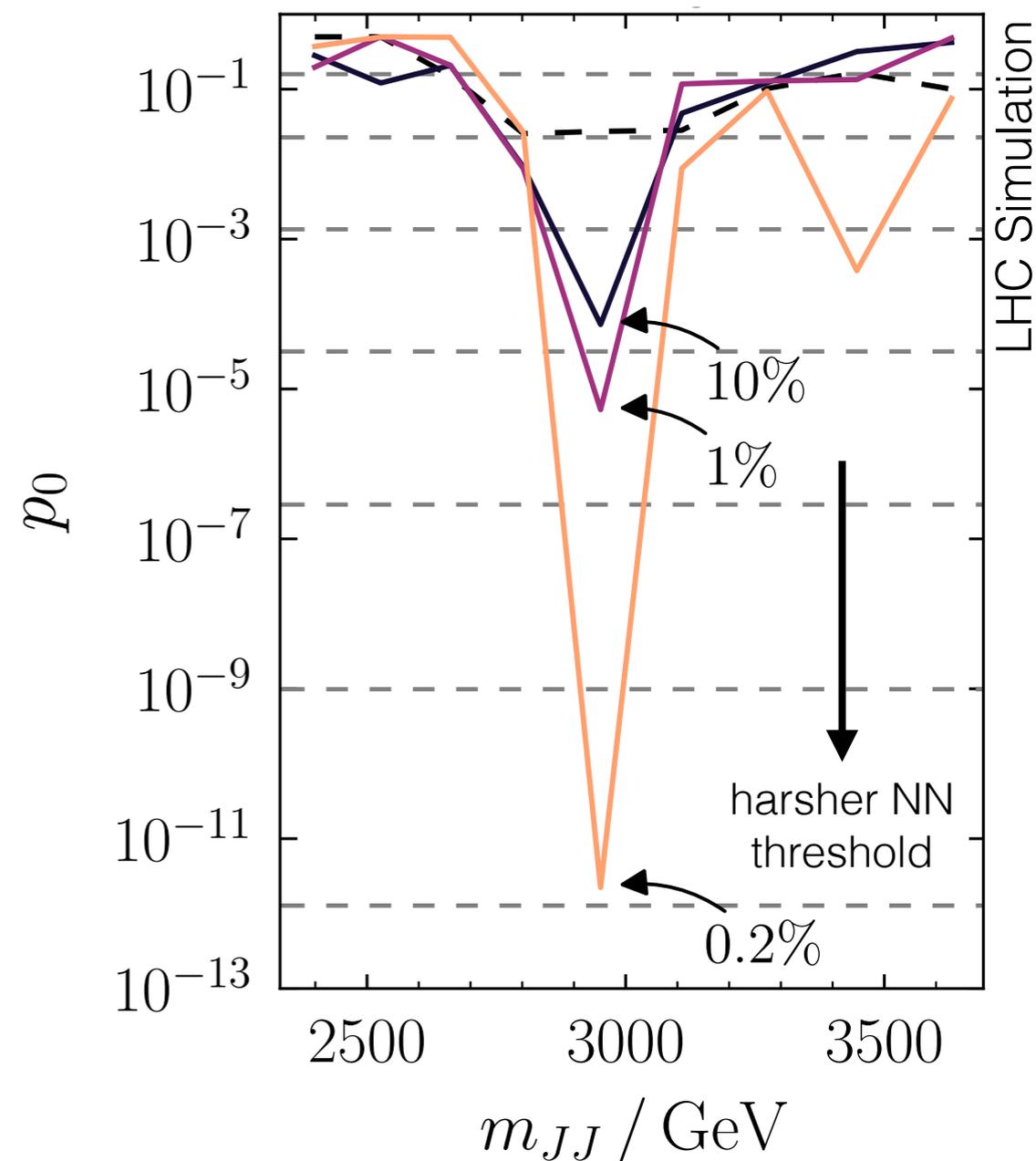
J. Collins, K. Howe, **BN**,
PRL 121 (2018) 241803

Methods

Push the dimensionality, relax the assumptions (non-resonant, ...)

Science

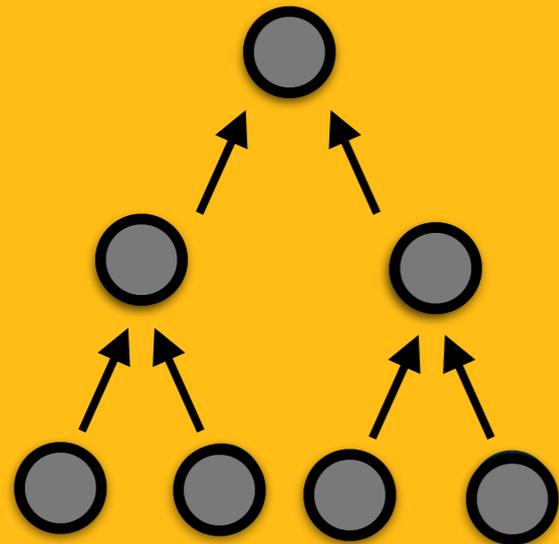
- Anomalies @ colliders
- Anomalies @ astroparticle/cosmology
- Anomalies @ dark matter direct det.



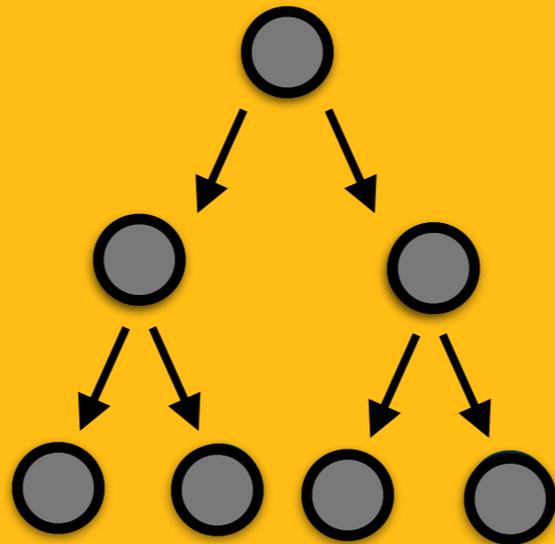
Outline for today

82

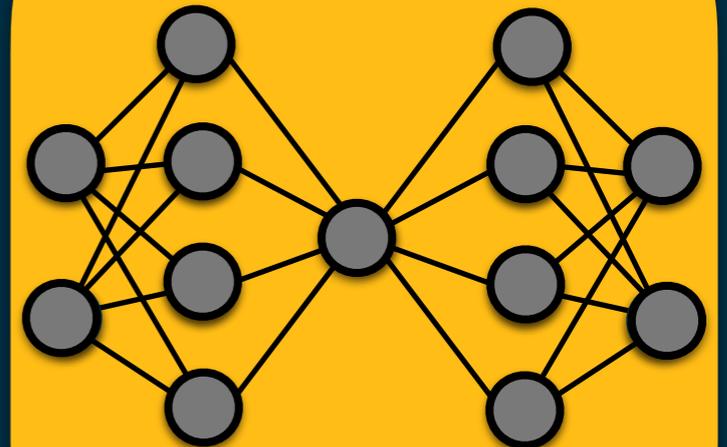
I'll focus on three core, cross-cutting areas of $ML \cap Physics$



Forward Models
(fast simulation)



Inverse Models
(unfolding)



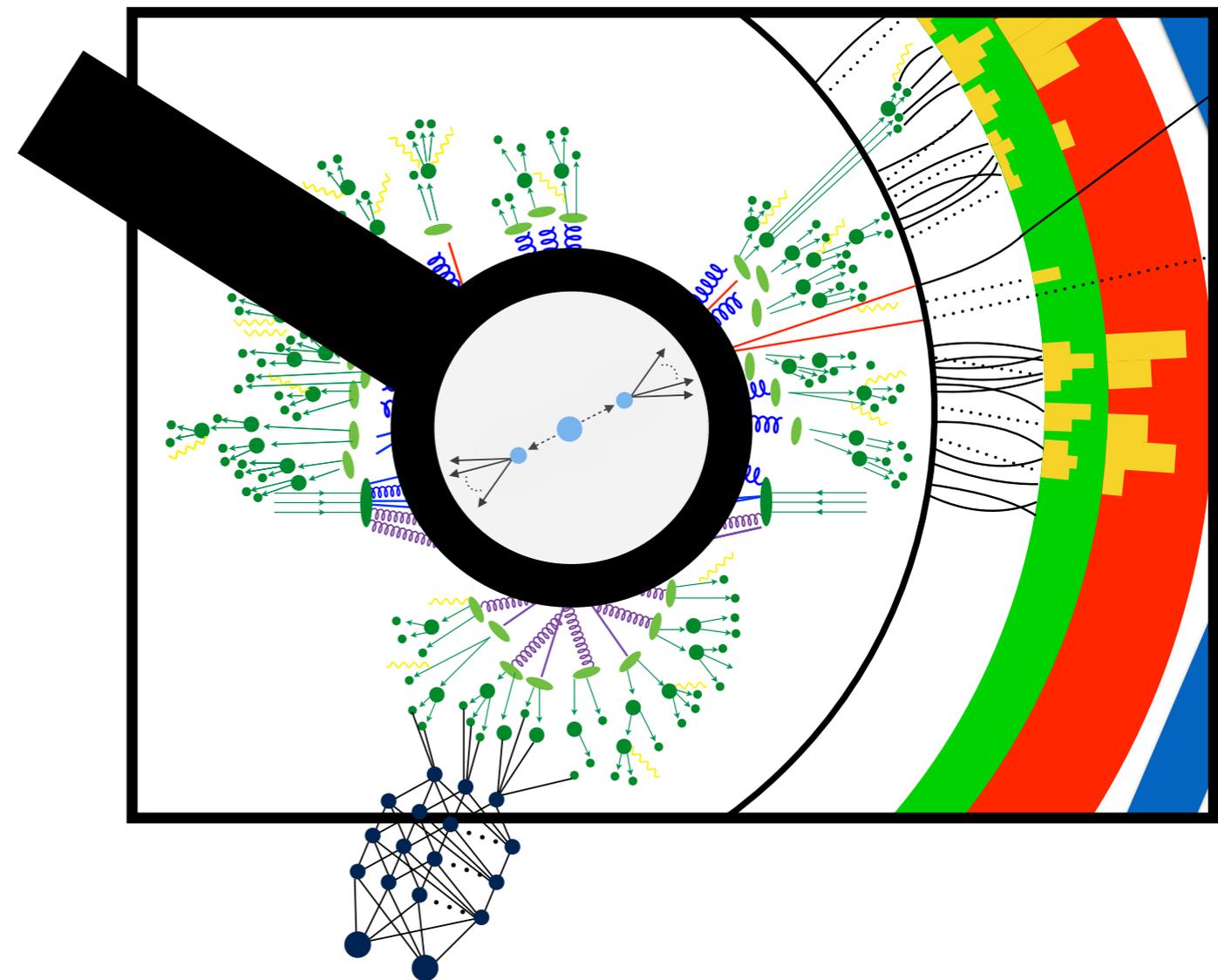
Simulation-free
(anomaly detection)

To illustrate these exciting topics, I'll give one vignette per area

We need innovative computational techniques to make the **data-driven discoveries of the future.**

This is not just about improving precision, it is about enabling new science!

We need physicists
(theory + experiment) to address unique challenges



Questions?

Krish Desai
Yale BS/MS 2020

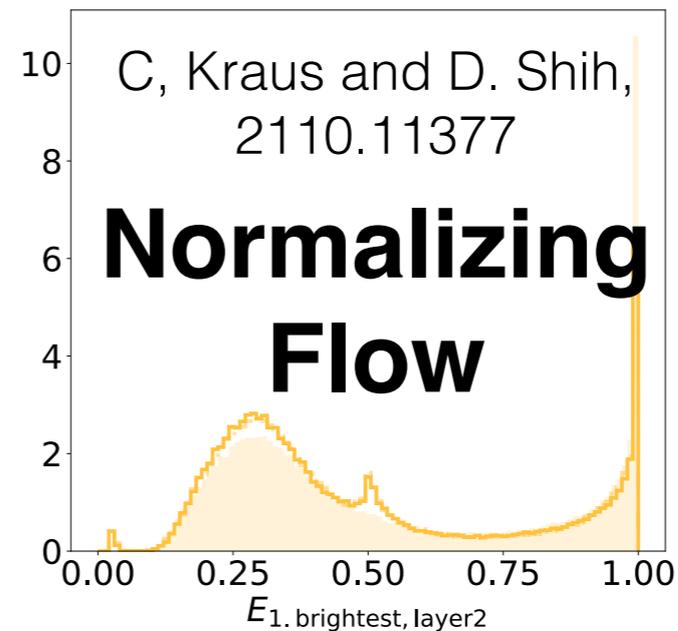
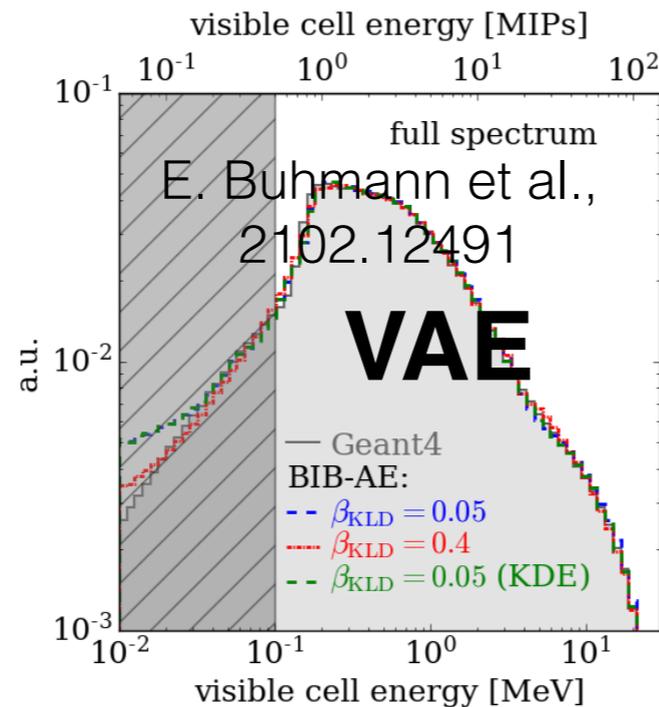
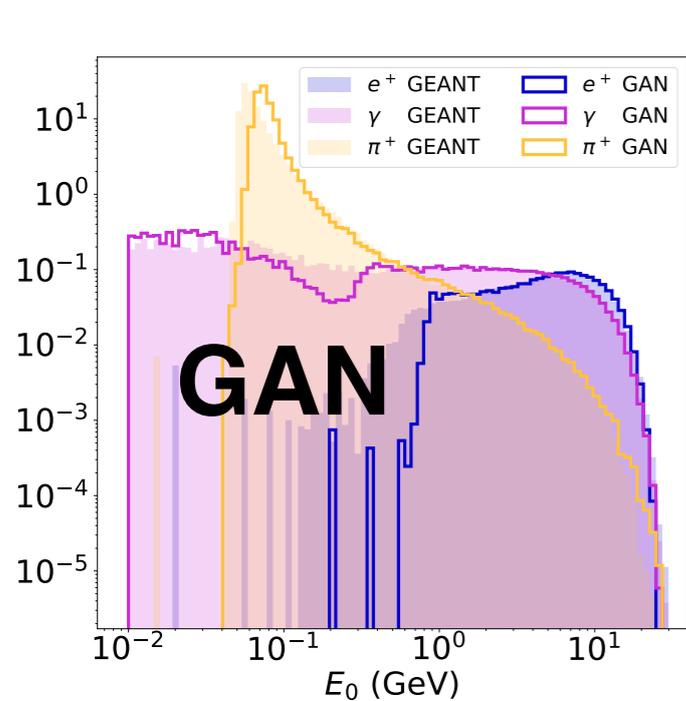


Marisel Pettee
Yale PhD 2021

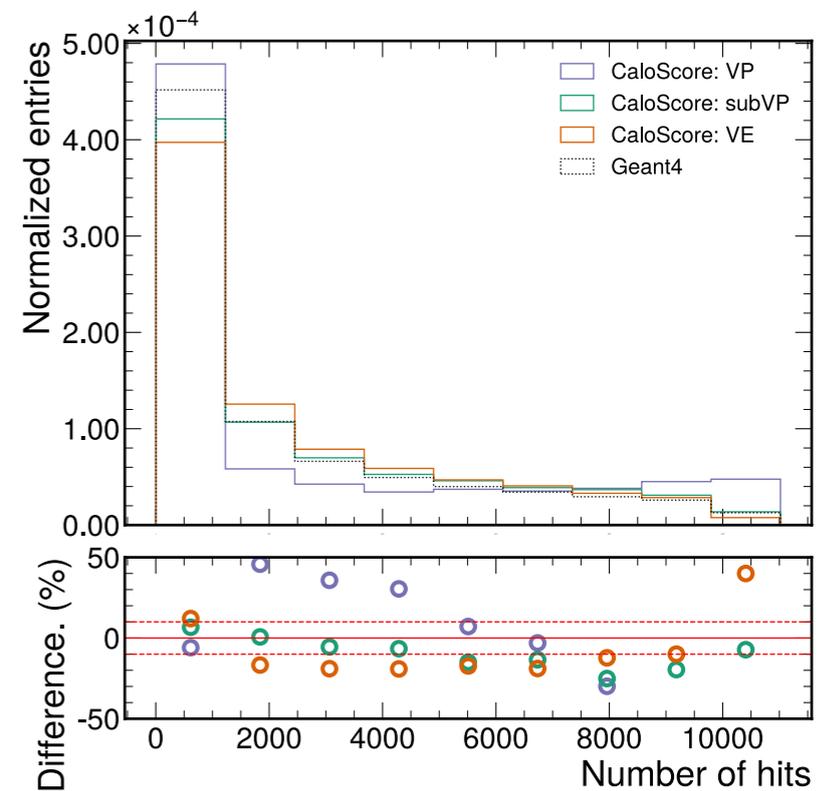
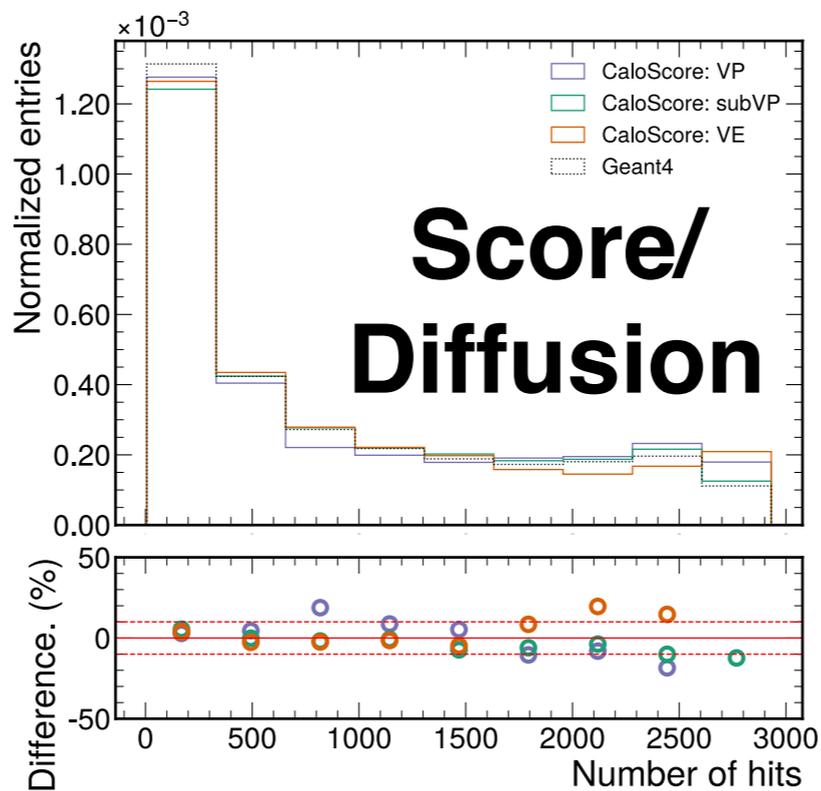
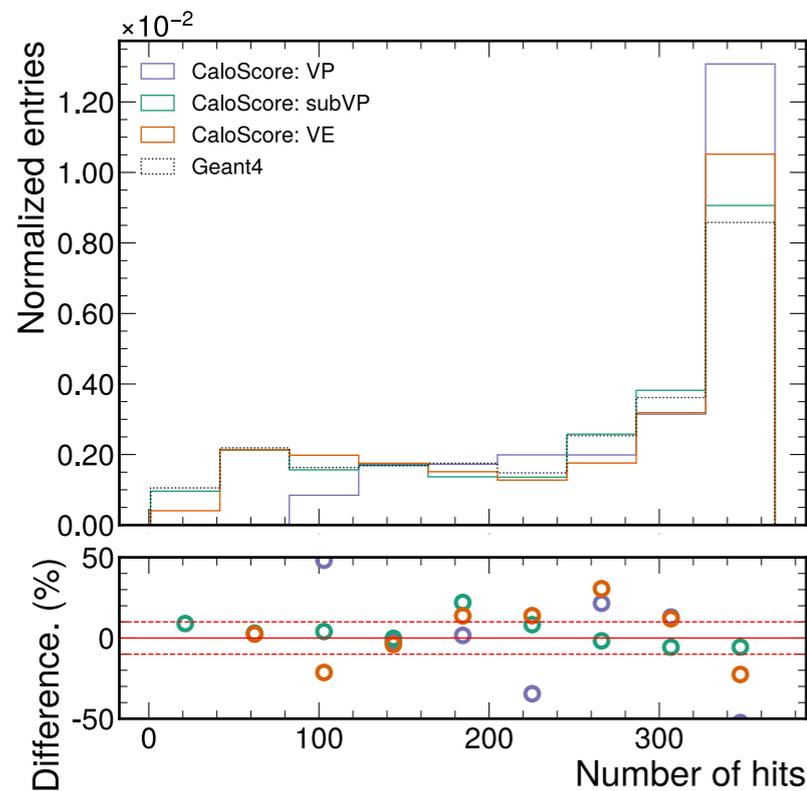
Backup



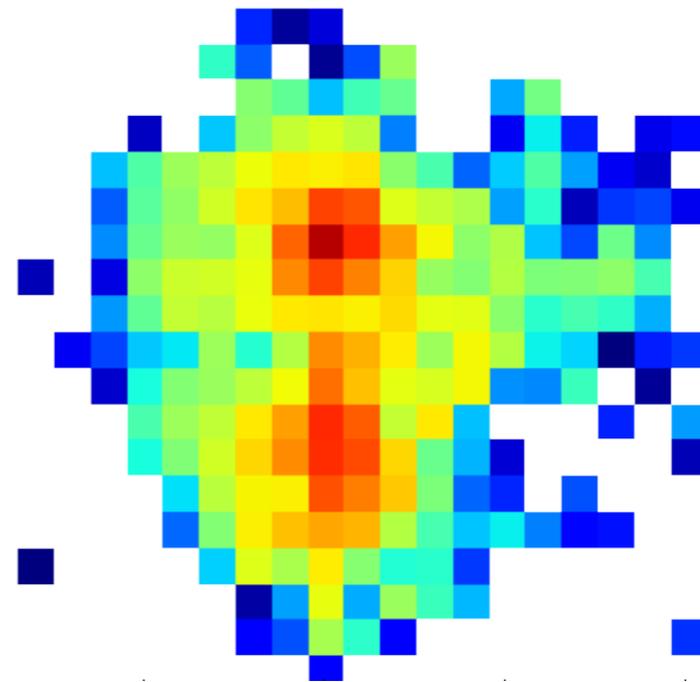
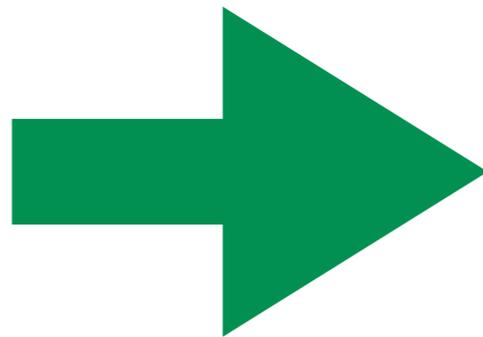
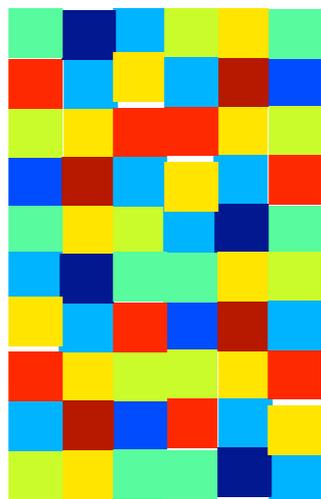
Calo(GAN, VAE, Flow, Score)



Multiple innovations beyond GANs



A **generator** is nothing other than a function that maps random numbers to structure.



Deep generative models: the map is a deep neural network.

GANs

*Generative
Adversarial Networks*

**Score-
based**

NFs

Normalizing Flows

VAEs

Variational Autoencoders

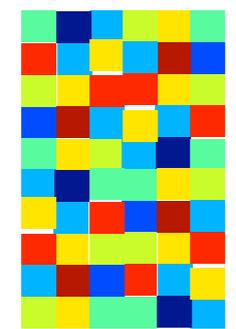
Deep generative models: the map is a deep neural network.

Introduction: GANs

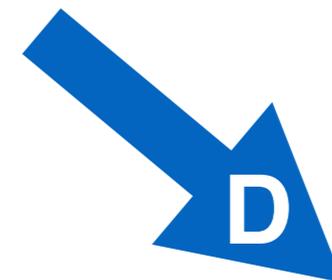
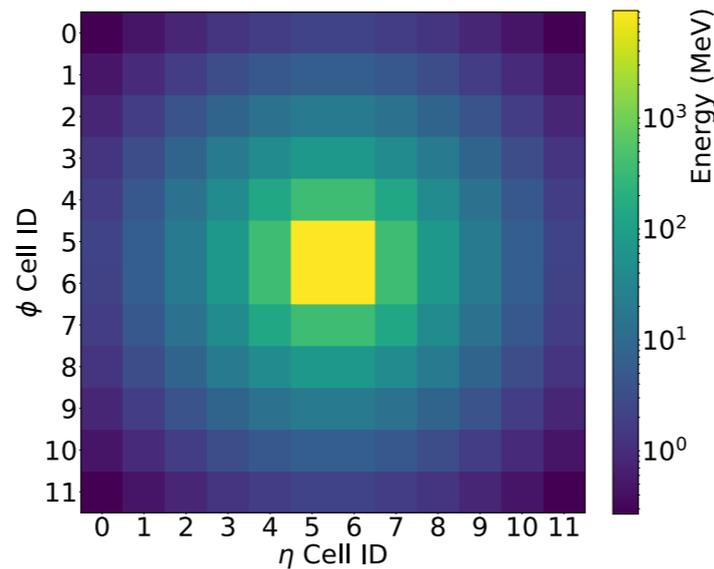
89

Generative Adversarial Networks (GANs):

*A two-network game where one **maps noise to structure** and one **classifies images as fake or real**.*

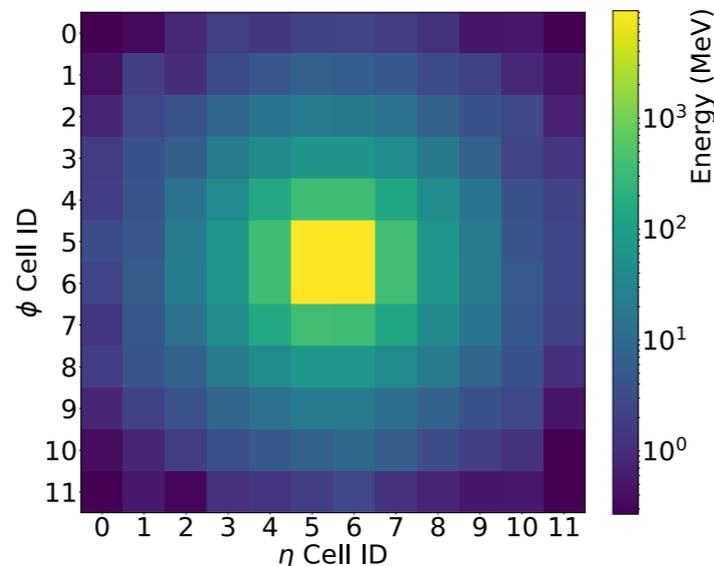


noise



{real, fake}

When **D** is maximally confused, **G** will be a good generator



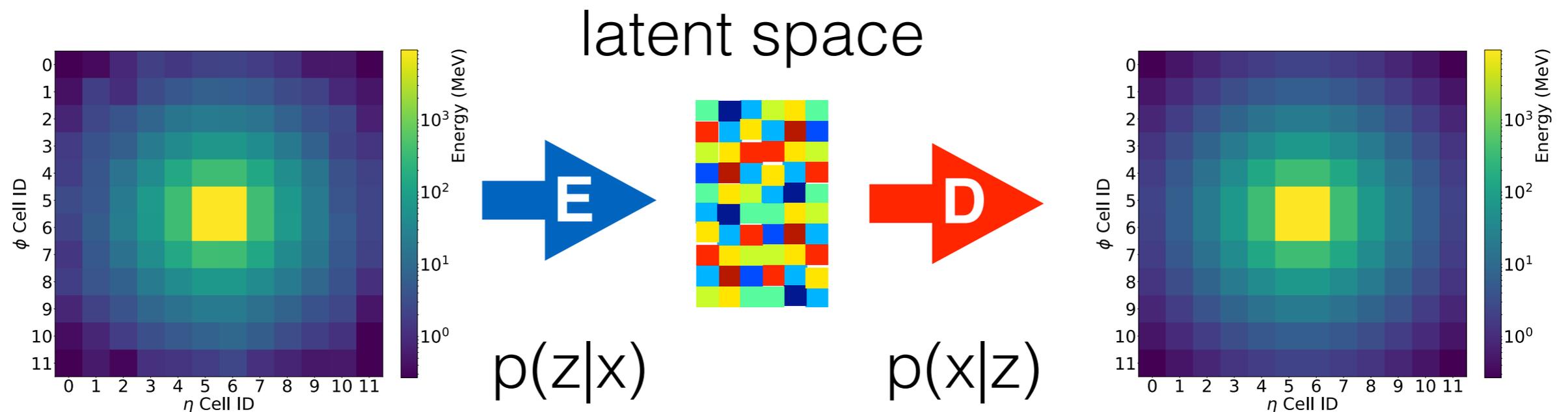
Physics-based simulator or data

Introduction: VAEs

90

Variational Autoencoders (VAEs):

A pair of networks that embed the data into a latent space with a given prior and decode back to the data space.



Physics-based
simulator or data

Probabilistic
encoder

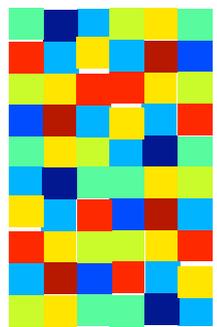
Probabilistic
decoder

Introduction: NFs

91

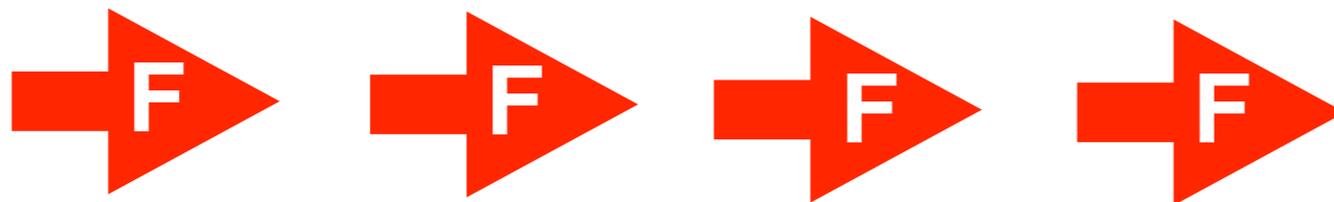
Normalizing Flows (NFs):

A series of invertible transformations mapping a known density into the data density.



latent space

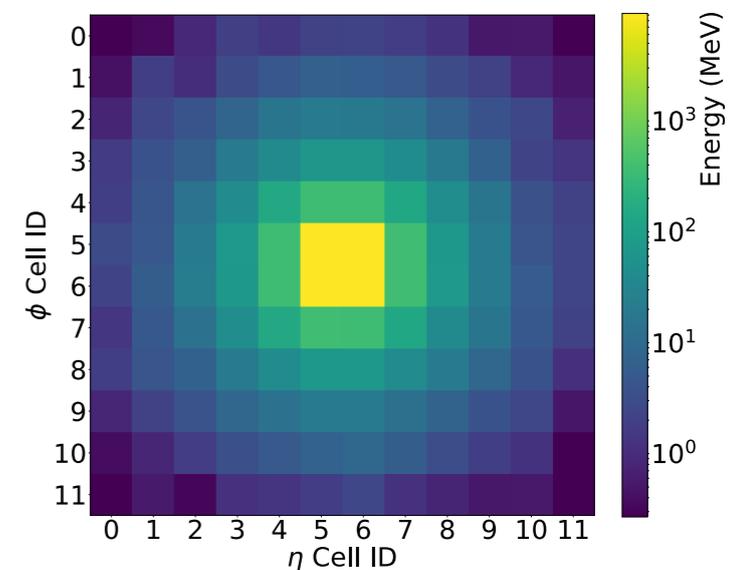
$p(z)$



*Invertible transformations with tractable **Jacobians***

$$p(x) = p(z) \left| \frac{dF^{-1}}{dx} \right|$$

Optimize via maximum likelihood



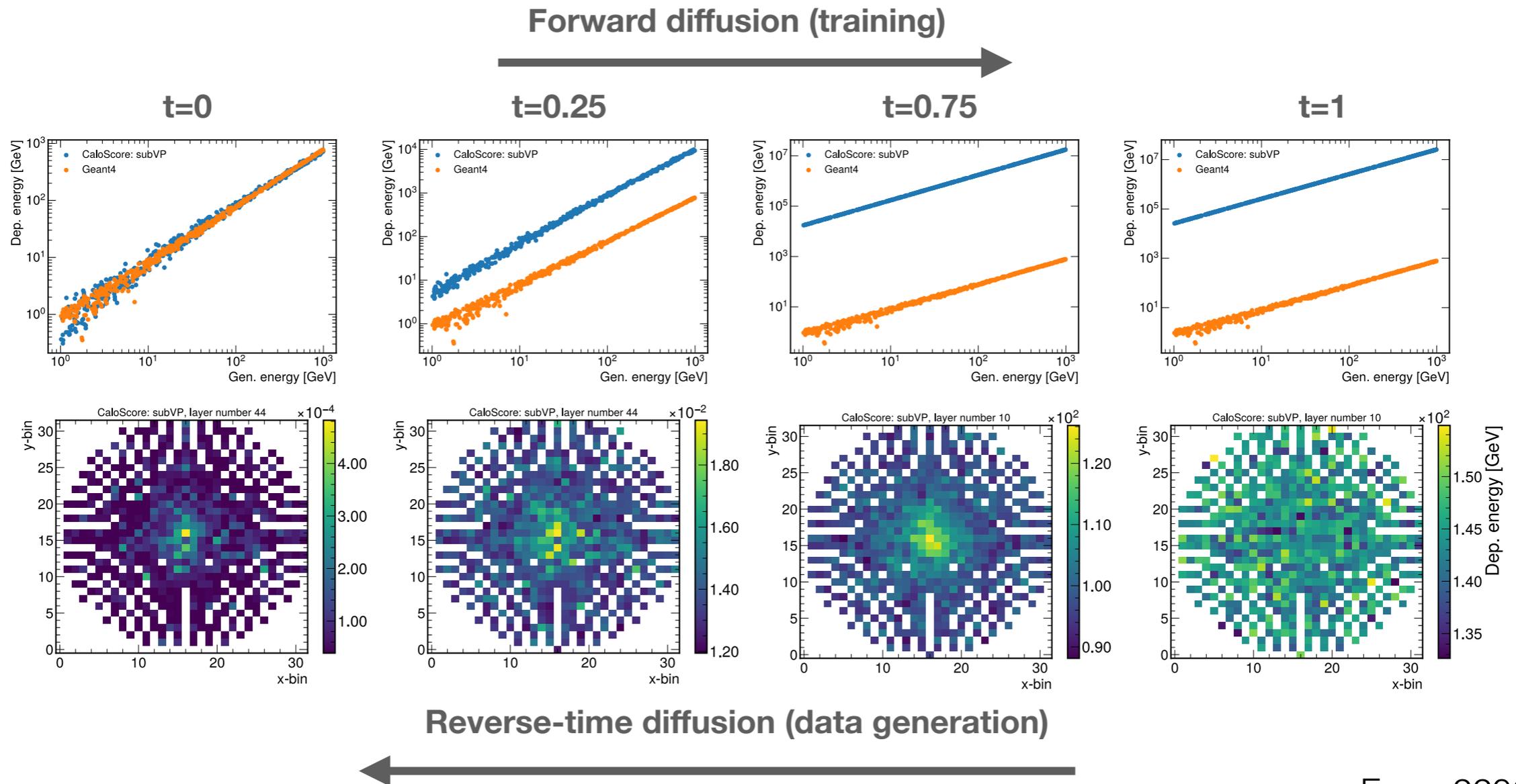
$p(x)$

Introduction: Score-based

92

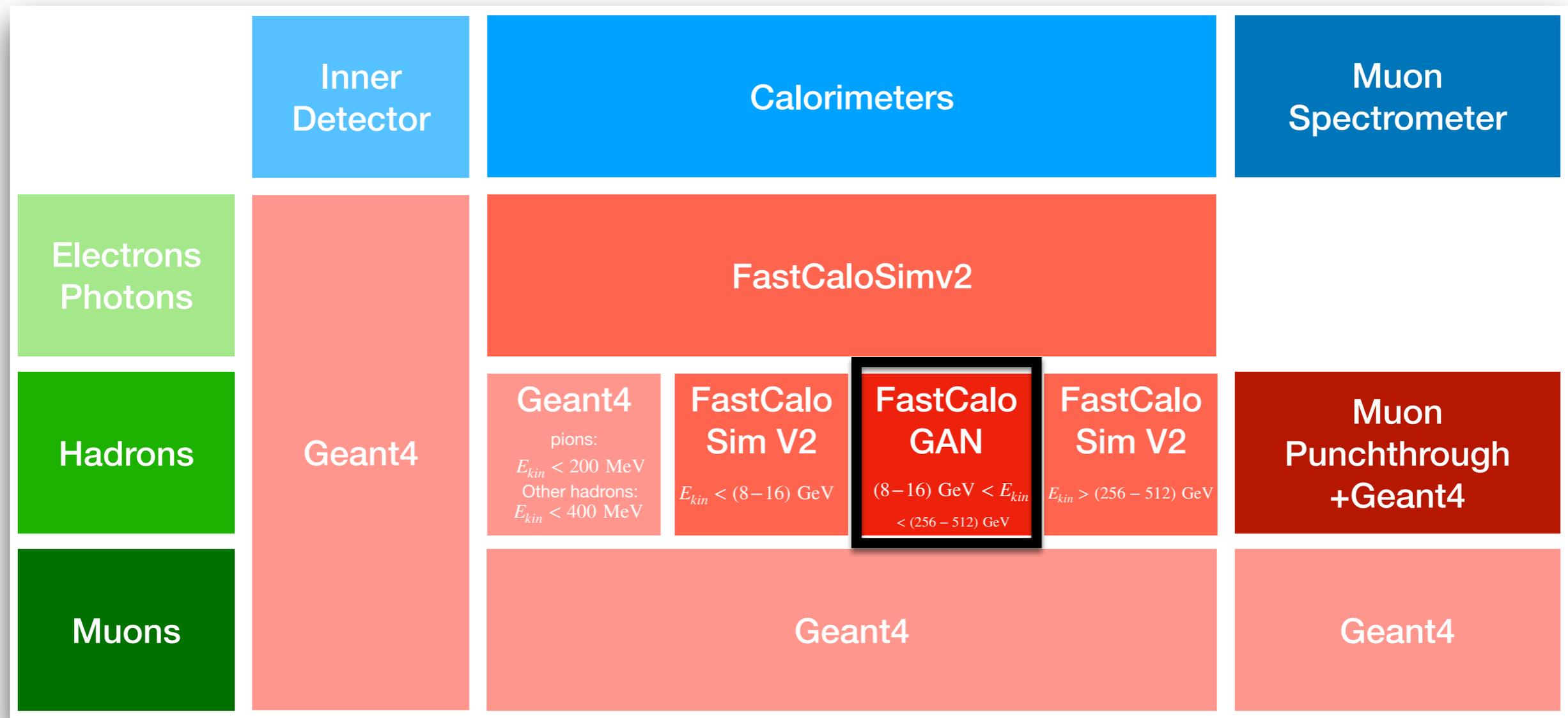
Score-based

Learn the gradient of the density instead of the probability density itself.





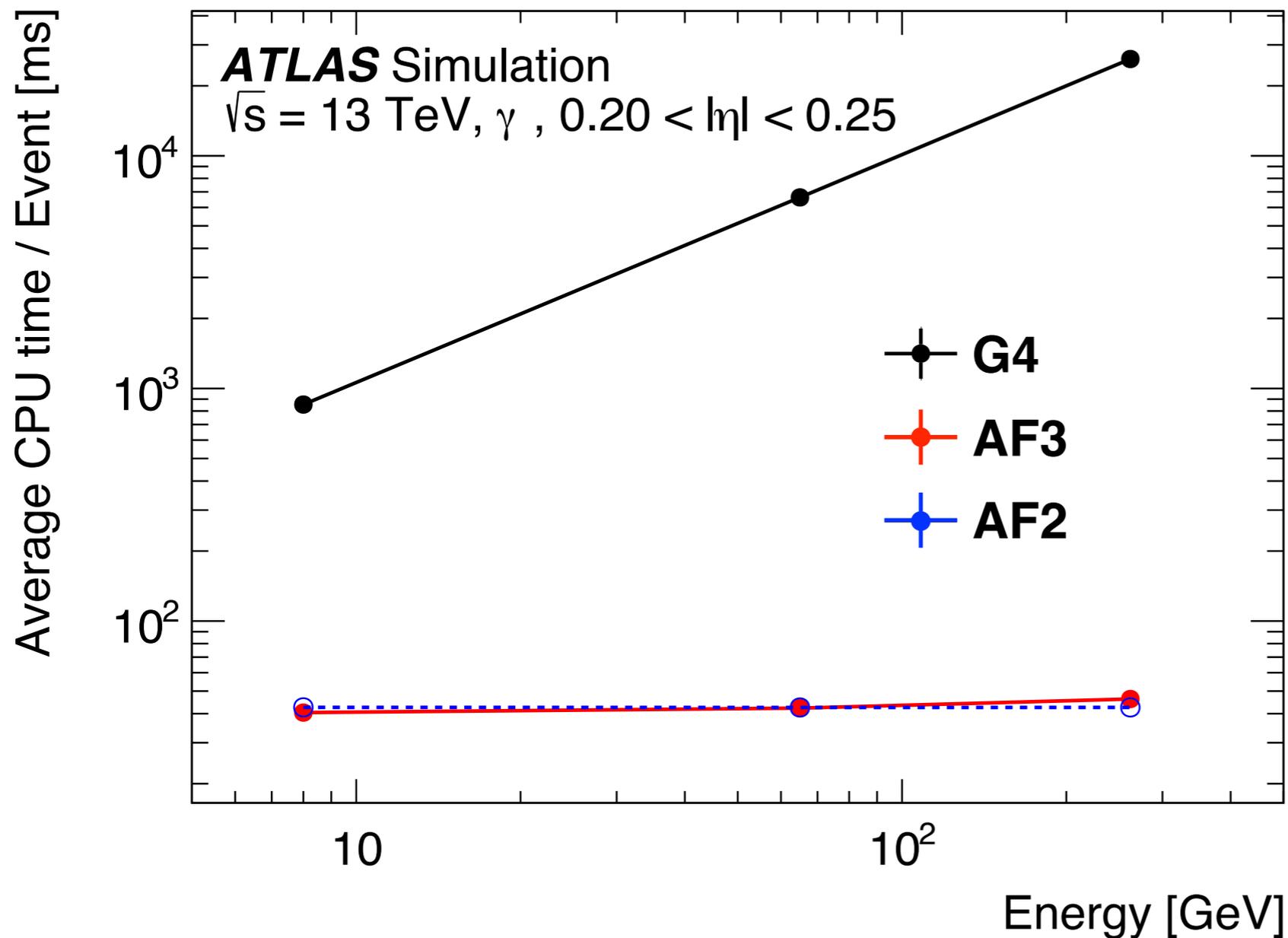
Integration into real detector sim.



The ATLAS Collaboration fast simulation (AF3) now includes a GAN at intermediate energies for pions



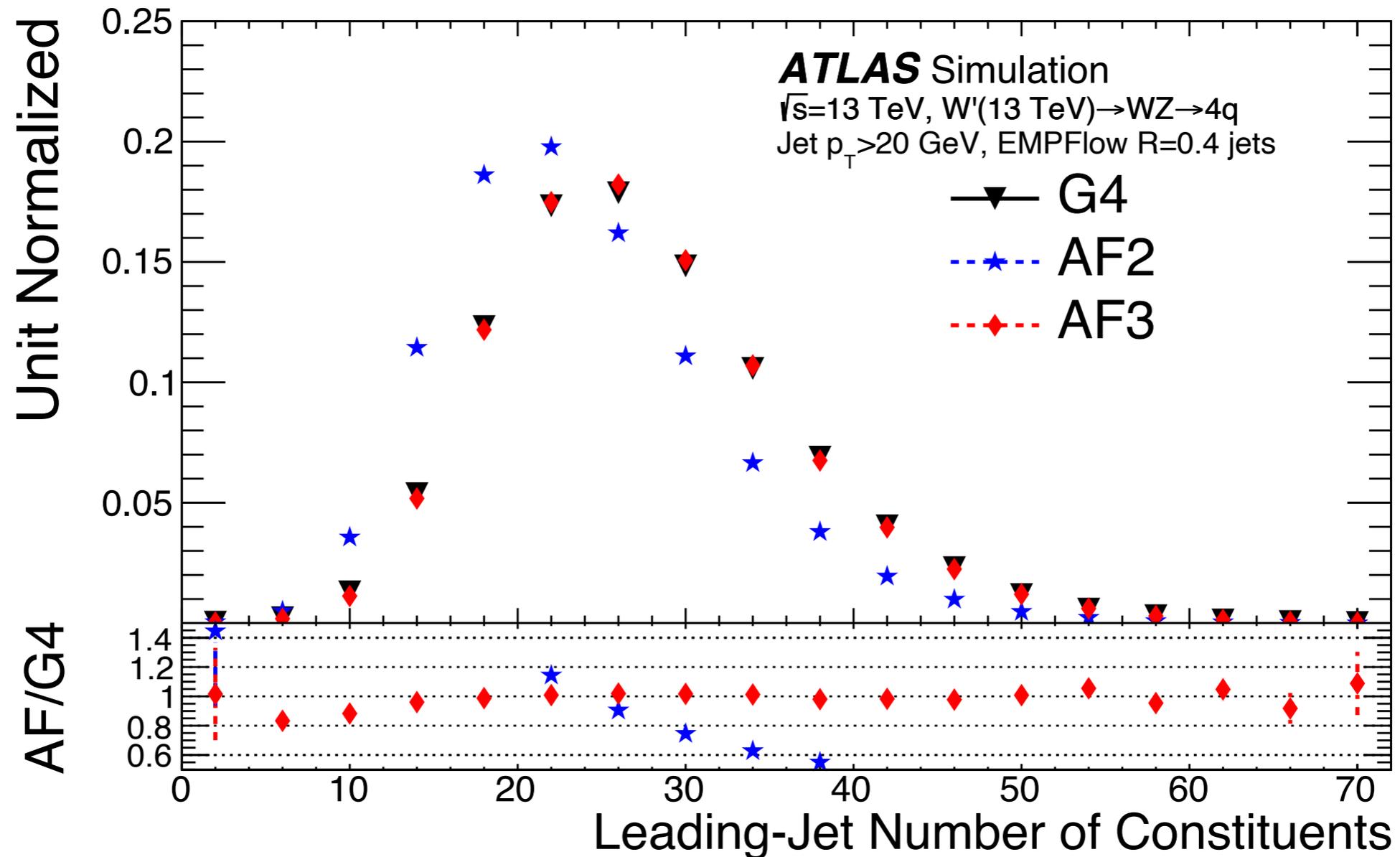
Integration into real detector sim.



As expected, the fast sim. timing is independent of energy, while Geant4 requires more time for higher energy.



Integration into real detector sim.



The new fast simulation (**AF3**) significantly improves jet substructure with respect to the older one (**AF2**).

$$X \sim \mathcal{N}(\mu, \sigma)$$

$$X \sim \mathcal{N}(\mu, \sigma)$$



```
x = np.random.normal(mu, sigma)
```

Removed
randomness from
simulator

$$X \sim \mathcal{N}(\mu, \sigma)$$



```
x = np.random.normal(mu, sigma)
```



```
Z = np.random.uniform(0, 1)
```

```
x = sigma*Phiinv(z)+mu
```

(`Phiinv` = inverse Gaussian CDF)

Removed
randomness from
simulator

$$X \sim \mathcal{N}(\mu, \sigma)$$



```
x = np.random.normal(mu, sigma)
```



```
z = np.random.uniform(0, 1)
```

```
x = sigma*Phiinv(z)+mu
```

(Phiinv = inverse Gaussian CDF)

Now, can compute
 $\partial/\partial\mu$ and $\partial/\partial\sigma$

Differentiable Simulation

100

Removed
randomness from
simulator

$$X \sim \mathcal{N}(\mu, \sigma)$$



```
x = np.random.normal(mu, sigma)
```



```
z = np.random.uniform(0, 1)
```

```
x = sigma*Phiinv(z)+mu
```

(Phiinv = inverse Gaussian CDF)

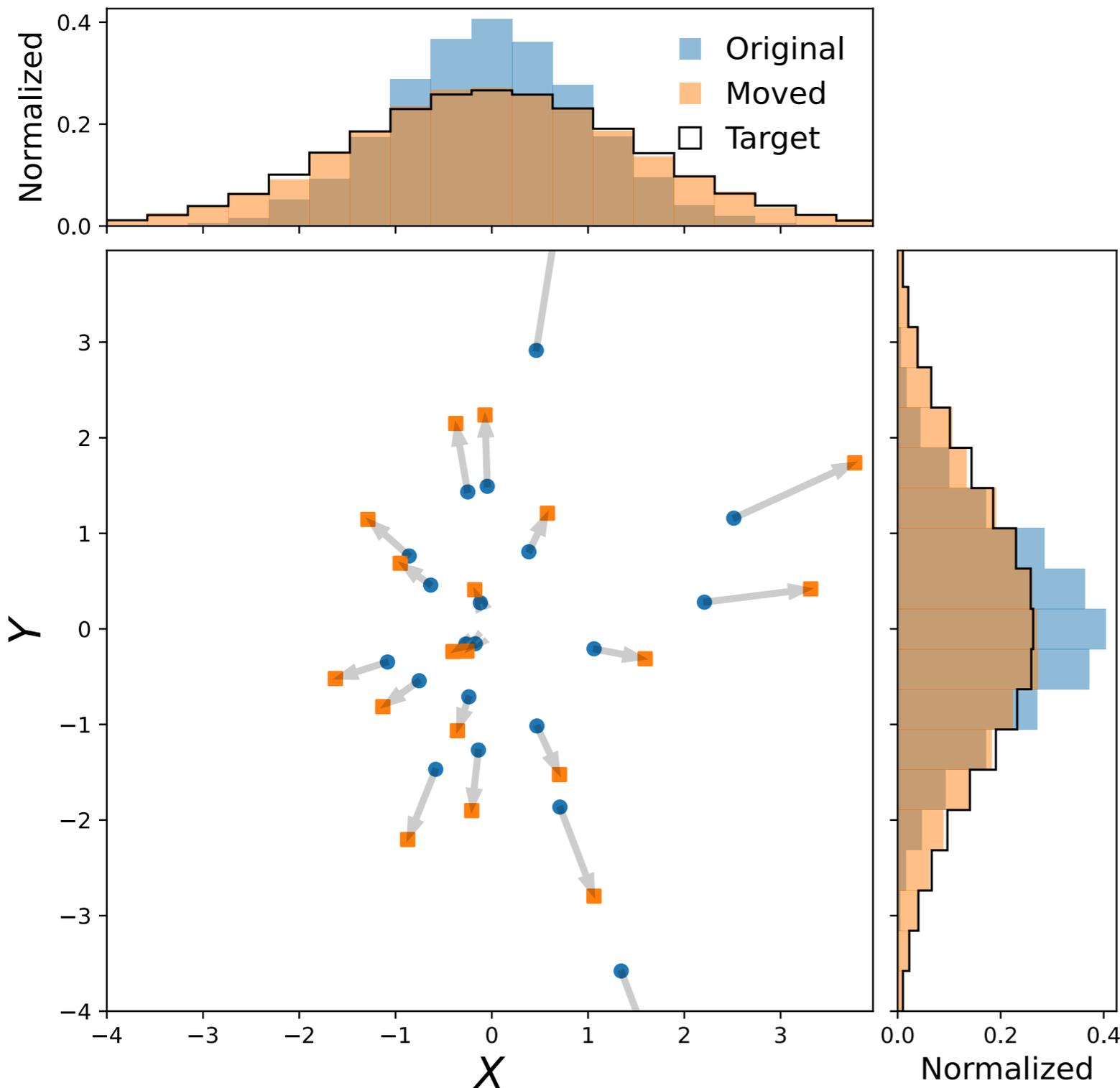
Now, can compute
 $\partial/\partial\mu$ and $\partial/\partial\sigma$

We can then do:

$$\text{sim}(\mu_0 + \epsilon) \approx \text{sim}(\mu_0) + \frac{\partial \text{sim}}{\partial \mu} \epsilon$$

Differentiable Simulation

101



$$X \sim \mathcal{N}(\mu, \sigma)$$



```
x = np.random.normal(mu, sigma)
```



```
z = np.random.uniform(0, 1)
```

```
x = sigma*Phiinv(z)+mu
```

(Phiinv = inverse Gaussian CDF)

Now, can compute
 $\partial/\partial\mu$ and $\partial/\partial\sigma$

We can then do:

$$\text{sim}(\mu_0 + \epsilon) \approx \text{sim}(\mu_0) + \frac{\partial \text{sim}}{\partial \mu} \epsilon$$

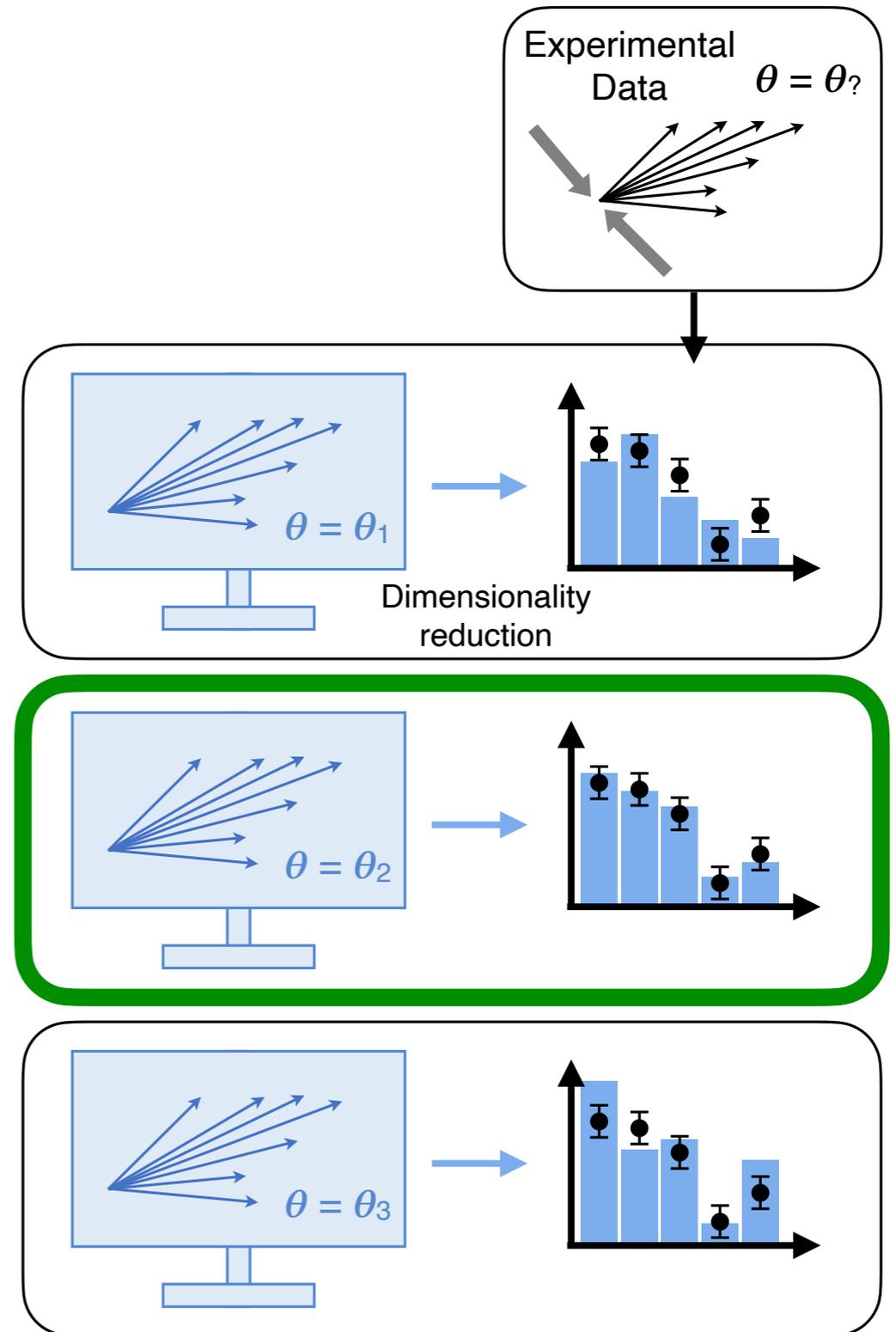
Why event moving?

102

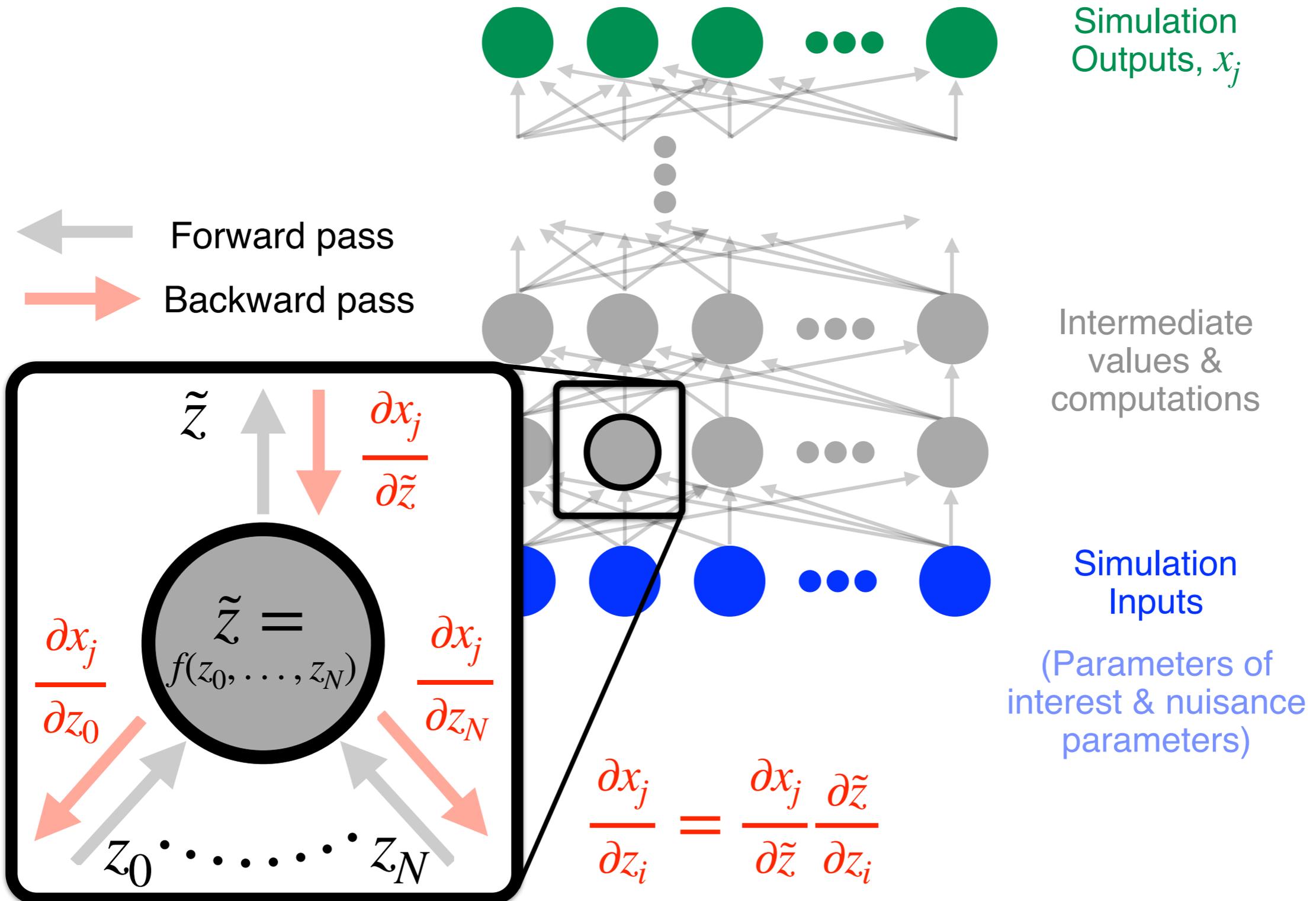
Often, we generate many simulations with different parameters (templates) and fit them to data.

We also often have to use histograms in order to interpolate.

With event moving, we can interpolate in many dimensions and eliminate MC stat. uncertainties!

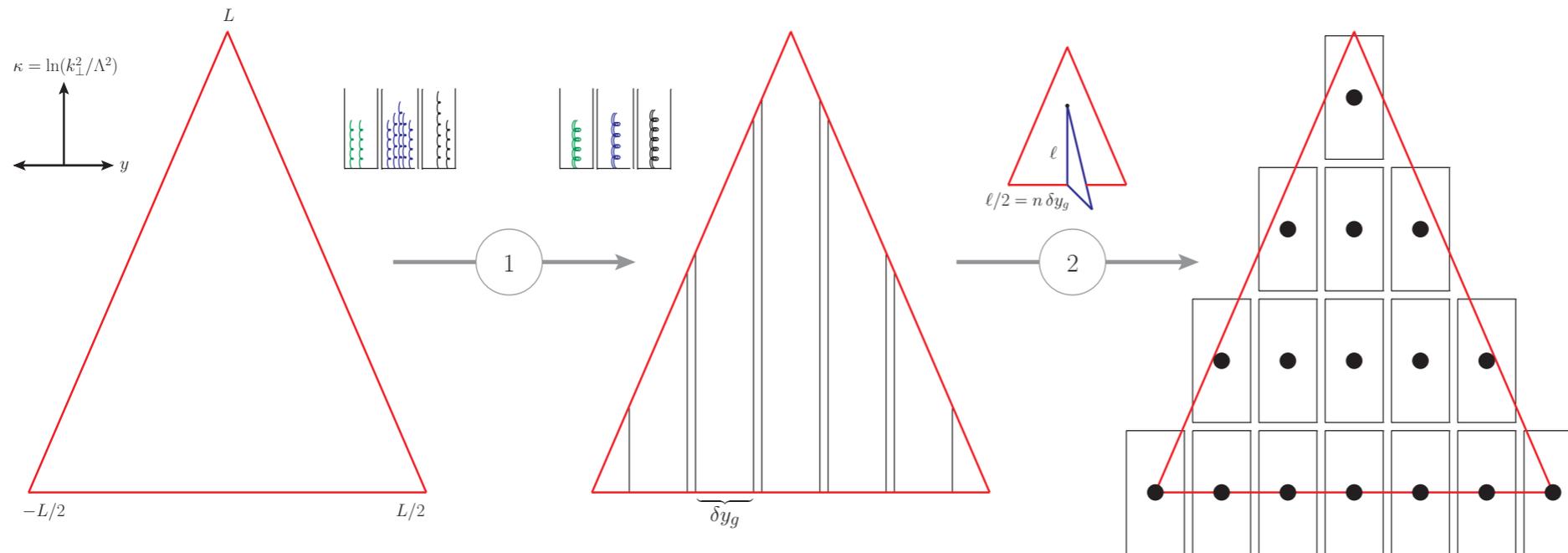


A brief word on Autodiff

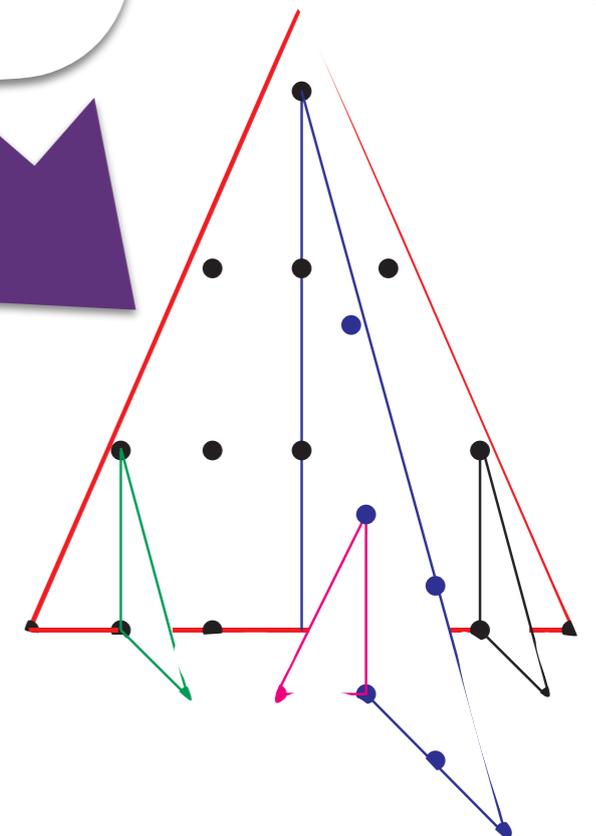


Towards a differential parton shower

104

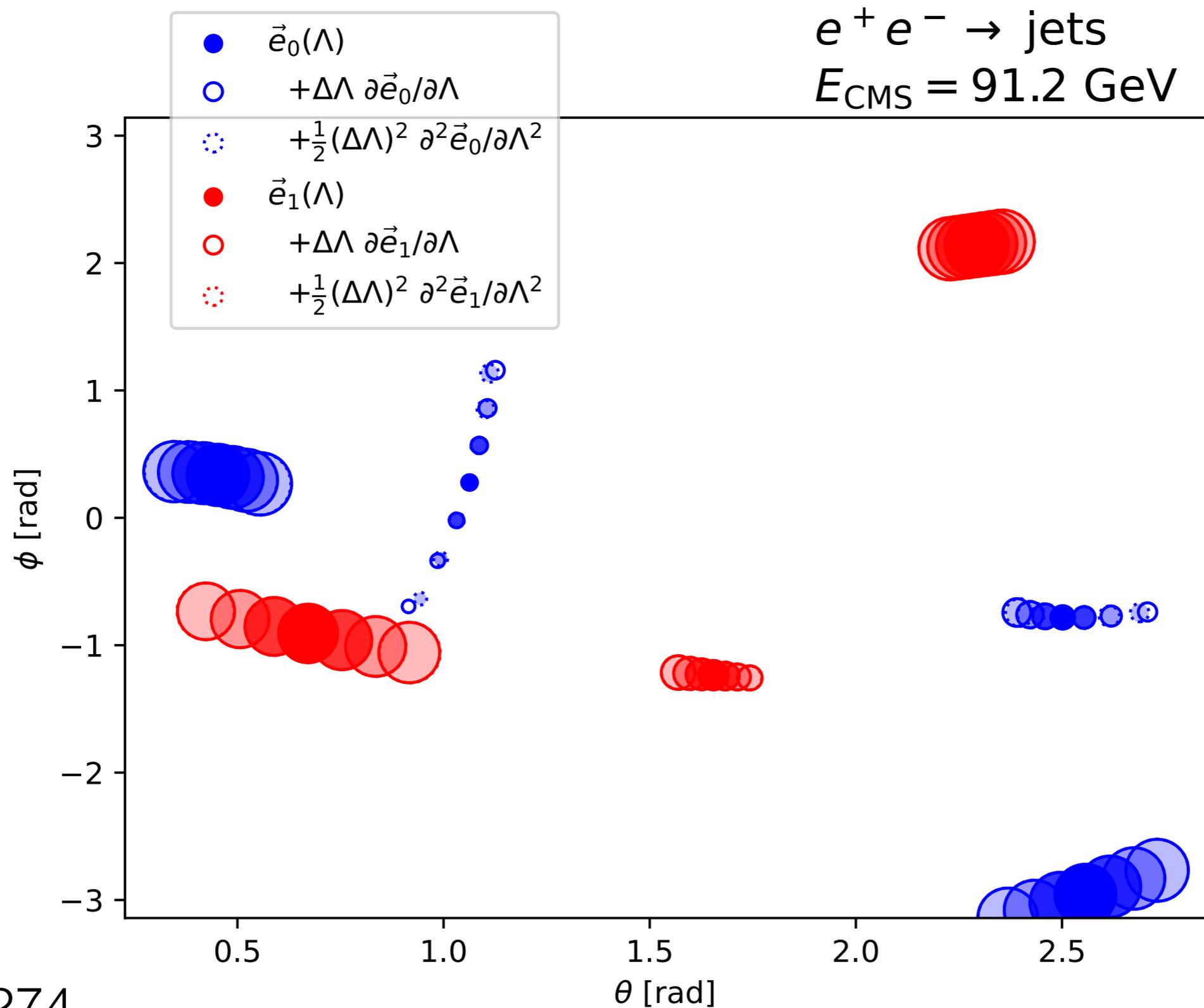


Full parton shower is a bit tricky since variable (unbounded) number of random numbers. Let's start with "Discrete QCD" where the number is fixed.



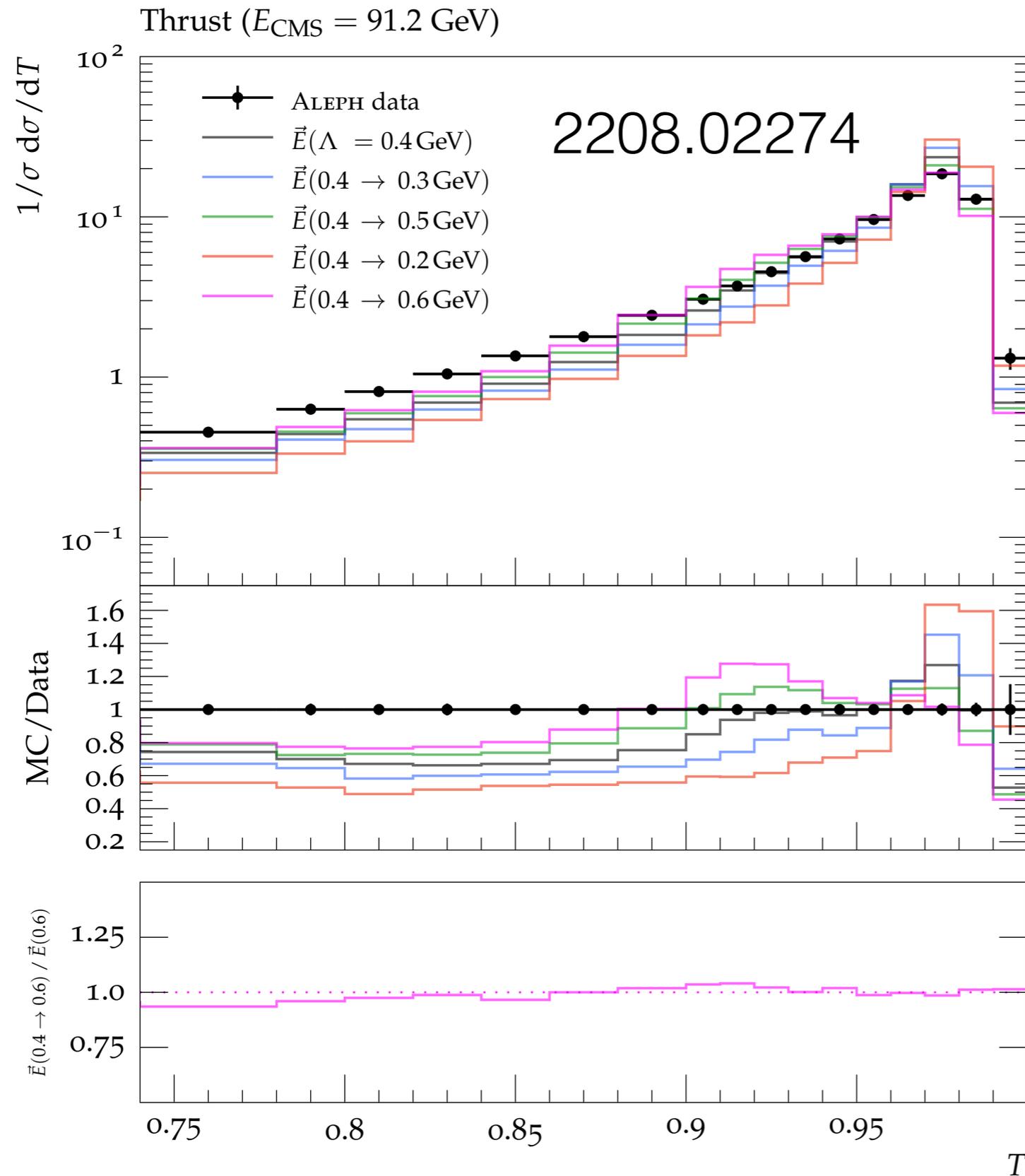
Towards a differential parton shower

105



Towards a differential parton shower

106



As a first test, we show how this can be used to extract the strong coupling constant.

All of these samples have the same random numbers!